

# **Introduction to Programming by MPI for Parallel FEM Report S1 & S2 in Fortran (2/2)**

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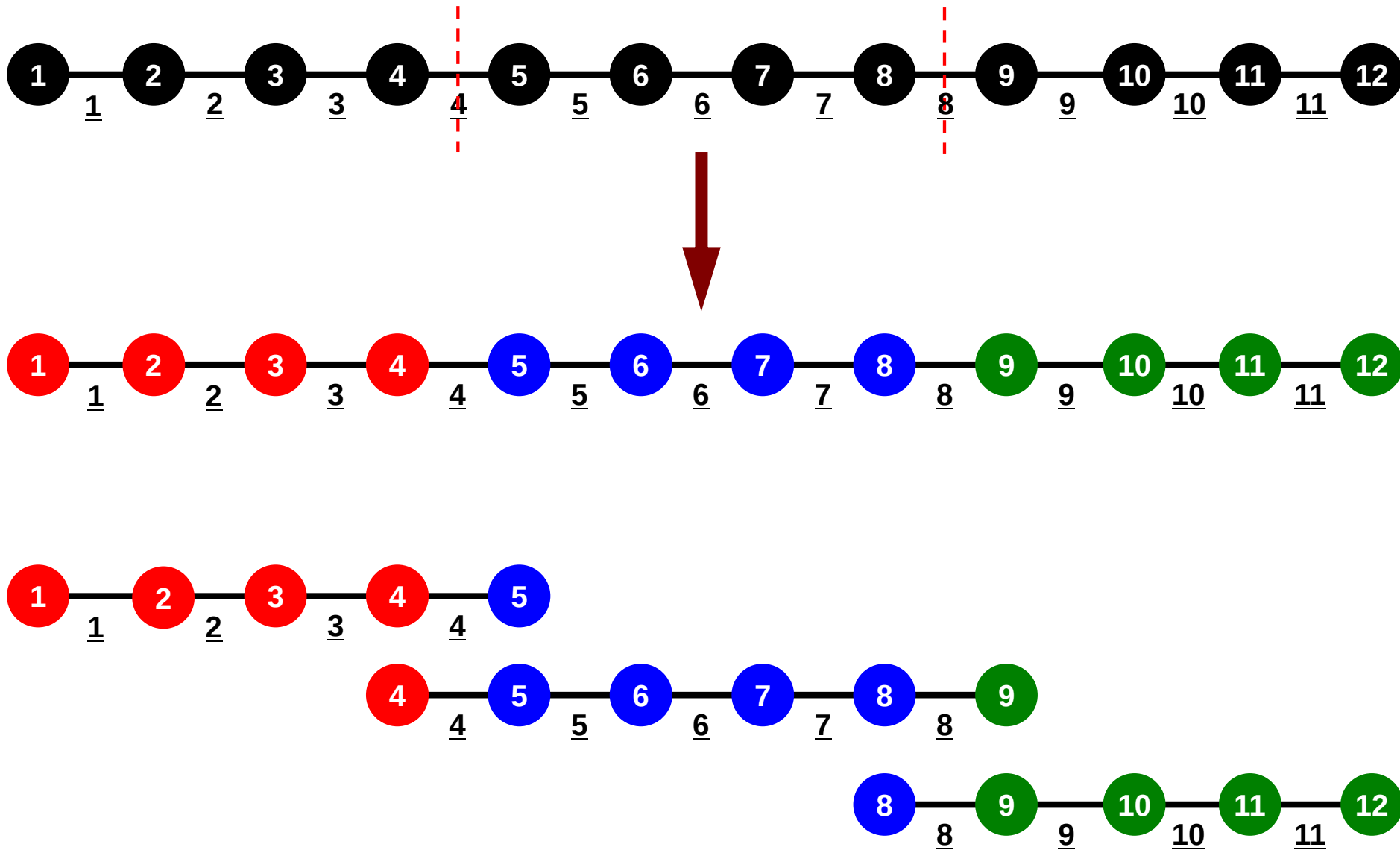
- What is MPI ?
- Your First MPI Program: Hello World
- Collective Communication
- **Point-to-Point Communication**

# Point-to-Point Communicatio

## 1対1通信

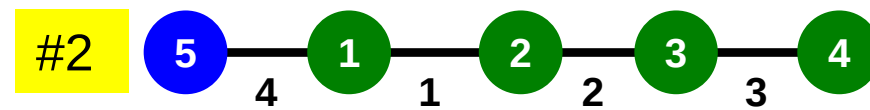
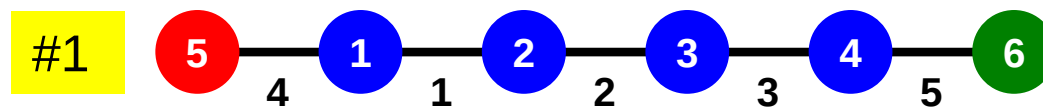
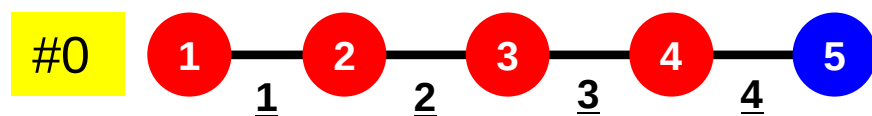
- What is PtoP Communication ?
- 2D Problem, Generalized Communication Table
- Report S2

# 1D FEM: 12 nodes/11 elem's/3 domains



# 1D FEM: 12 nodes/11 elem's/3 domains

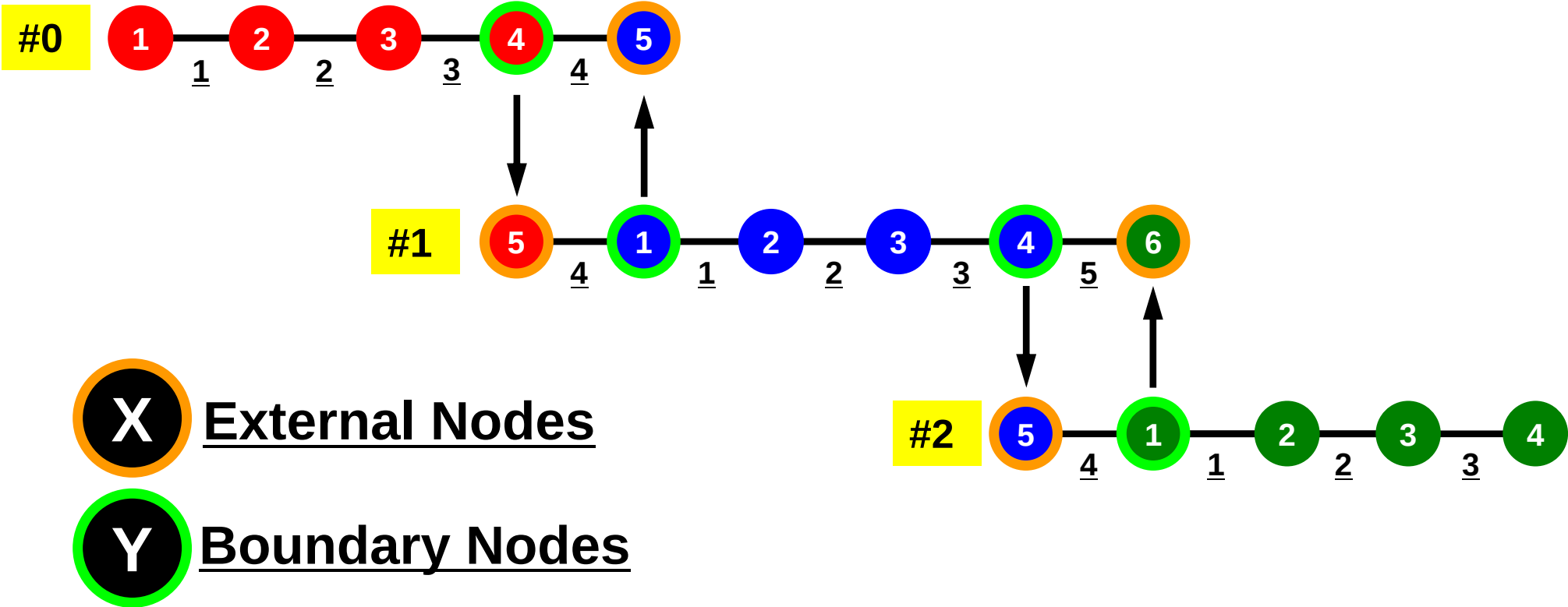
Local ID: Starting from 1 for node and elem at each domain



# 1D FEM: 12 nodes/11 elem's/3 domains

Internal/External/Boundary Nodes

Boundary Nodes: Part of Internal Nodes, and External Nodes of Other Domains



# Preconditioned Conjugate Gradient Method (CG)

```

Compute  $\mathbf{r}^{(0)} = \mathbf{b} - [\mathbf{A}]\mathbf{x}^{(0)}$ 
for i= 1, 2, ...
  solve  $[\mathbf{M}]\mathbf{z}^{(i-1)} = \mathbf{r}^{(i-1)}$ 
   $\rho_{i-1} = \mathbf{r}^{(i-1)} \mathbf{z}^{(i-1)}$ 
  if i=1
     $\mathbf{p}^{(1)} = \mathbf{z}^{(0)}$ 
  else
     $\beta_{i-1} = \rho_{i-1} / \rho_{i-2}$ 
     $\mathbf{p}^{(i)} = \mathbf{z}^{(i-1)} + \beta_{i-1} \mathbf{p}^{(i-1)}$ 
  endif
   $\mathbf{q}^{(i)} = [\mathbf{A}]\mathbf{p}^{(i)}$ 
   $\alpha_i = \rho_{i-1} / \mathbf{p}^{(i)} \mathbf{q}^{(i)}$ 
   $\mathbf{x}^{(i)} = \mathbf{x}^{(i-1)} + \alpha_i \mathbf{p}^{(i)}$ 
   $\mathbf{r}^{(i)} = \mathbf{r}^{(i-1)} - \alpha_i \mathbf{q}^{(i)}$ 
  check convergence  $|\mathbf{r}|$ 
end

```

Preconditioner:

Diagonal Scaling

Point-Jacobi Preconditioning

$$[\mathbf{M}] = \begin{bmatrix} D_1 & 0 & \dots & 0 & 0 \\ 0 & D_2 & & 0 & 0 \\ \dots & & \dots & & \dots \\ 0 & 0 & & D_{N-1} & 0 \\ 0 & 0 & \dots & 0 & D_N \end{bmatrix}$$

# Preconditioning, DAXPY

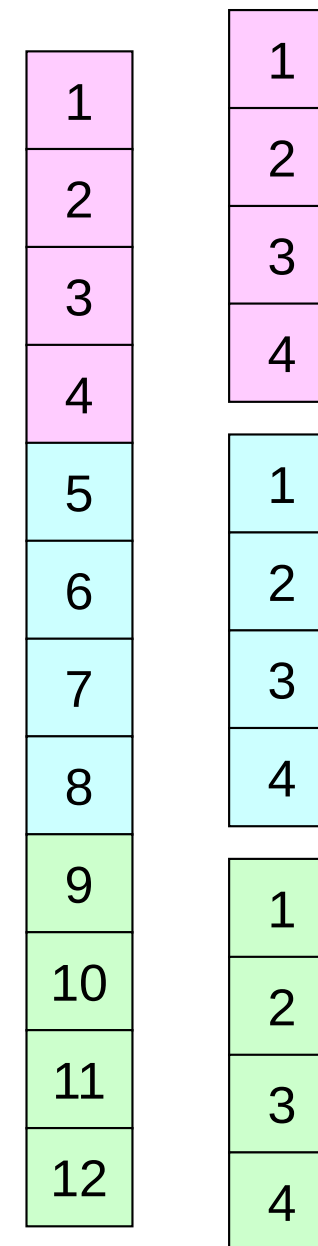
Local Operations by Only Internal Points: Parallel Processing is possible

```
!C
!C-- {z}= [Minv]{r}

do i= 1, N
  W(i,Z)= W(i,DD) * W(i,R)
enddo
```

```
!C
!C-- {x}= {x} + ALPHA*{p}      DAXPY: double a{x} plus {y}
!C  {r}= {r} - ALPHA*{q}

do i= 1, N
  PHI(i)= PHI(i) + ALPHA * W(i,P)
  W(i,R)= W(i,R) - ALPHA * W(i,Q)
enddo
```

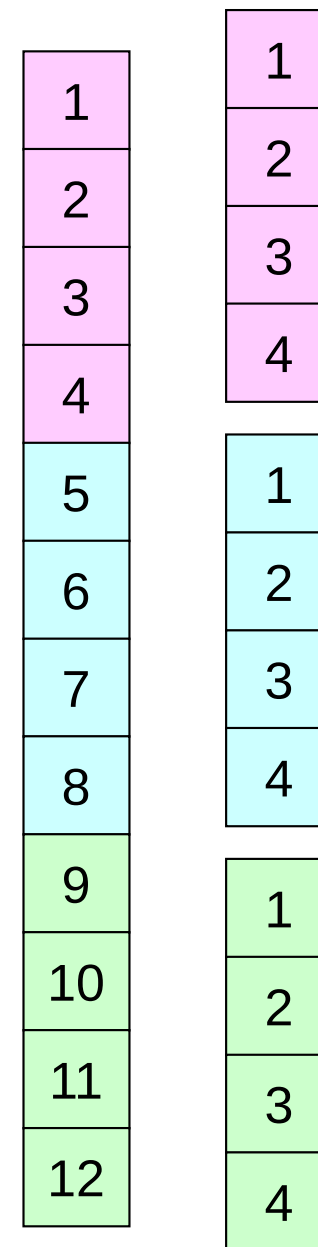


# Dot Products

Global Summation needed: Communication ?

```
!C
!C-- ALPHA= RHO / {p} {q}

C1= 0. d0
do i= 1, N
  C1= C1 + W(i, P)*W(i, Q)
enddo
ALPHA= RHO / C1
```



# Matrix-Vector Products

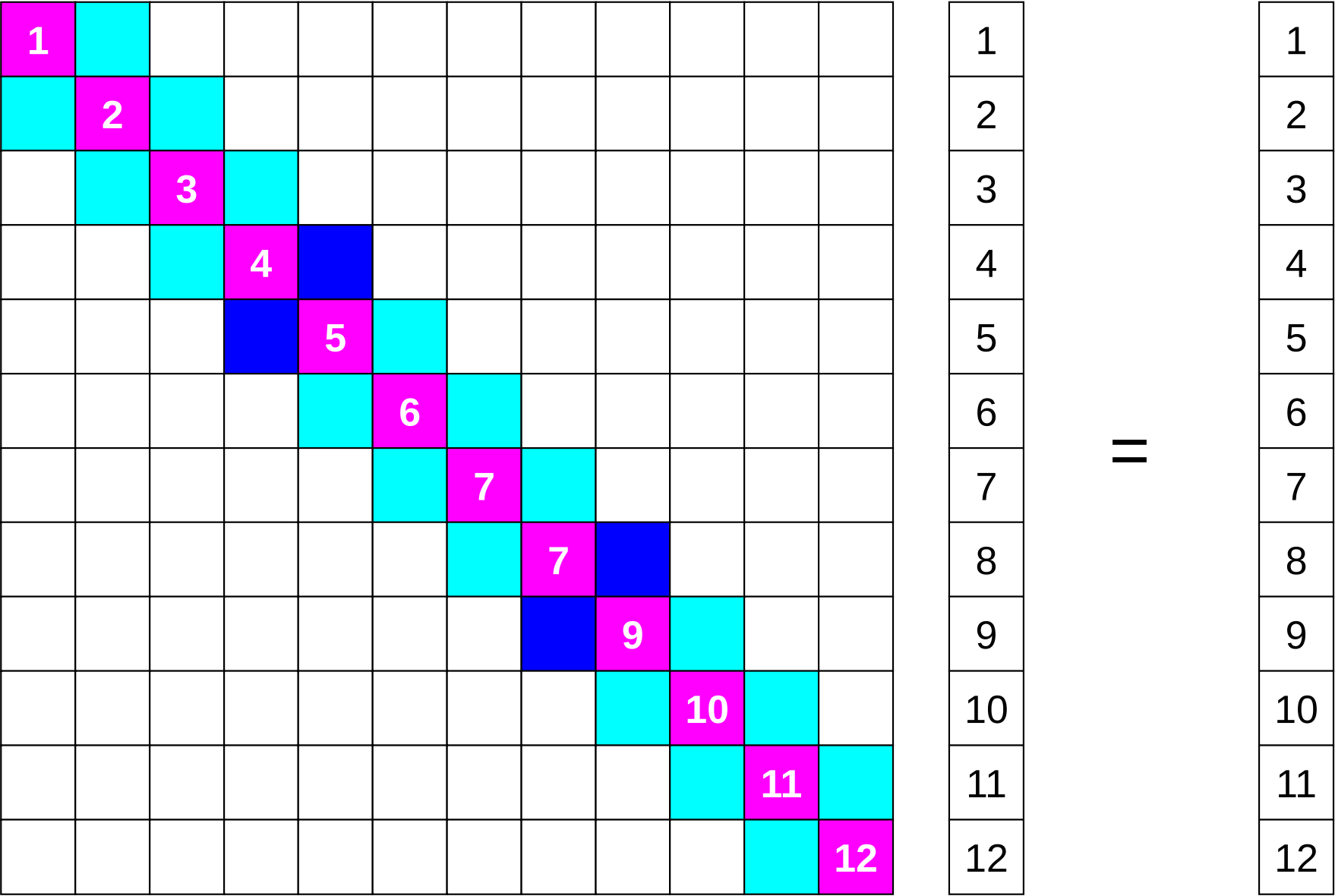
## Values at External Points: P-to-P Communication

```
!C
!C-- {q} = [A] {p}

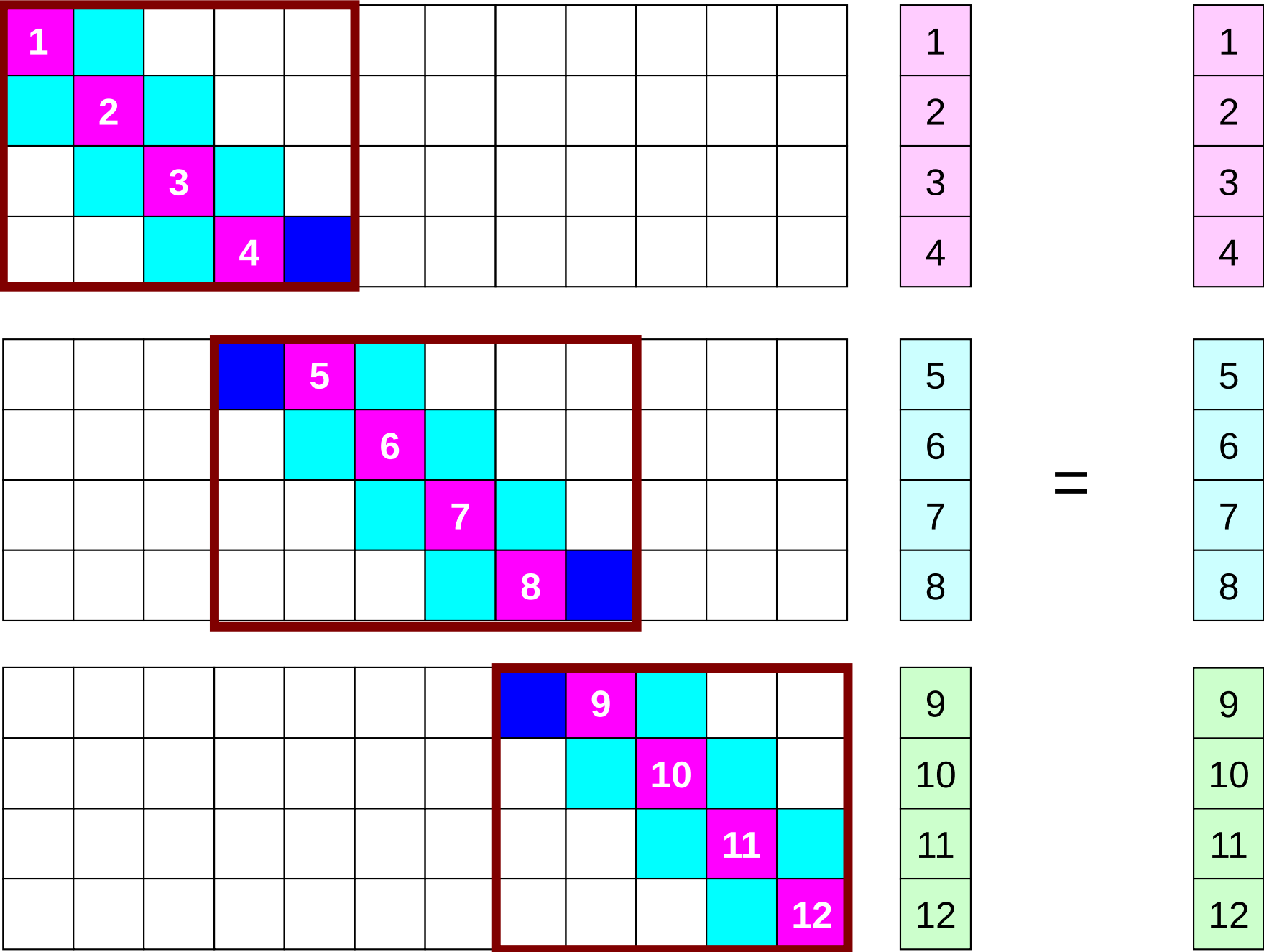
do i= 1, N
  W(i, Q) = DIAG(i)*W(i, P)
  do j= INDEX(i-1)+1, INDEX(i)
    W(i, Q) = W(i, Q) + AMAT(j)*W(ITEM(j), P)
  enddo
enddo
```



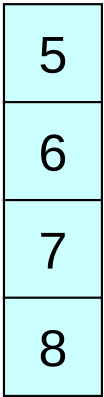
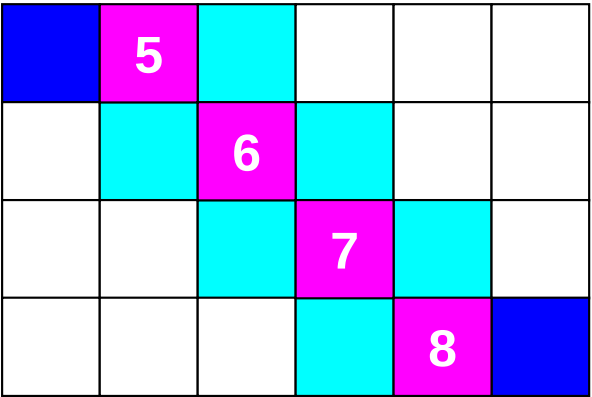
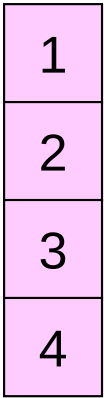
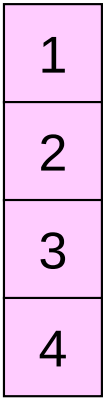
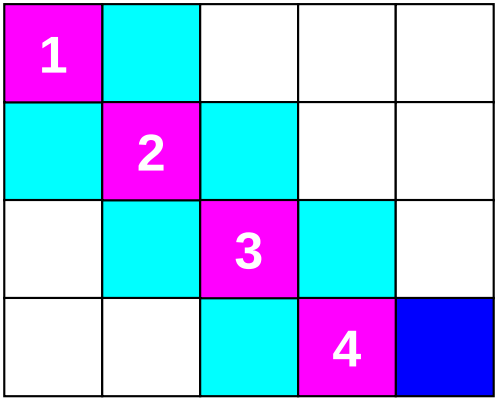
# Mat-Vec Products: Local Op. Possible



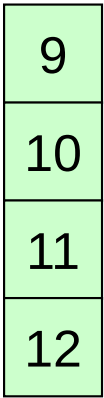
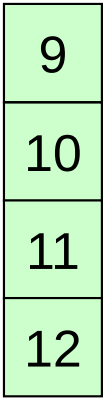
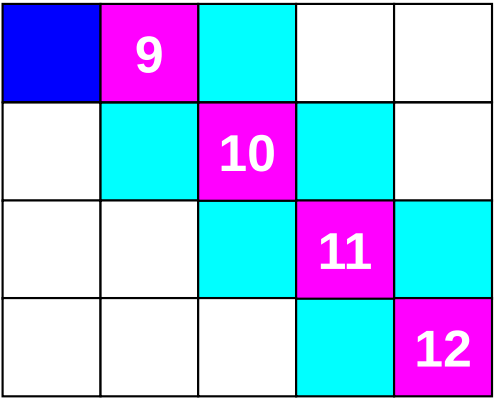
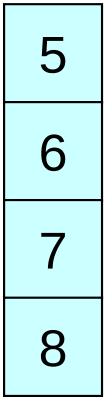
# Mat-Vec Products: Local Op. Possible



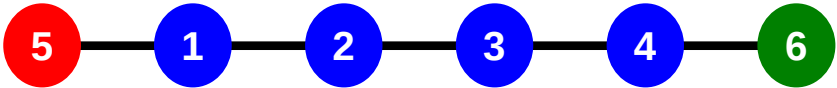
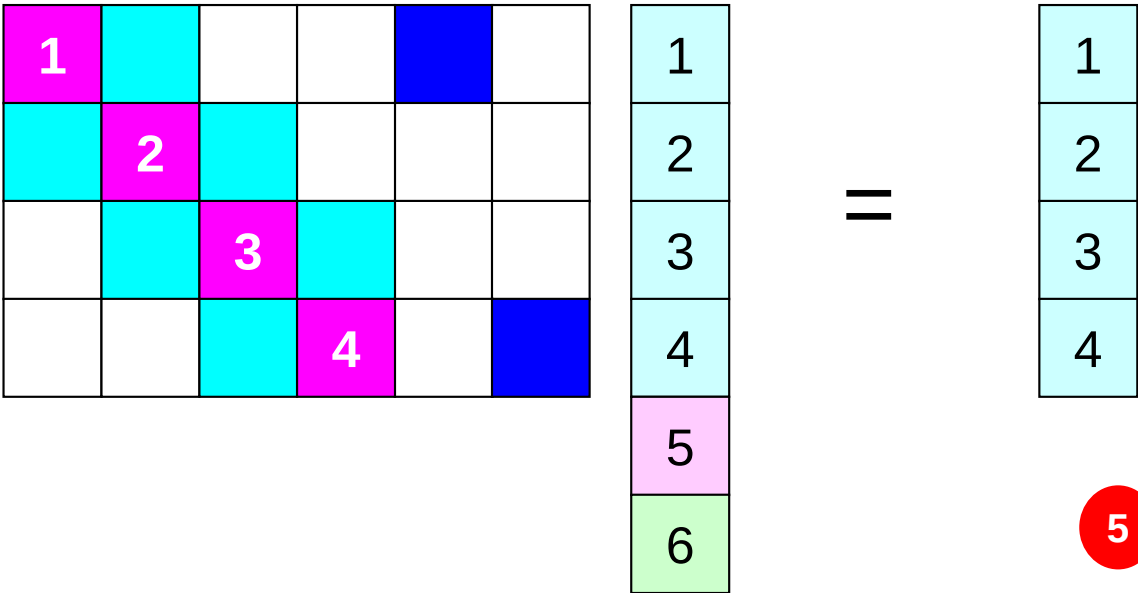
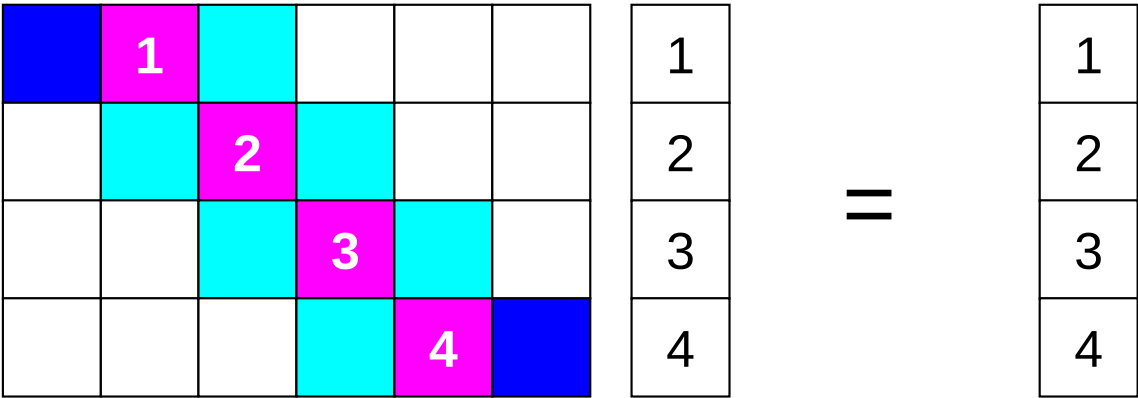
# Mat-Vec Products: Local Op. Possible



=



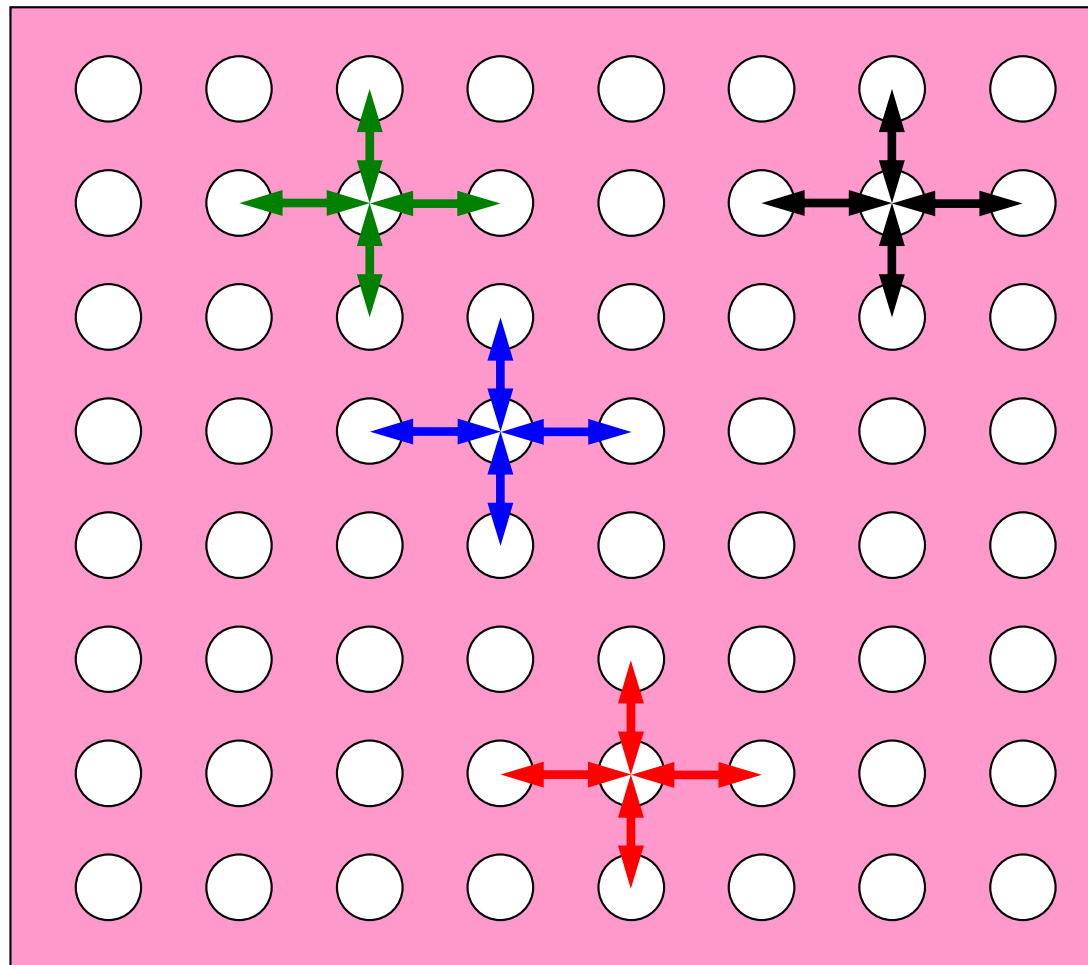
# Mat-Vec Products: Local Op. #1





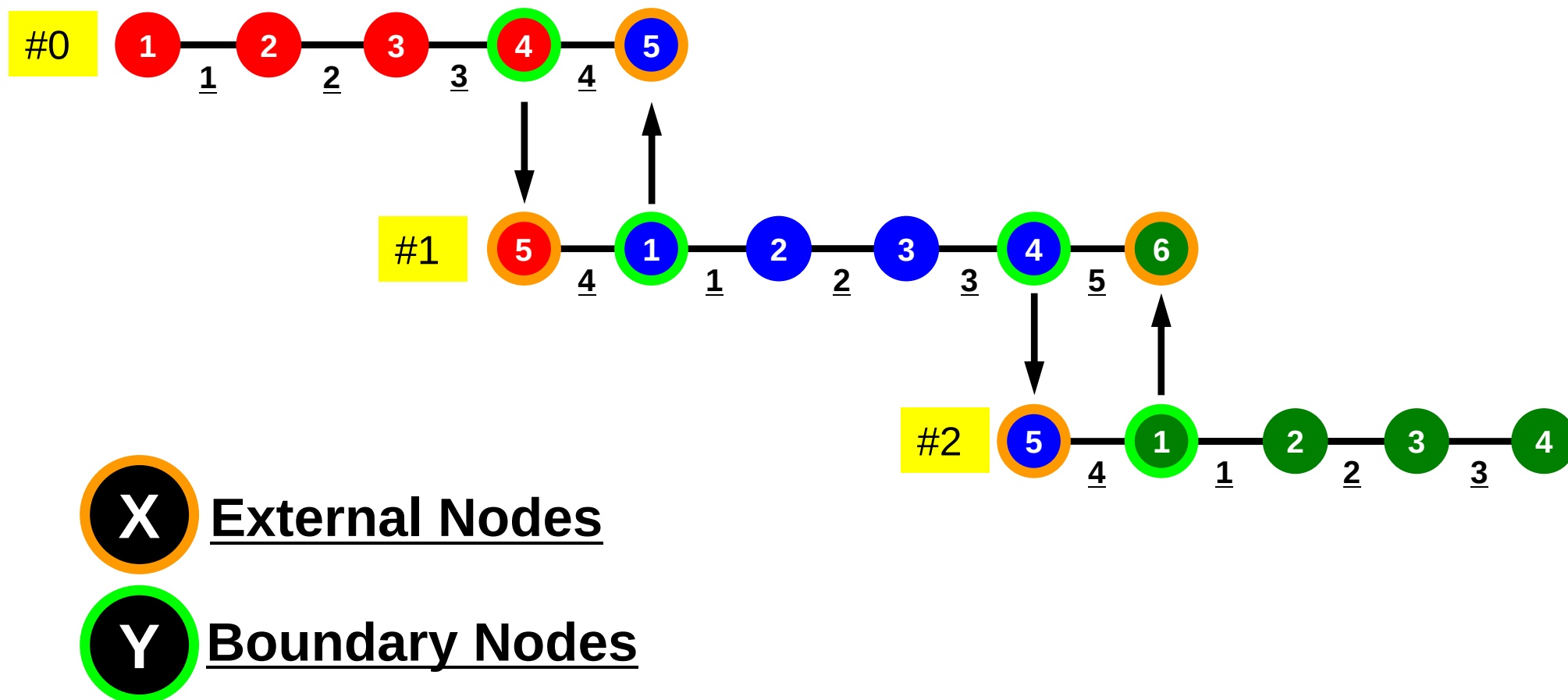
# Collective/PtoP Communications

Interactions with only Neighboring Processes/Element  
Finite Difference Method (FDM), Finite Element  
Method (FEM)



# When do we need PtoP comm.: 1D-FEM

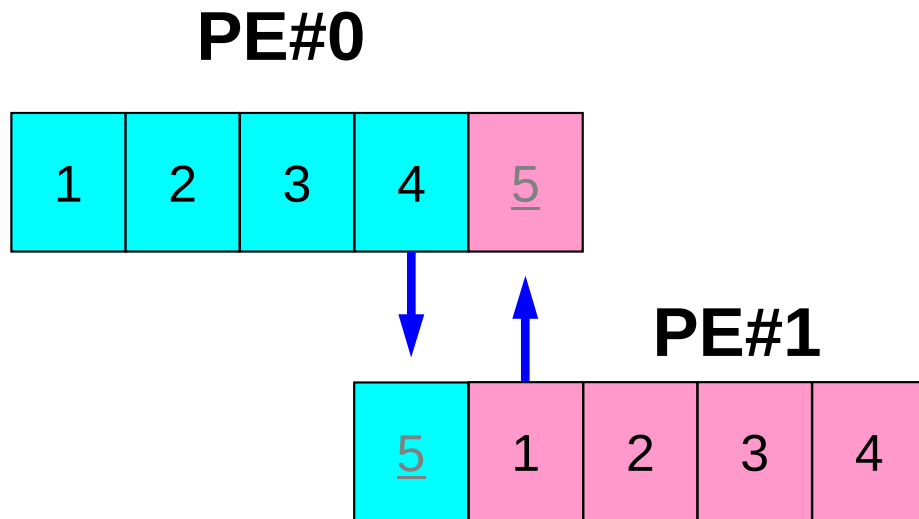
Info in neighboring domains is required for FEM operations  
Matrix assembling, Iterative Method



# Method for P-to-P Comm.

- **MPI\_Send, MPI\_Recv**
- These are “blocking” functions.
  - “Dead lock” occurs for these “blocking” functions.
- A “blocking” MPI call means that the program execution will be suspended until the message buffer is safe to use.
- The MPI standards specify that a blocking SEND or RECV does not return until the send buffer is safe to reuse (for MPI\_Send), or the receive buffer is ready to use (for MPI\_Recv).
  - Blocking comm. confirms “secure” communication, but it is very inconvenient and impractical.
- Please just remember that “there are such functions”.

# MPI\_Send/MPI\_Recv



```
if (my_rank.eq.0) NEIB_ID=1
if (my_rank.eq.1) NEIB_ID=0

...
call MPI_SEND (NEIB_ID, arg's)
call MPI_RECV (NEIB_ID, arg's)
...
```

- This seems reasonable, but it stops at MPI\_Send/MPI\_Recv.
  - Sometimes it works (according to implementation).
- “Sending 0-to-1” does not terminate, until “Receiving@1-from-0” is done.
  - But, “Sending 1-to-0” does not terminate, if “Receiving@0-from-1” is not done.

# MPI\_Send/MPI\_Recv

## PE#0

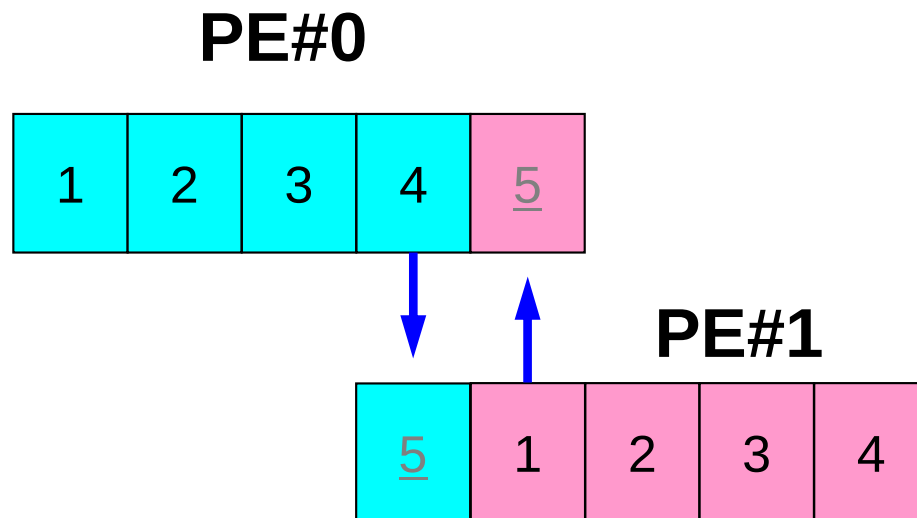
```
call MPI_SEND (NEIB_ID, arg's)  
call MPI_RECV (NEIB_ID, arg's)
```

## PE#1

```
call MPI_SEND (NEIB_ID, arg's)  
call MPI_RECV (NEIB_ID, arg's)
```

- Both of PE#0 and PE#1 are “sending”
- “Sending” does not terminate, if “receiving” at destination is not completed
- Both of PE#0 and PE#1 are waiting for completion of “receiving” after “sending” -> Processes stop

# MPI\_Send/MPI\_Recv (cont.)



```
if (my_rank.eq.0) NEIB_ID=1
if (my_rank.eq.1) NEIB_ID=0

...
if (my_rank.eq.0) then
  call MPI_SEND (NEIB_ID, arg's)
  call MPI_RECV (NEIB_ID, arg's)
endif

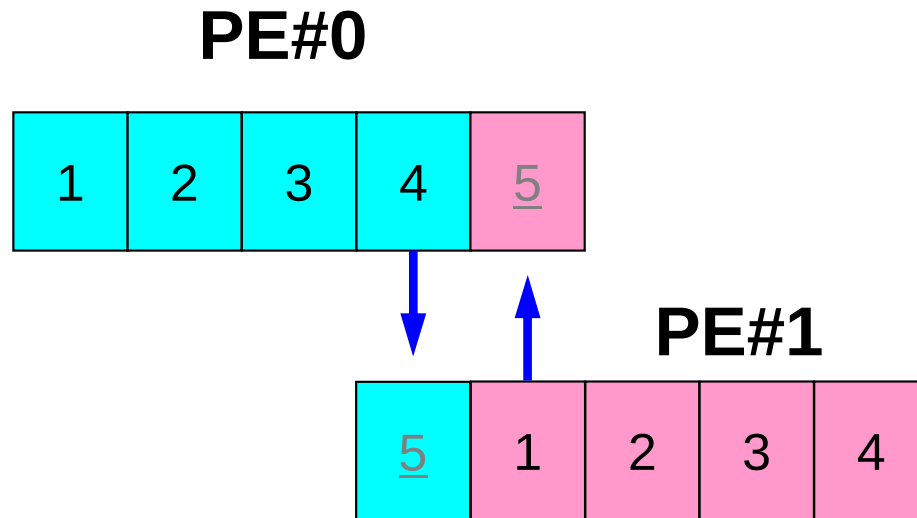
if (my_rank.eq.1) then
  call MPI_RECV (NEIB_ID, arg's)
  call MPI_SEND (NEIB_ID, arg's)
endif

...
```

- It works.
- It is OK for Structured Meshes for FDM (Finite Difference Method).

# How to do PtoP Comm. ?

- Using “non-blocking” functions **MPI\_Isend** & **MPI\_Irecv** together with **MPI\_Waitall** for synchronization
- **MPI\_Sendrecv** is also available.



```
if (my_rank.eq.0) NEIB_ID=1
if (my_rank.eq.1) NEIB_ID=0

...
call MPI_Isend (NEIB_ID, arg's)
call MPI_Irecv (NEIB_ID, arg's)
...
call MPI_Waitall (for Irecv)
...
call MPI_Waitall (for Isend)
```

**MPI\_Waitall** for both of  
**MPI\_Isend/MPI\_Irecv** is possible

# MPI\_ISEND

- Begins a non-blocking send
  - Send the contents of sending buffer (starting from **sendbuf**, number of messages: **count**) to **dest** with **tag** .
  - Contents of sending buffer cannot be modified before calling corresponding **MPI\_Waitall**.

- **call MPI\_ISEND**

**(sendbuf, count, datatype, dest, tag, comm, request, ierr)**

- |                                                                                                                                                                                          |        |   |                                                 |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------|---|-------------------------------------------------|
| – <u>sendbuf</u>                                                                                                                                                                         | choice | I | starting address of sending buffer              |
| – <u>count</u>                                                                                                                                                                           | I      | I | number of elements sent to each process         |
| – <u>datatype</u>                                                                                                                                                                        | I      | I | data type of elements of sending buffer         |
| – <u>dest</u>                                                                                                                                                                            | I      | I | rank of destination                             |
| – <u>tag</u>                                                                                                                                                                             | I      | I | message tag                                     |
| This integer can be used by the application to distinguish messages. Communication occurs if tag's of MPI_Isend and MPI_Irecv are matched. Usually tag is set to be "0" (in this class), |        |   |                                                 |
| – <u>comm</u>                                                                                                                                                                            | I      | I | communicator                                    |
| – <u>request</u>                                                                                                                                                                         | I      | 0 | communication request array used in MPI_Waitall |
| – <u>ierr</u>                                                                                                                                                                            | I      | 0 | completion code                                 |

# Communication Request: request

## 通信識別子

- call MPI\_ISEND

(sendbuf, count, datatype, dest, tag, comm, request, ierr)

- |                   |        |   |                                                                                                                                                                                          |
|-------------------|--------|---|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| – <u>sendbuf</u>  | choice | I | starting address of sending buffer                                                                                                                                                       |
| – <u>count</u>    | I      | I | number of elements sent to each process                                                                                                                                                  |
| – <u>datatype</u> | I      | I | data type of elements of sending buffer                                                                                                                                                  |
| – <u>dest</u>     | I      | I | rank of destination                                                                                                                                                                      |
| – <u>tag</u>      | I      | I | message tag                                                                                                                                                                              |
|                   |        |   | This integer can be used by the application to distinguish messages. Communication occurs if tag's of MPI_Isend and MPI_Irecv are matched. Usually tag is set to be "0" (in this class), |
| – <u>comm</u>     | I      | I | communicator                                                                                                                                                                             |
| – <u>request</u>  | I      | 0 | communication request used in MPI_Waitall<br>Size of the array is total number of neighboring processes                                                                                  |
| – <u>ierr</u>     | I      | 0 | completion code                                                                                                                                                                          |

- Just define the array

```
allocate (request(NEIBPETOT))
```

# MPI\_Irecv

- Begins a non-blocking receive
  - Receiving the contents of receiving buffer (starting from **recvbuf**, number of messages: **count**) from **source** with **tag** .
  - Contents of receiving buffer cannot be used before calling corresponding **MPI\_Waitall**.

- **call MPI\_Irecv**  
**(recvbuf, count, datatype, dest, tag, comm, request, ierr)**

|                                                                                                                                            |        |   |                                           |
|--------------------------------------------------------------------------------------------------------------------------------------------|--------|---|-------------------------------------------|
| – <u>recvbuf</u>                                                                                                                           | choice | I | starting address of receiving buffer      |
| – <u>count</u>                                                                                                                             | I      | I | number of elements in receiving buffer    |
| – <u>datatype</u>                                                                                                                          | I      | I | data type of elements of receiving buffer |
| – <u>source</u>                                                                                                                            | I      | I | rank of source                            |
| – <u>tag</u>                                                                                                                               | I      | I | message tag                               |
| This integer can be used by the application to distinguish messages. Communication occurs if tag's of MPI_Isend and MPI_Irecv are matched. |        |   |                                           |
| Usually tag is set to be "0" (in this class),                                                                                              |        |   |                                           |
| – <u>comm</u>                                                                                                                              | I      | I | communicator                              |
| – <u>request</u>                                                                                                                           | I      | 0 | communication request used in MPI_Waitall |
| – <u>ierr</u>                                                                                                                              | I      | 0 | completion code                           |

# MPI\_WAITALL

- **MPI\_Waitall** blocks until all comm's, associated with request in the array, complete. It is used for terminating MPI\_Isend and MPI\_Irecv.
- At sending phase, contents of sending buffer cannot be modified before calling corresponding **MPI\_Waitall**. At receiving phase, contents of receiving buffer cannot be used before calling corresponding **MPI\_Waitall**.
- MPI\_Isend and MPI\_Irecv can be synchronized simultaneously with a single **MPI\_Waitall** if it is consistent.
  - Same request should be used in MPI\_Isend and MPI\_Irecv.
- Its operation is similar to that of **MPI\_Barrier** but, **MPI\_Waitall** can not be replaced by **MPI\_Barrier**.
  - Possible troubles using **MPI\_Barrier** instead of **MPI\_Waitall**: Contents of **request** and **status** are not updated properly, very slow operations etc.
- **call MPI\_WAITALL (count, request, status, ierr)**
  - count      I            I            number of processes to be synchronized
  - request    I            I/O        comm. request used in MPI\_Waitall (array size: count)
  - status     I            0            array of status objects  
MPI\_STATUS\_SIZE: defined in 'mpif.h', 'mpi.h'
  - ierr        I            0            completion code

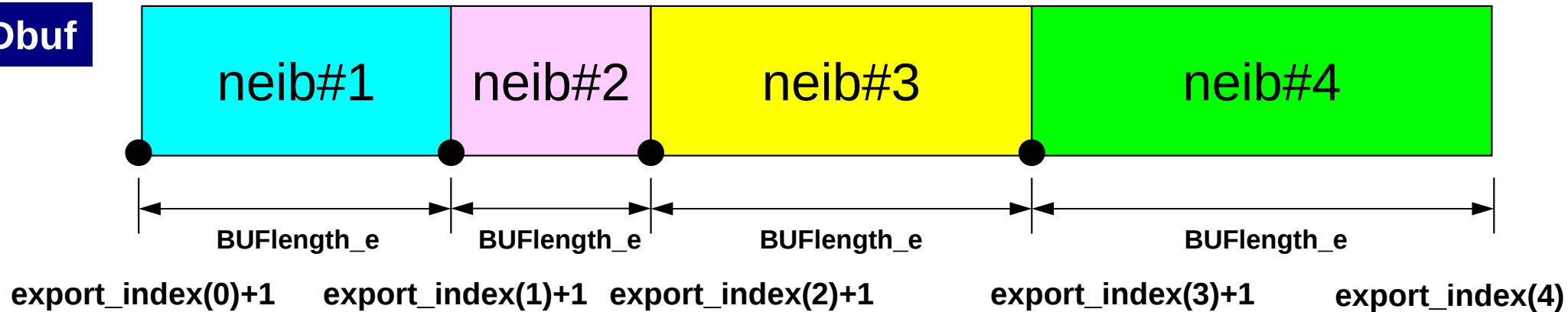
# Array of status object: status 状況オブジェクト配列

- **call MPI\_WAITALL (count, request, status, ierr)**
  - count    I        I        number of processes to be synchronized
  - request   I        I/O     comm. request used in MPI\_Waitall (array size: count)
  - status    I        0        array of status objects  
MPI\_STATUS\_SIZE: defined in 'mpif.h', 'mpi.h'
  - ierr       I        0        completion code
- Just define the array

```
allocate (stat(MPI_STATUS_SIZE, NEIBPETOT))
```

# SEND: MPI\_Isend/Irecv/Waitall

**SENDbuf**



```
do neib= 1, NEIBPETOT
```

```
  iS_e= export_index(neib-1) + 1
```

```
  iE_e= export_index(neib )
```

```
  BUFlength_e= iE_e + 1 - iS_e
```

```
  call MPI_ISEND
```

```
&      (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER,
```

```
&      NEIBPE(neib), 0, MPI_COMM_WORLD,
```

```
&      request_send(neib), ierr)
```

```
enddo
```

```
call MPI_WAITALL (NEIBPETOT, request_send, stat_send, ierr)
```

# RECV: MPI\_Isend/Irecv/Waitall

```
do neib= 1, NEIBPETOT
```

```
  iS_i= import_index(neib-1) + 1
```

```
  iE_i= import_index(neib )
```

```
  BUFlength_i= iE_i + 1 - iS_i
```

```
  call MPI_Irecv
```

```
&      (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER,
```

```
&      &
```

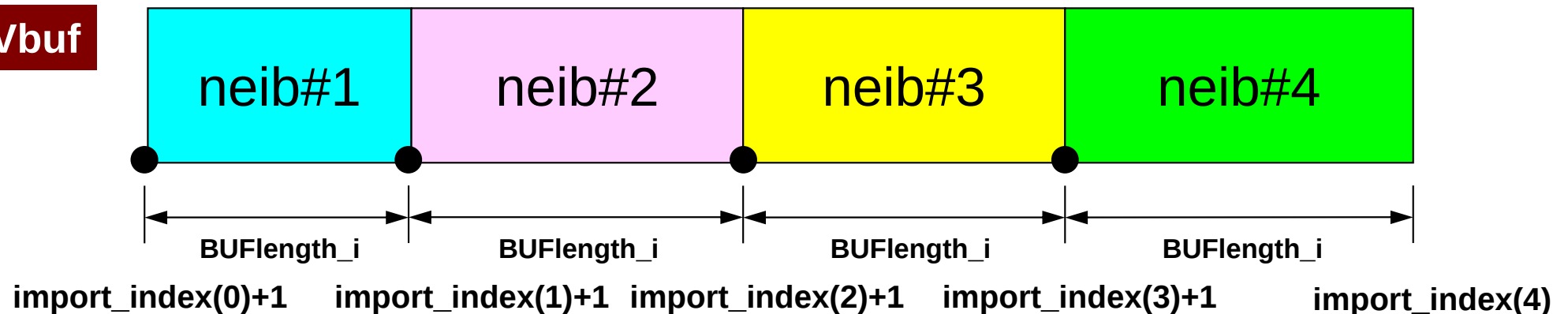
```
      NEIBPE(neib), 0, MPI_COMM_WORLD,
```

```
      request_recv(neib), ierr)
```

```
enddo
```

```
call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)
```

**RECVbuf**



# MPI\_SENDRECV

- MPI\_Send+MPI\_Recv: not recommended, many restrictions
- **call MPI\_SENDRECV**  
**(sendbuf, sendcount, sendtype, dest, sendtag, recvbuf, recvcount, recvtype, source, recvtag, comm, status, ierr)**

|                    |        |   |                                                                          |
|--------------------|--------|---|--------------------------------------------------------------------------|
| – <u>sendbuf</u>   | choice | I | starting address of sending buffer                                       |
| – <u>sendcount</u> | I      | I | number of elements in sending buffer                                     |
| – <u>sendtype</u>  | I      | I | datatype of each sending buffer element                                  |
| – <u>dest</u>      | I      | I | rank of destination                                                      |
| – <u>sendtag</u>   | I      | I | message tag for sending                                                  |
| – <u>comm</u>      | I      | I | communicator                                                             |
| – <u>recvbuf</u>   | choice | I | starting address of receiving buffer                                     |
| – <u>recvcount</u> | I      | I | number of elements in receiving buffer                                   |
| – <u>recvtype</u>  | I      | I | datatype of each receiving buffer element                                |
| – <u>source</u>    | I      | I | rank of source                                                           |
| – <u>recvtag</u>   | I      | I | message tag for receiving                                                |
| – <u>comm</u>      | I      | I | communicator                                                             |
| – <u>status</u>    | I      | 0 | array of status objects<br>MPI_STATUS_SIZE: defined in 'mpif.h', 'mpi.h' |
| – <u>ierr</u>      | I      | 0 | completion code                                                          |

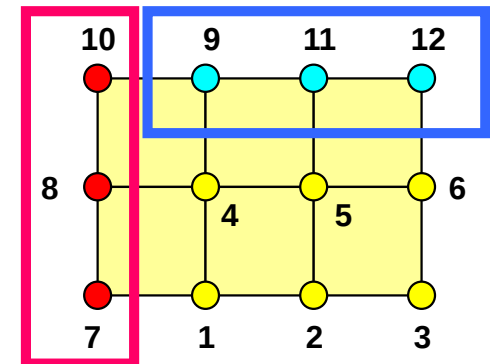
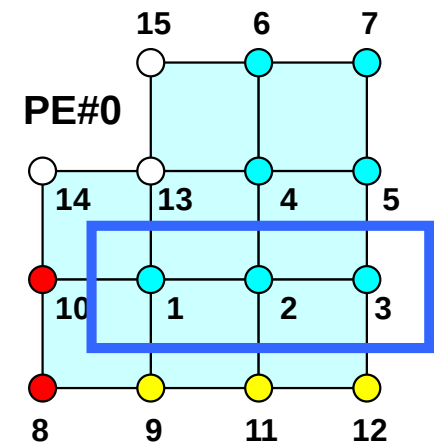
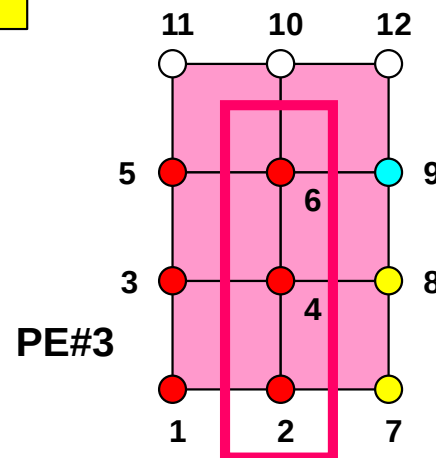
# RECV: receiving to external nodes

Recv. continuous data to recv. buffer from neighbors

- **MPI\_Irecv**

(recvbuf, count, datatype, dest, tag, comm, request)

- **recvbuf** choice I starting address of receiving buffer
- **count** I I number of elements in receiving buffer
- **datatype** I I data type of elements of receiving buffer
- **source** I I rank of source



PE#2

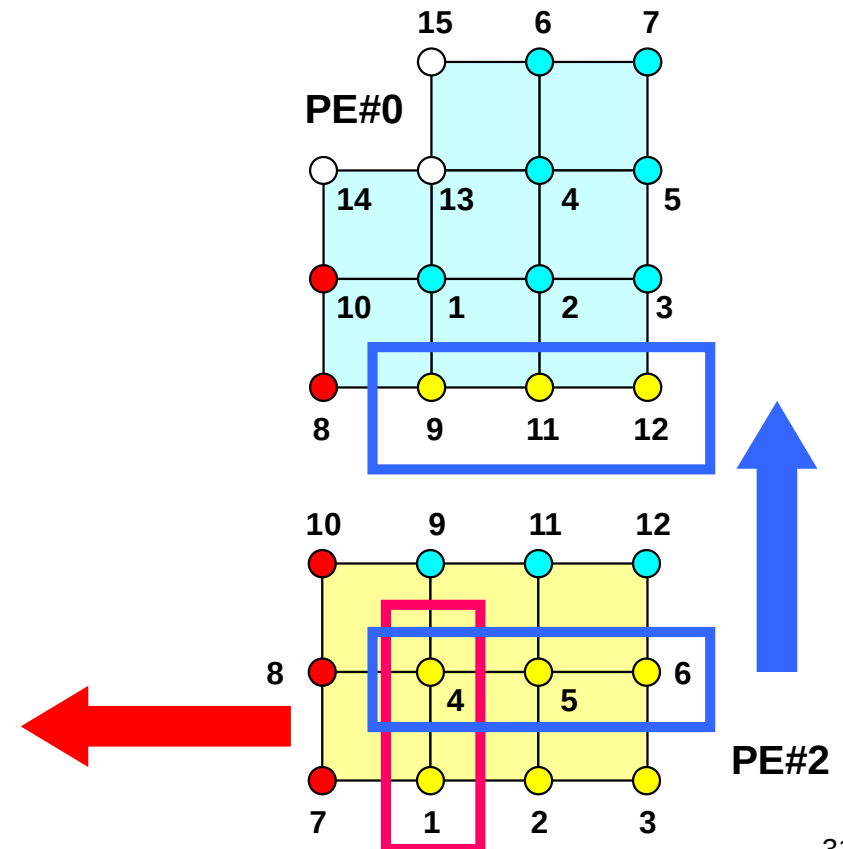
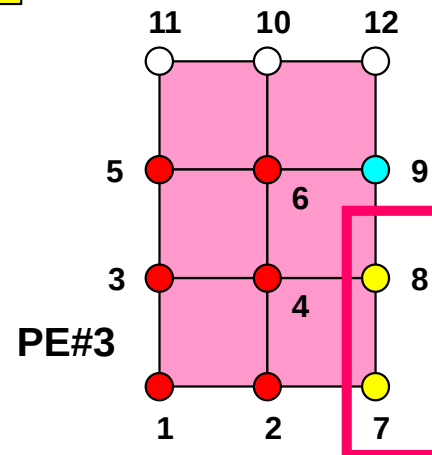
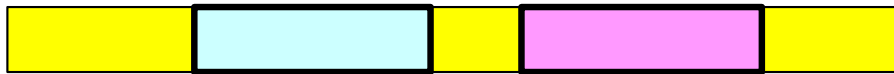
# SEND: sending from boundary nodes

Send continuous data to send buffer of neighbors

- **MPI\_Isend**

(**sendbuf**, **count**, **datatype**, **dest**, **tag**, **comm**, **request**)

- **sendbuf** choice I starting address of sending buffer
- **count** I I number of elements sent to each process
- **datatype** I I data type of elements of sending buffer
- **dest** I I rank of destination



# Request, Status in Fortran

- **MPI\_Isend: request**
- **MPI\_Irecv: request**
- **MPI\_Waitall: request, status**

```
integer request(NEIBPETOT)  
integer status (MPI_STAUTS_SIZE,NEIBPETOT)
```

- **MPI\_Sendrecv: status**

```
integer status (MPI_STATUS_SIZE)
```

# Files on Odyssey

## Fortran

```
>$ cd /work/gt36/t36XXX/pFEM/  
>$ module load fj  
>$ cp /work/gt00/z30088/pFEM/F/s2-f.tar .  
>$ tar xvf s2-f.tar
```

## C

```
>$ cd /work/gt36/t36XXX/pFEM/  
>$ module load fj  
>$ cp /work/gt00/home/z30088/pFEM/C/s2-c.tar .  
>$ tar xvf s2-c.tar
```

## Confirmation

```
>$ ls  
mpi  
  
>$ cd mpi/S2
```

This directory is called as <\$0-S2>.

<\$0-S2> = <\$0-TOP>/mpi/S2

# Ex.1: Send-Recv a Scalar

- Exchange VAL (real, 8-byte) between PE#0 & PE#1

```

if (my_rank.eq.0) NEIB= 1
if (my_rank.eq.1) NEIB= 0

call MPI_Isend (VAL , 1, MPI_DOUBLE_PRECISION, NEIB, ..., req_send(1), ...)
call MPI_Irecv (VALtemp, 1, MPI_DOUBLE_PRECISION, NEIB, ..., req_recv(1), ...)
call MPI_Waitall (... , req_recv, stat_recv, ...) Recv.buf VALtemp can be used
call MPI_Waitall (... , req_send, stat_send, ...) Send buf VAL can be modified
VAL= VALtemp

```

```

if (my_rank.eq.0) NEIB= 1
if (my_rank.eq.1) NEIB= 0

call MPI_Sendrecv (VAL , 1, MPI_DOUBLE_PRECISION, NEIB, ... &
                  VALtemp, 1, MPI_DOUBLE_PRECISION, NEIB, ..., status, ...)
VAL= VALtemp

```

Name of recv. buffer could be "VAL", but not recommended.

# Ex.1: Send-Recv a Scalar

## Isend/Irecv/Waitall

```
$> cd /work/gt36/t36XXX/pFEM/mpi/S2
$> module load fj
$> mpifrtpx -Kfast ex1-1.f
$> pjsub go2.sh
```

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer(kind=4) :: my_rank, PETOT, NEIB
real (kind=8) :: VAL, VALtemp
integer(kind=4), dimension(MPI_STATUS_SIZE,1) :: stat_send, stat_recv
integer(kind=4), dimension(1) :: request_send, request_recv

call MPI_INIT (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

if (my_rank.eq.0) then
  NEIB= 1
  VAL = 10.d0
else
  NEIB= 0
  VAL = 11.d0
endif

call MPI_ISEND (VAL, 1,MPI_DOUBLE_PRECISION,NEIB,0,MPI_COMM_WORLD,request_send(1),ierr)
call MPI_IRecv (VALx,1,MPI_DOUBLE_PRECISION,NEIB,0,MPI_COMM_WORLD,request_recv(1),ierr)
call MPI_WAITALL (1, request_recv, stat_recv, ierr)
call MPI_WAITALL (1, request_send, stat_send, ierr)
VAL= VALx

call MPI_FINALIZE (ierr)
end
```

# go2.sh

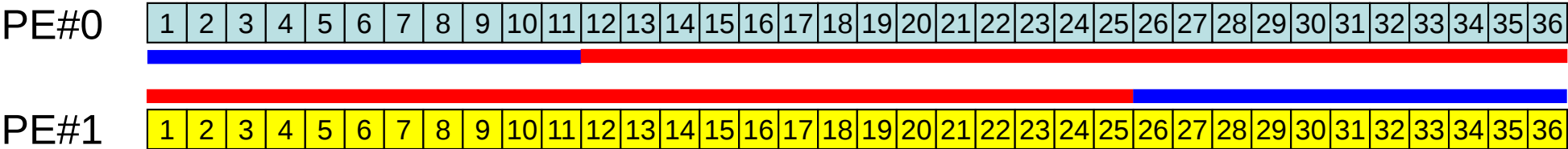
```
#!/bin/sh
#PJM -N "test"
#PJM -L rscgrp=lecture6-o
#PJM -L node=1
#PJM --mpi proc=2
#PJM -L elapse=00:15:00
#PJM -g gt36
#PJM -j
#PJM -e err
#PJM -o test.lst

module load fj
module load fjmpi

mpiexec ./a.out
```

# Ex.2: Send-Recv an Array (1/3)

- Exchange VEC (real, 8-byte) between PE#0 & PE#1
- PE#0 to PE#1
  - PE#0: send VEC(1)-VEC(11) (length=11)
  - PE#1: recv. as VEC(26)-VEC(36) (length=11)
- PE#1 to PE#0
  - PE#1: send VEC(1)-VEC(25) (length=25)
  - PE#0: recv. as VEC(12)-VEC(36) (length=25)
- Practice: Develop a program for this operation.



# Practice: t1

- Initial status of VEC(:):
  - PE#0 VEC(1-36)= 101,102,103,~,135,136
  - PE#1 VEC(1-36)= 201,202,203,~,235,236
- Confirm the results in the next page
- MPI\_Isend/Irecv/Waitall

# Estimated Results

t1

|   |          |    |      |
|---|----------|----|------|
| 0 | #BEFORE# | 1  | 101. |
| 0 | #BEFORE# | 2  | 102. |
| 0 | #BEFORE# | 3  | 103. |
| 0 | #BEFORE# | 4  | 104. |
| 0 | #BEFORE# | 5  | 105. |
| 0 | #BEFORE# | 6  | 106. |
| 0 | #BEFORE# | 7  | 107. |
| 0 | #BEFORE# | 8  | 108. |
| 0 | #BEFORE# | 9  | 109. |
| 0 | #BEFORE# | 10 | 110. |
| 0 | #BEFORE# | 11 | 111. |
| 0 | #BEFORE# | 12 | 112. |
| 0 | #BEFORE# | 13 | 113. |
| 0 | #BEFORE# | 14 | 114. |
| 0 | #BEFORE# | 15 | 115. |
| 0 | #BEFORE# | 16 | 116. |
| 0 | #BEFORE# | 17 | 117. |
| 0 | #BEFORE# | 18 | 118. |
| 0 | #BEFORE# | 19 | 119. |
| 0 | #BEFORE# | 20 | 120. |
| 0 | #BEFORE# | 21 | 121. |
| 0 | #BEFORE# | 22 | 122. |
| 0 | #BEFORE# | 23 | 123. |
| 0 | #BEFORE# | 24 | 124. |
| 0 | #BEFORE# | 25 | 125. |
| 0 | #BEFORE# | 26 | 126. |
| 0 | #BEFORE# | 27 | 127. |
| 0 | #BEFORE# | 28 | 128. |
| 0 | #BEFORE# | 29 | 129. |
| 0 | #BEFORE# | 30 | 130. |
| 0 | #BEFORE# | 31 | 131. |
| 0 | #BEFORE# | 32 | 132. |
| 0 | #BEFORE# | 33 | 133. |
| 0 | #BEFORE# | 34 | 134. |
| 0 | #BEFORE# | 35 | 135. |
| 0 | #BEFORE# | 36 | 136. |

|   |          |    |      |
|---|----------|----|------|
| 0 | #AFTER # | 1  | 101. |
| 0 | #AFTER # | 2  | 102. |
| 0 | #AFTER # | 3  | 103. |
| 0 | #AFTER # | 4  | 104. |
| 0 | #AFTER # | 5  | 105. |
| 0 | #AFTER # | 6  | 106. |
| 0 | #AFTER # | 7  | 107. |
| 0 | #AFTER # | 8  | 108. |
| 0 | #AFTER # | 9  | 109. |
| 0 | #AFTER # | 10 | 110. |
| 0 | #AFTER # | 11 | 111. |
| 0 | #AFTER # | 12 | 201. |
| 0 | #AFTER # | 13 | 202. |
| 0 | #AFTER # | 14 | 203. |
| 0 | #AFTER # | 15 | 204. |
| 0 | #AFTER # | 16 | 205. |
| 0 | #AFTER # | 17 | 206. |
| 0 | #AFTER # | 18 | 207. |
| 0 | #AFTER # | 19 | 208. |
| 0 | #AFTER # | 20 | 209. |
| 0 | #AFTER # | 21 | 210. |
| 0 | #AFTER # | 22 | 211. |
| 0 | #AFTER # | 23 | 212. |
| 0 | #AFTER # | 24 | 213. |
| 0 | #AFTER # | 25 | 214. |
| 0 | #AFTER # | 26 | 215. |
| 0 | #AFTER # | 27 | 216. |
| 0 | #AFTER # | 28 | 217. |
| 0 | #AFTER # | 29 | 218. |
| 0 | #AFTER # | 30 | 219. |
| 0 | #AFTER # | 31 | 220. |
| 0 | #AFTER # | 32 | 221. |
| 0 | #AFTER # | 33 | 222. |
| 0 | #AFTER # | 34 | 223. |
| 0 | #AFTER # | 35 | 224. |
| 0 | #AFTER # | 36 | 225. |

|   |          |    |      |
|---|----------|----|------|
| 1 | #BEFORE# | 1  | 201. |
| 1 | #BEFORE# | 2  | 202. |
| 1 | #BEFORE# | 3  | 203. |
| 1 | #BEFORE# | 4  | 204. |
| 1 | #BEFORE# | 5  | 205. |
| 1 | #BEFORE# | 6  | 206. |
| 1 | #BEFORE# | 7  | 207. |
| 1 | #BEFORE# | 8  | 208. |
| 1 | #BEFORE# | 9  | 209. |
| 1 | #BEFORE# | 10 | 210. |
| 1 | #BEFORE# | 11 | 211. |
| 1 | #BEFORE# | 12 | 212. |
| 1 | #BEFORE# | 13 | 213. |
| 1 | #BEFORE# | 14 | 214. |
| 1 | #BEFORE# | 15 | 215. |
| 1 | #BEFORE# | 16 | 216. |
| 1 | #BEFORE# | 17 | 217. |
| 1 | #BEFORE# | 18 | 218. |
| 1 | #BEFORE# | 19 | 219. |
| 1 | #BEFORE# | 20 | 220. |
| 1 | #BEFORE# | 21 | 221. |
| 1 | #BEFORE# | 22 | 222. |
| 1 | #BEFORE# | 23 | 223. |
| 1 | #BEFORE# | 24 | 224. |
| 1 | #BEFORE# | 25 | 225. |
| 1 | #BEFORE# | 26 | 226. |
| 1 | #BEFORE# | 27 | 227. |
| 1 | #BEFORE# | 28 | 228. |
| 1 | #BEFORE# | 29 | 229. |
| 1 | #BEFORE# | 30 | 230. |
| 1 | #BEFORE# | 31 | 231. |
| 1 | #BEFORE# | 32 | 232. |
| 1 | #BEFORE# | 33 | 233. |
| 1 | #BEFORE# | 34 | 234. |
| 1 | #BEFORE# | 35 | 235. |
| 1 | #BEFORE# | 36 | 236. |

|   |          |    |      |
|---|----------|----|------|
| 1 | #AFTER # | 1  | 201. |
| 1 | #AFTER # | 2  | 202. |
| 1 | #AFTER # | 3  | 203. |
| 1 | #AFTER # | 4  | 204. |
| 1 | #AFTER # | 5  | 205. |
| 1 | #AFTER # | 6  | 206. |
| 1 | #AFTER # | 7  | 207. |
| 1 | #AFTER # | 8  | 208. |
| 1 | #AFTER # | 9  | 209. |
| 1 | #AFTER # | 10 | 210. |
| 1 | #AFTER # | 11 | 211. |
| 1 | #AFTER # | 12 | 212. |
| 1 | #AFTER # | 13 | 213. |
| 1 | #AFTER # | 14 | 214. |
| 1 | #AFTER # | 15 | 215. |
| 1 | #AFTER # | 16 | 216. |
| 1 | #AFTER # | 17 | 217. |
| 1 | #AFTER # | 18 | 218. |
| 1 | #AFTER # | 19 | 219. |
| 1 | #AFTER # | 20 | 220. |
| 1 | #AFTER # | 21 | 221. |
| 1 | #AFTER # | 22 | 222. |
| 1 | #AFTER # | 23 | 223. |
| 1 | #AFTER # | 24 | 224. |
| 1 | #AFTER # | 25 | 225. |
| 1 | #AFTER # | 26 | 101. |
| 1 | #AFTER # | 27 | 102. |
| 1 | #AFTER # | 28 | 103. |
| 1 | #AFTER # | 29 | 104. |
| 1 | #AFTER # | 30 | 105. |
| 1 | #AFTER # | 31 | 106. |
| 1 | #AFTER # | 32 | 107. |
| 1 | #AFTER # | 33 | 108. |
| 1 | #AFTER # | 34 | 109. |
| 1 | #AFTER # | 35 | 110. |
| 1 | #AFTER # | 36 | 111. |

## Ex.2: Send-Recv an Array (2/3)

```
if (my_rank.eq.0) then
  call MPI_Isend (VEC( 1), 11, MPI_DOUBLE_PRECISION, 1, ..., req_send(1), ...)
  call MPI_Irecv (VEC(12), 25, MPI_DOUBLE_PRECISION, 1, ..., req_recv(1), ...)
endif

if (my_rank.eq.1) then
  call MPI_Isend (VEC( 1), 25, MPI_DOUBLE_PRECISION, 0, ..., req_send(1), ...)
  call MPI_Irecv (VEC(26), 11, MPI_DOUBLE_PRECISION, 0, ..., req_recv(1), ...)
endif

call MPI_Waitall (... , req_recv, stat_recv, ...)
call MPI_Waitall (... , req_send, stat_send, ...)
```

It works, but complicated operations.

Not looks like SPMD.

Not portable.

## Ex.2: Send-Recv an Array (3/3)

```
if (my_rank.eq.0) then
  NEIB= 1
  start_send= 1
  length_send= 11
  start_recv= length_send + 1
  length_recv= 25
endif

if (my_rank.eq.1) then
  NEIB= 0
  start_send= 1
  length_send= 25
  start_recv= length_send + 1
  length_recv= 11
endif

call MPI_Isend
(VEC(start_send), length_send, MPI_DOUBLE_PRECISION, NEIB, ..., req_send(1), ...) &
call MPI_Irecv
(VEC(start_recv), length_recv, MPI_DOUBLE_PRECISION, NEIB, ..., req_recv(1), ...) &

call MPI_Waitall (... , req_recv, stat_recv, ...)
call MPI_Waitall (... , req_send, stat_send, ...)
```

This is “SMPD” !!

t1

# Notice: Send/Recv Arrays

**#PE0**

send:

```
VEC(start_send)~  
VEC(start_send+length_send-1)
```

**#PE1**

send:

```
VEC(start_send)~  
VEC(start_send+length_send-1)
```

**#PE0**

recv:

```
VEC(start_recv)~  
VEC(start_recv+length_recv-1)
```

**#PE1**

recv:

```
VEC(start_recv)~  
VEC(start_recv+length_recv-1)
```

- “length\_send” of sending process must be equal to “length\_recv” of receiving process.
  - PE#0 to PE#1, PE#1 to PE#0
- “sendbuf” and “recvbuf”: different address

# Point-to-Point Communication

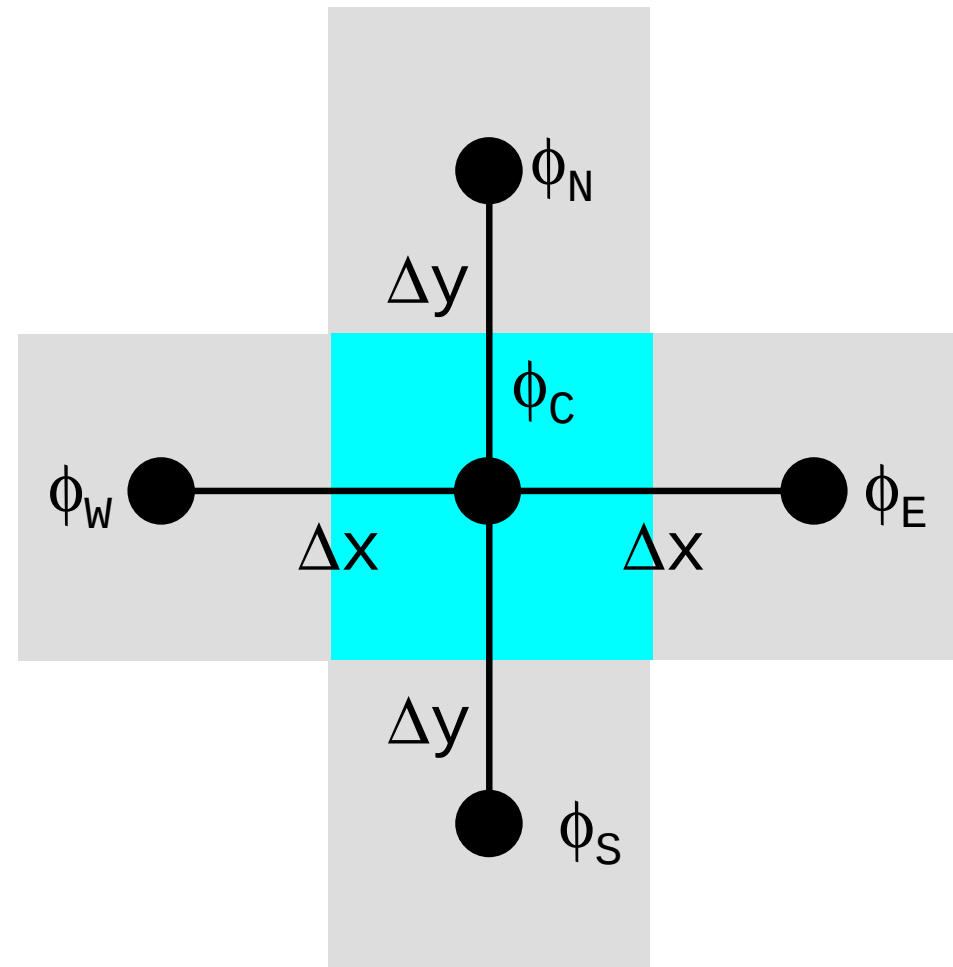
- What is PtoP Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

[illegible]

# 2D FDM (5-point, central difference)

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = f$$

$$\left( \frac{\phi_E - 2\phi_C + \phi_W}{\Delta x^2} \right) + \left( \frac{\phi_N - 2\phi_C + \phi_S}{\Delta y^2} \right) = f_C$$



# Decompose into 4 domains

|           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

# 4 domains: Global ID

PE#2

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |

PE#3

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |

PE#0

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |

PE#1

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

# 4 domains: Local ID

PE#2

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

PE#3

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

PE#0

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

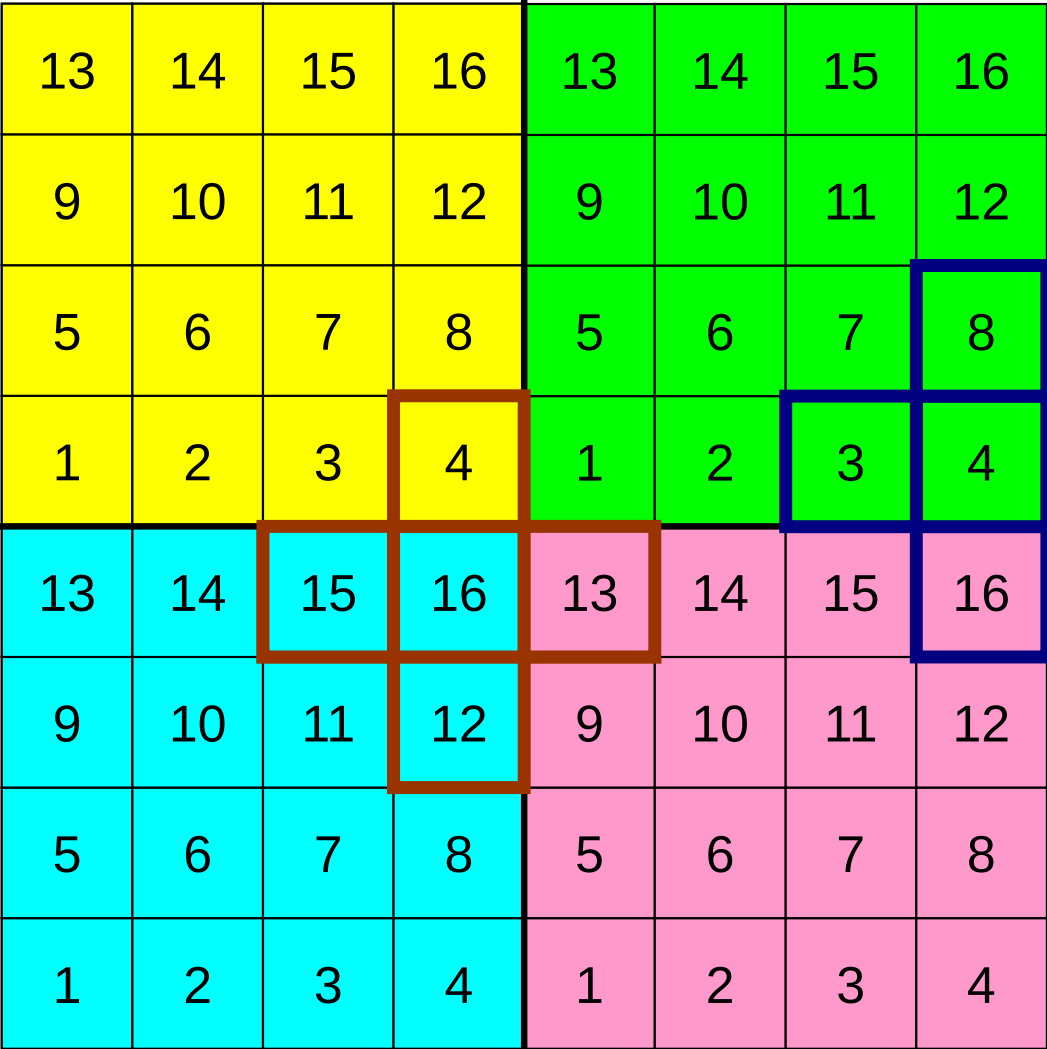
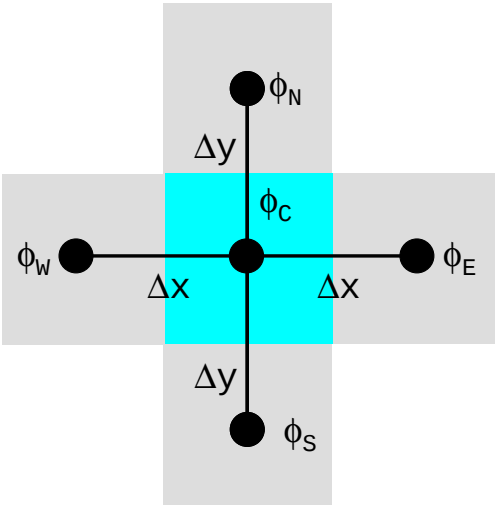
PE#1

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

# External Points: Overlapped Region

PE#2

PE#3



PE#0

PE#1

# External Points: Overlapped Region

PE#2

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

PE#3

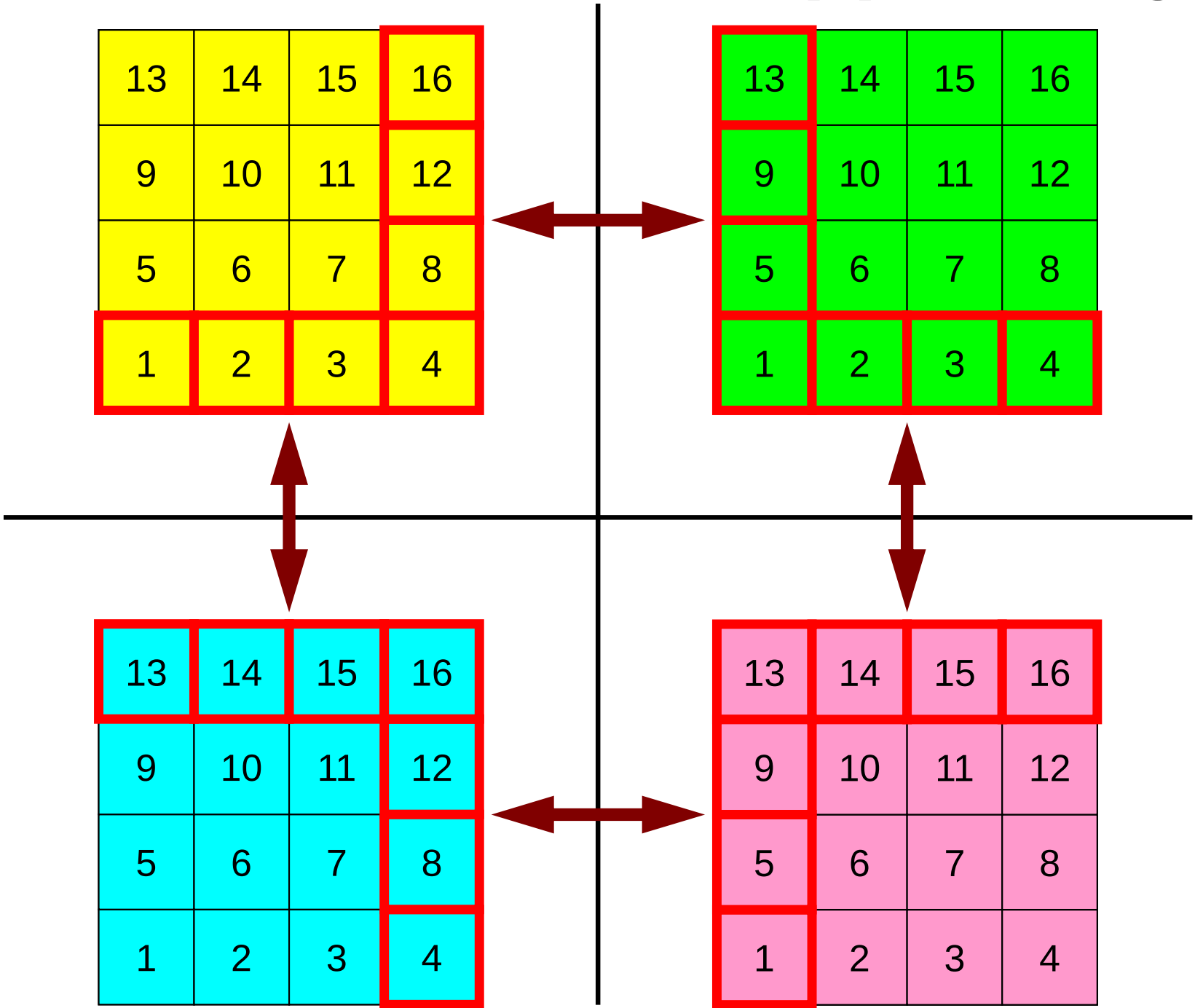
|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

PE#0

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

PE#1

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |



# Local ID of External Points ?

PE#2

|    |    |    |    |   |
|----|----|----|----|---|
| 13 | 14 | 15 | 16 | ? |
| 9  | 10 | 11 | 12 | ? |
| 5  | 6  | 7  | 8  | ? |
| 1  | 2  | 3  | 4  | ? |
| ?  | ?  | ?  | ?  |   |

PE#3

|   |    |    |    |    |
|---|----|----|----|----|
| ? | 13 | 14 | 15 | 16 |
| ? | 9  | 10 | 11 | 12 |
| ? | 5  | 6  | 7  | 8  |
| ? | 1  | 2  | 3  | 4  |
|   | ?  | ?  | ?  | ?  |

PE#0

|    |    |    |    |   |
|----|----|----|----|---|
| ?  | ?  | ?  | ?  |   |
| 13 | 14 | 15 | 16 | ? |
| 9  | 10 | 11 | 12 | ? |
| 5  | 6  | 7  | 8  | ? |
| 1  | 2  | 3  | 4  | ? |

PE#1

|   |    |    |    |    |
|---|----|----|----|----|
|   | ?  | ?  | ?  | ?  |
| ? | 13 | 14 | 15 | 16 |
| ? | 9  | 10 | 11 | 12 |
| ? | 5  | 6  | 7  | 8  |
| ? | 1  | 2  | 3  | 4  |

# Overlapped Region

PE#2

|    |    |    |    |   |
|----|----|----|----|---|
| 13 | 14 | 15 | 16 | ? |
| 9  | 10 | 11 | 12 | ? |
| 5  | 6  | 7  | 8  | ? |
| 1  | 2  | 3  | 4  | ? |

|   |   |   |   |
|---|---|---|---|
| ? | ? | ? | ? |
|---|---|---|---|

PE#3

|   |    |    |    |    |
|---|----|----|----|----|
| ? | 13 | 14 | 15 | 16 |
| ? | 9  | 10 | 11 | 12 |
| ? | 5  | 6  | 7  | 8  |
| ? | 1  | 2  | 3  | 4  |

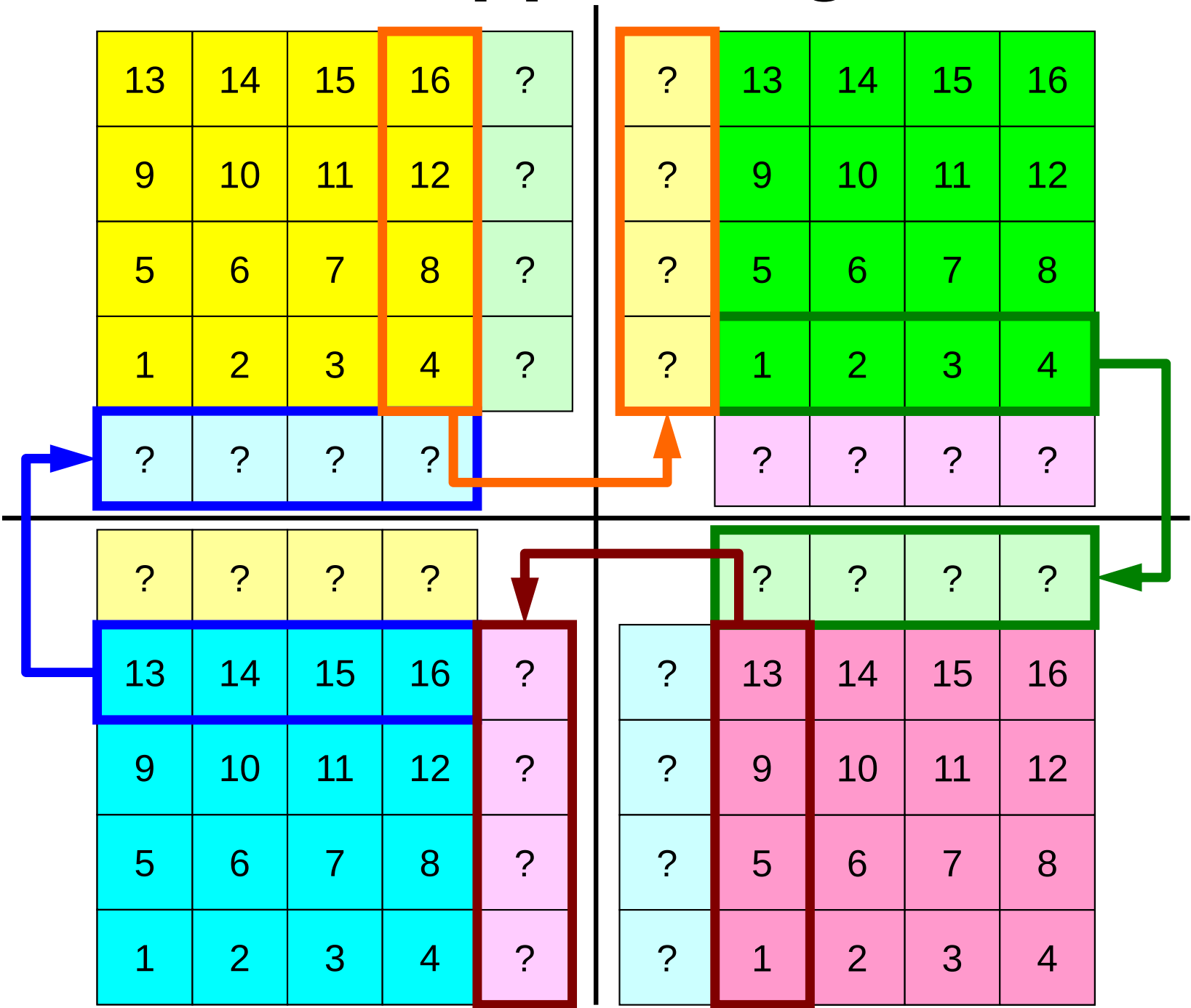
|   |   |   |   |
|---|---|---|---|
| ? | ? | ? | ? |
|---|---|---|---|

PE#0

|    |    |    |    |   |
|----|----|----|----|---|
| ?  | ?  | ?  | ?  |   |
| 13 | 14 | 15 | 16 | ? |
| 9  | 10 | 11 | 12 | ? |
| 5  | 6  | 7  | 8  | ? |
| 1  | 2  | 3  | 4  | ? |

PE#1

|   |    |    |    |    |   |
|---|----|----|----|----|---|
|   |    | ?  | ?  | ?  | ? |
| ? | 13 | 14 | 15 | 16 |   |
| ? | 9  | 10 | 11 | 12 |   |
| ? | 5  | 6  | 7  | 8  |   |
| ? | 1  | 2  | 3  | 4  |   |



# Overlapped Region

PE#2

|    |    |    |    |   |
|----|----|----|----|---|
| 13 | 14 | 15 | 16 | ? |
| 9  | 10 | 11 | 12 | ? |
| 5  | 6  | 7  | 8  | ? |
| 1  | 2  | 3  | 4  | ? |
| ?  | ?  | ?  | ?  |   |

PE#3

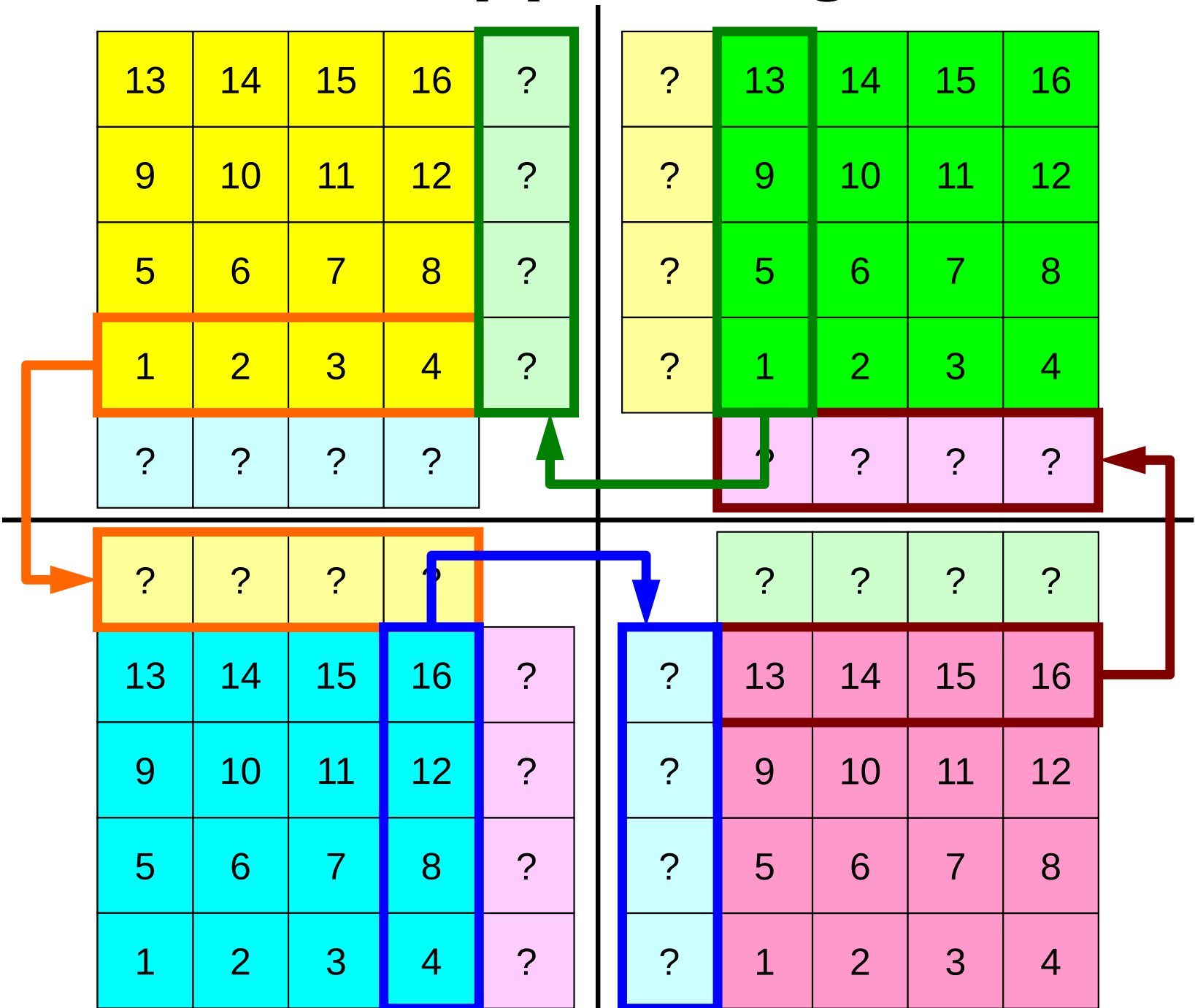
|   |    |    |    |    |
|---|----|----|----|----|
| ? | 13 | 14 | 15 | 16 |
| ? | 9  | 10 | 11 | 12 |
| ? | 5  | 6  | 7  | 8  |
| ? | 1  | 2  | 3  | 4  |
|   | ?  | ?  | ?  | ?  |

PE#0

|    |    |    |    |   |
|----|----|----|----|---|
| ?  | ?  | ?  | ?  |   |
| 13 | 14 | 15 | 16 | ? |
| 9  | 10 | 11 | 12 | ? |
| 5  | 6  | 7  | 8  | ? |
| 1  | 2  | 3  | 4  | ? |

PE#1

|   |    |    |    |    |
|---|----|----|----|----|
|   | ?  | ?  | ?  | ?  |
| ? | 13 | 14 | 15 | 16 |
| ? | 9  | 10 | 11 | 12 |
| ? | 5  | 6  | 7  | 8  |
| ? | 1  | 2  | 3  | 4  |



# Point-to-Point Communication

- What is PtoP Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

# Problem Setting: 2D FDM

|           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

- 2D region with 64 meshes (8x8)
- Each mesh has global ID from 1 to 64
  - In this example, this global ID is considered as dependent variable, such as temperature, pressure etc.
  - Something like computed results

# Problem Setting: Distributed Local Data

**PE#2**

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |

**PE#3**

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |

- 4 sub-domains.
- Info. of external points (global ID of mesh) is received from neighbors.
  - PE#0 receives

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

**PE#0**

**PE#1**

**PE#2**

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |  |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |  |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |  |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |  |
|           |           |           |           |  |

**PE#3**

|  |           |           |           |           |
|--|-----------|-----------|-----------|-----------|
|  | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
|  | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
|  | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
|  | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
|  |           |           |           |           |

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
|           |           |           |           |  |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |  |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |  |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |  |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |  |

|  |           |           |           |           |
|--|-----------|-----------|-----------|-----------|
|  |           |           |           |           |
|  | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
|  | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
|  | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
|  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

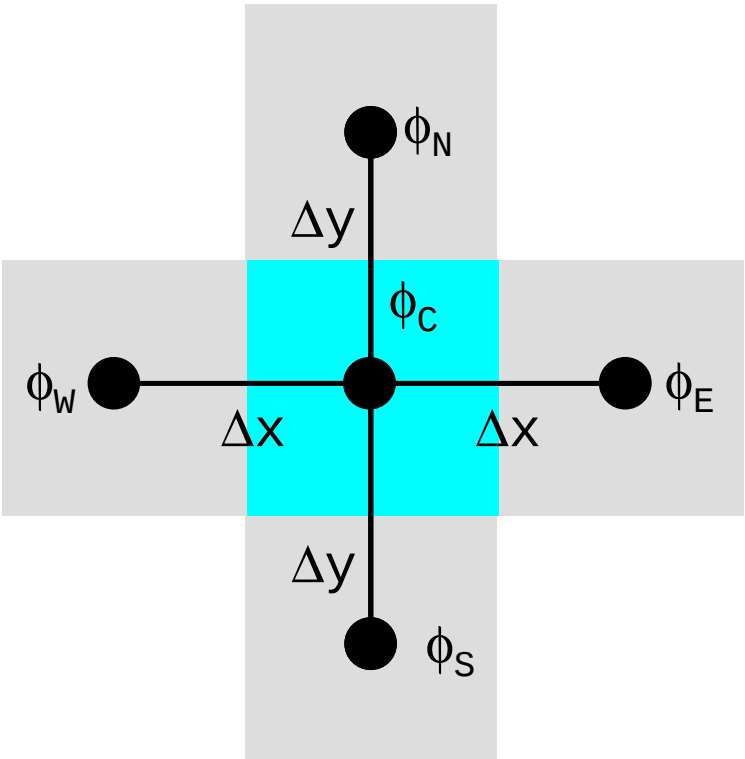
**PE#0**

**PE#1**

# Operations of 2D FDM

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = f$$

$$\left(\frac{\phi_E - 2\phi_C + \phi_W}{\Delta x^2}\right) + \left(\frac{\phi_N - 2\phi_C + \phi_S}{\Delta y^2}\right) = f_C$$

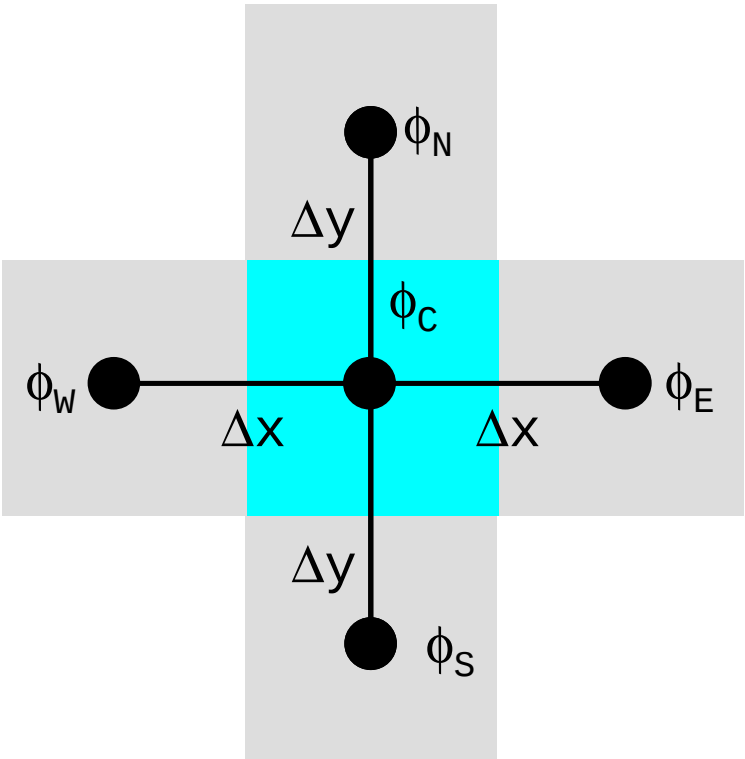


|           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

# Operations of 2D FDM

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = f$$

$$\left(\frac{\phi_E - 2\phi_C + \phi_W}{\Delta x^2}\right) + \left(\frac{\phi_N - 2\phi_C + \phi_S}{\Delta y^2}\right) = f_C$$



|           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

# Computation (1/3)

|             |           |           |           |           |           |           |           |           |             |
|-------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-------------|
| <u>PE#2</u> | <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> | <u>PE#3</u> |
|             | <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |             |
|             | <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |             |
|             | <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |             |
|             | <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |             |
|             | <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |             |
|             | <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |             |
| <u>PE#0</u> | <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  | <u>PE#1</u> |

- On each PE, info. of internal pts ( $i=1-N(=16)$ ) are read from distributed local data, info. of boundary pts are sent to neighbors, and they are received as info. of external pts.

# Computation (2/3): Before Send/Recv

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>33</u> | 9: <u>49</u>  | 17: <u>?</u> |
| 2: <u>34</u> | 10: <u>50</u> | 18: <u>?</u> |
| 3: <u>35</u> | 11: <u>51</u> | 19: <u>?</u> |
| 4: <u>36</u> | 12: <u>52</u> | 20: <u>?</u> |
| 5: <u>41</u> | 13: <u>57</u> | 21: <u>?</u> |
| 6: <u>42</u> | 14: <u>58</u> | 22: <u>?</u> |
| 7: <u>43</u> | 15: <u>59</u> | 23: <u>?</u> |
| 8: <u>44</u> | 16: <u>60</u> | 24: <u>?</u> |

PE#2

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |  |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |  |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |  |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |  |
|           |           |           |           |  |

PE#3

|  |           |           |           |           |
|--|-----------|-----------|-----------|-----------|
|  | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
|  | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
|  | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
|  | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
|  |           |           |           |           |

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>37</u> | 9: <u>53</u>  | 17: <u>?</u> |
| 2: <u>38</u> | 10: <u>54</u> | 18: <u>?</u> |
| 3: <u>39</u> | 11: <u>55</u> | 19: <u>?</u> |
| 4: <u>40</u> | 12: <u>56</u> | 20: <u>?</u> |
| 5: <u>45</u> | 13: <u>61</u> | 21: <u>?</u> |
| 6: <u>46</u> | 14: <u>62</u> | 22: <u>?</u> |
| 7: <u>47</u> | 15: <u>63</u> | 23: <u>?</u> |
| 8: <u>48</u> | 16: <u>64</u> | 24: <u>?</u> |

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>1</u>  | 9: <u>17</u>  | 17: <u>?</u> |
| 2: <u>2</u>  | 10: <u>18</u> | 18: <u>?</u> |
| 3: <u>3</u>  | 11: <u>19</u> | 19: <u>?</u> |
| 4: <u>4</u>  | 12: <u>20</u> | 20: <u>?</u> |
| 5: <u>9</u>  | 13: <u>25</u> | 21: <u>?</u> |
| 6: <u>10</u> | 14: <u>26</u> | 22: <u>?</u> |
| 7: <u>11</u> | 15: <u>27</u> | 23: <u>?</u> |
| 8: <u>12</u> | 16: <u>28</u> | 24: <u>?</u> |

PE#0

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
|           |           |           |           |  |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |  |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |  |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |  |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |  |

PE#1

|  |           |           |           |           |
|--|-----------|-----------|-----------|-----------|
|  |           |           |           |           |
|  | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
|  | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
|  | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
|  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>5</u>  | 9: <u>21</u>  | 17: <u>?</u> |
| 2: <u>6</u>  | 10: <u>22</u> | 18: <u>?</u> |
| 3: <u>7</u>  | 11: <u>23</u> | 19: <u>?</u> |
| 4: <u>8</u>  | 12: <u>24</u> | 20: <u>?</u> |
| 5: <u>13</u> | 13: <u>29</u> | 21: <u>?</u> |
| 6: <u>14</u> | 14: <u>30</u> | 22: <u>?</u> |
| 7: <u>15</u> | 15: <u>31</u> | 23: <u>?</u> |
| 8: <u>16</u> | 16: <u>32</u> | 24: <u>?</u> |

# Computation (2/3): Before Send/Recv

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>33</u> | 9: <u>49</u>  | 17: <u>?</u> |
| 2: <u>34</u> | 10: <u>50</u> | 18: <u>?</u> |
| 3: <u>35</u> | 11: <u>51</u> | 19: <u>?</u> |
| 4: <u>36</u> | 12: <u>52</u> | 20: <u>?</u> |
| 5: <u>41</u> | 13: <u>57</u> | 21: <u>?</u> |
| 6: <u>42</u> | 14: <u>58</u> | 22: <u>?</u> |
| 7: <u>43</u> | 15: <u>59</u> | 23: <u>?</u> |
| 8: <u>44</u> | 16: <u>60</u> | 24: <u>?</u> |

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>1</u>  | 9: <u>17</u>  | 17: <u>?</u> |
| 2: <u>2</u>  | 10: <u>18</u> | 18: <u>?</u> |
| 3: <u>3</u>  | 11: <u>19</u> | 19: <u>?</u> |
| 4: <u>4</u>  | 12: <u>20</u> | 20: <u>?</u> |
| 5: <u>9</u>  | 13: <u>25</u> | 21: <u>?</u> |
| 6: <u>10</u> | 14: <u>26</u> | 22: <u>?</u> |
| 7: <u>11</u> | 15: <u>27</u> | 23: <u>?</u> |
| 8: <u>12</u> | 16: <u>28</u> | 24: <u>?</u> |

PE#2

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |  |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |  |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |  |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |  |
|           |           |           |           |  |

PE#0

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
|           |           |           |           |  |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |  |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |  |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |  |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |  |

PE#3

|  |           |           |           |           |
|--|-----------|-----------|-----------|-----------|
|  | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
|  | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
|  | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
|  | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
|  |           |           |           |           |

PE#1

|  |           |           |           |           |
|--|-----------|-----------|-----------|-----------|
|  |           |           |           |           |
|  | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
|  | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
|  | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
|  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>37</u> | 9: <u>53</u>  | 17: <u>?</u> |
| 2: <u>38</u> | 10: <u>54</u> | 18: <u>?</u> |
| 3: <u>39</u> | 11: <u>55</u> | 19: <u>?</u> |
| 4: <u>40</u> | 12: <u>56</u> | 20: <u>?</u> |
| 5: <u>45</u> | 13: <u>61</u> | 21: <u>?</u> |
| 6: <u>46</u> | 14: <u>62</u> | 22: <u>?</u> |
| 7: <u>47</u> | 15: <u>63</u> | 23: <u>?</u> |
| 8: <u>48</u> | 16: <u>64</u> | 24: <u>?</u> |

|              |               |              |
|--------------|---------------|--------------|
| 1: <u>5</u>  | 9: <u>21</u>  | 17: <u>?</u> |
| 2: <u>6</u>  | 10: <u>22</u> | 18: <u>?</u> |
| 3: <u>7</u>  | 11: <u>23</u> | 19: <u>?</u> |
| 4: <u>8</u>  | 12: <u>24</u> | 20: <u>?</u> |
| 5: <u>13</u> | 13: <u>29</u> | 21: <u>?</u> |
| 6: <u>14</u> | 14: <u>30</u> | 22: <u>?</u> |
| 7: <u>15</u> | 15: <u>31</u> | 23: <u>?</u> |
| 8: <u>16</u> | 16: <u>32</u> | 24: <u>?</u> |

# Computation (3/3): After Send/Recv

|              |               |               |
|--------------|---------------|---------------|
| 1: <u>33</u> | 9: <u>49</u>  | 17: <u>37</u> |
| 2: <u>34</u> | 10: <u>50</u> | 18: <u>45</u> |
| 3: <u>35</u> | 11: <u>51</u> | 19: <u>53</u> |
| 4: <u>36</u> | 12: <u>52</u> | 20: <u>61</u> |
| 5: <u>41</u> | 13: <u>57</u> | 21: <u>25</u> |
| 6: <u>42</u> | 14: <u>58</u> | 22: <u>26</u> |
| 7: <u>43</u> | 15: <u>59</u> | 23: <u>27</u> |
| 8: <u>44</u> | 16: <u>60</u> | 24: <u>28</u> |

PE#2

|           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> | <u>61</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> | <u>53</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> | <u>45</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> | <u>37</u> |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |           |

PE#3

|           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|
| <u>60</u> | <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>52</u> | <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>44</u> | <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>36</u> | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
|           | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |

|              |               |               |
|--------------|---------------|---------------|
| 1: <u>37</u> | 9: <u>53</u>  | 17: <u>36</u> |
| 2: <u>38</u> | 10: <u>54</u> | 18: <u>44</u> |
| 3: <u>39</u> | 11: <u>55</u> | 19: <u>52</u> |
| 4: <u>40</u> | 12: <u>56</u> | 20: <u>60</u> |
| 5: <u>45</u> | 13: <u>61</u> | 21: <u>29</u> |
| 6: <u>46</u> | 14: <u>62</u> | 22: <u>30</u> |
| 7: <u>47</u> | 15: <u>63</u> | 23: <u>31</u> |
| 8: <u>48</u> | 16: <u>64</u> | 24: <u>32</u> |

|              |               |               |
|--------------|---------------|---------------|
| 1: <u>1</u>  | 9: <u>17</u>  | 17: <u>5</u>  |
| 2: <u>2</u>  | 10: <u>18</u> | 18: <u>14</u> |
| 3: <u>3</u>  | 11: <u>19</u> | 19: <u>21</u> |
| 4: <u>4</u>  | 12: <u>20</u> | 20: <u>29</u> |
| 5: <u>9</u>  | 13: <u>25</u> | 21: <u>33</u> |
| 6: <u>10</u> | 14: <u>26</u> | 22: <u>34</u> |
| 7: <u>11</u> | 15: <u>27</u> | 23: <u>35</u> |
| 8: <u>12</u> | 16: <u>28</u> | 24: <u>36</u> |

PE#0

|           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |           |
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> | <u>29</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> | <u>21</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> | <u>13</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  |

PE#1

|           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|
|           | <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |
| <u>28</u> | <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>20</u> | <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>4</u>  | <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

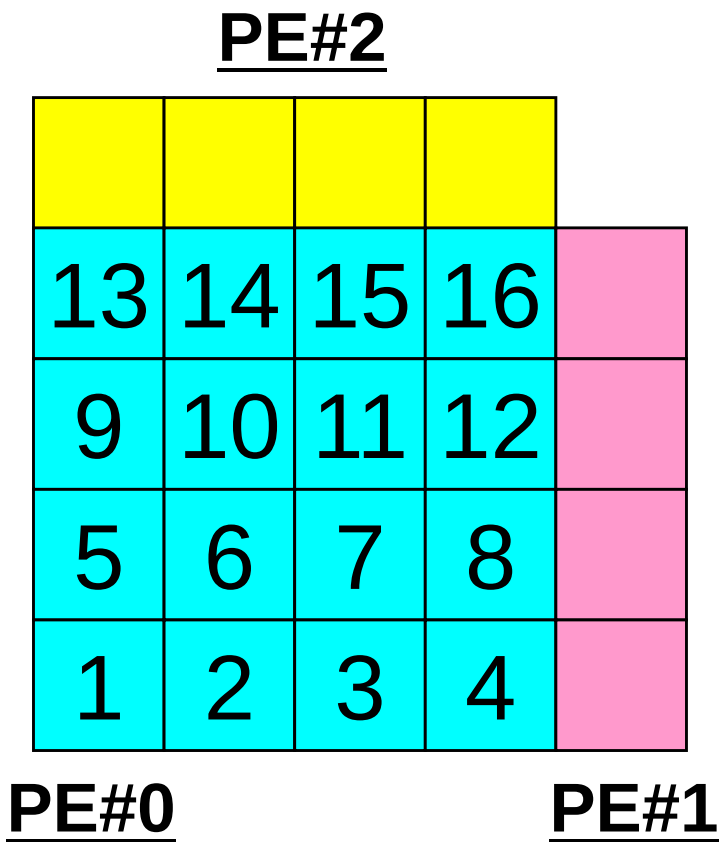
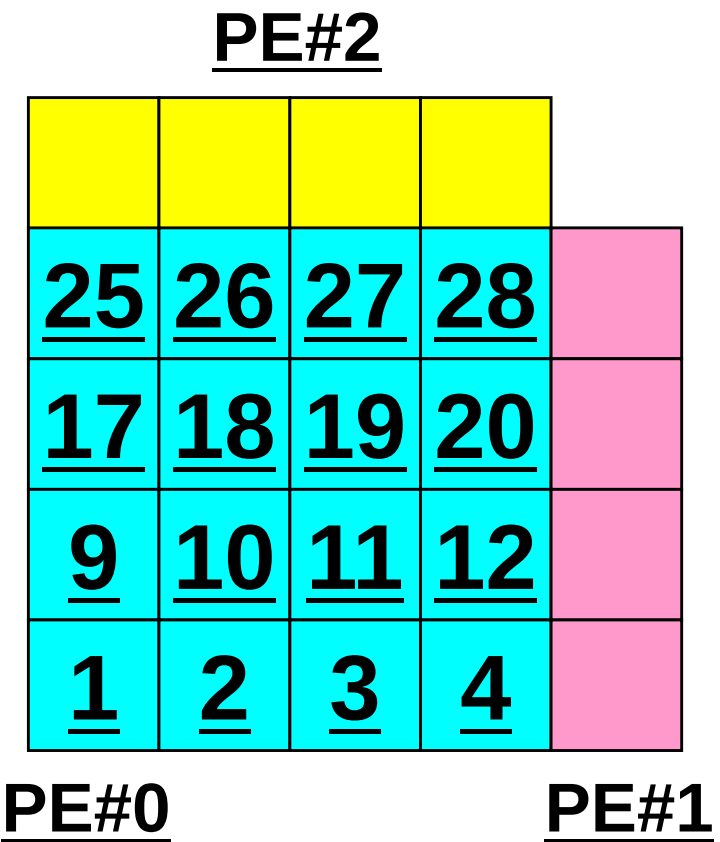
|              |               |               |
|--------------|---------------|---------------|
| 1: <u>5</u>  | 9: <u>21</u>  | 17: <u>4</u>  |
| 2: <u>6</u>  | 10: <u>22</u> | 18: <u>12</u> |
| 3: <u>7</u>  | 11: <u>23</u> | 19: <u>20</u> |
| 4: <u>8</u>  | 12: <u>24</u> | 20: <u>28</u> |
| 5: <u>13</u> | 13: <u>29</u> | 21: <u>37</u> |
| 6: <u>14</u> | 14: <u>30</u> | 22: <u>38</u> |
| 7: <u>15</u> | 15: <u>31</u> | 23: <u>39</u> |
| 8: <u>16</u> | 16: <u>32</u> | 24: <u>40</u> |

# Peer-to-Peer Communication

- What is P2P Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

# Overview of Distributed Local Data

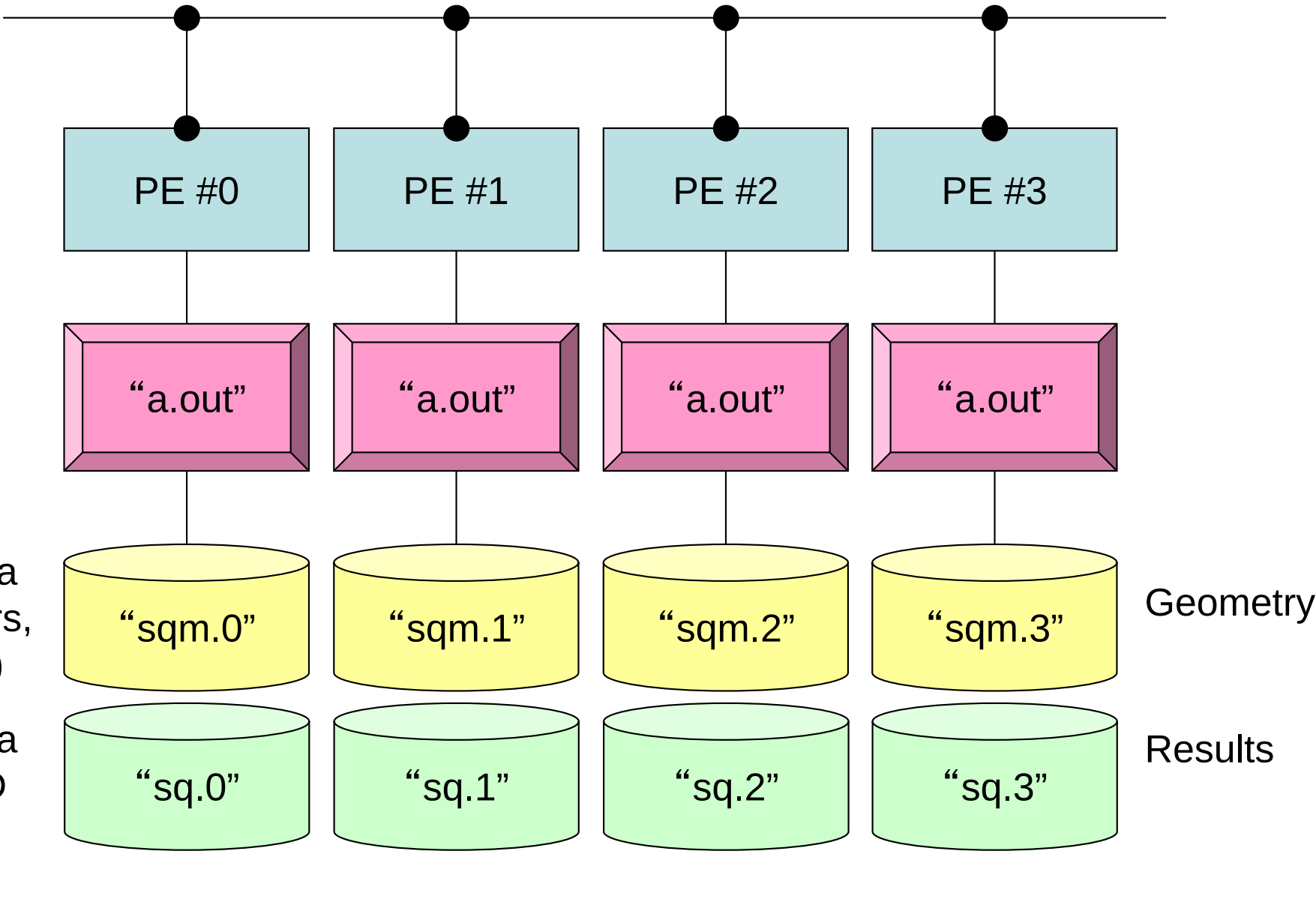
## Example on PE#0



Value at each mesh (= Global ID)

Local ID

# SPMD...



# 2D FDM: PE#0

## Information at each domain (1/4)

Internal Points  
Meshes originally assigned to the domain

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 9  | 10 | 11 | 12 |
| 5  | 6  | 7  | 8  |
| 1  | 2  | 3  | 4  |

# 2D FDM: PE#0

## Information at each domain (2/4)

PE#2

|                                                                                   |                                                                                   |                                                                                   |                                                                                   |                                                                                     |
|-----------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|
|  |  |  |  |                                                                                     |
| 13                                                                                | 14                                                                                | 15                                                                                | 16                                                                                |    |
| 9                                                                                 | 10                                                                                | 11                                                                                | 12                                                                                |   |
| 5                                                                                 | 6                                                                                 | 7                                                                                 | 8                                                                                 |  |
| 1                                                                                 | 2                                                                                 | 3                                                                                 | 4                                                                                 |  |

PE#1

Internal Points

Meshes originally assigned to the domain

External Points

Meshes originally assigned to different domain, but required for computation of meshes in the domain (meshes in overlapped regions)

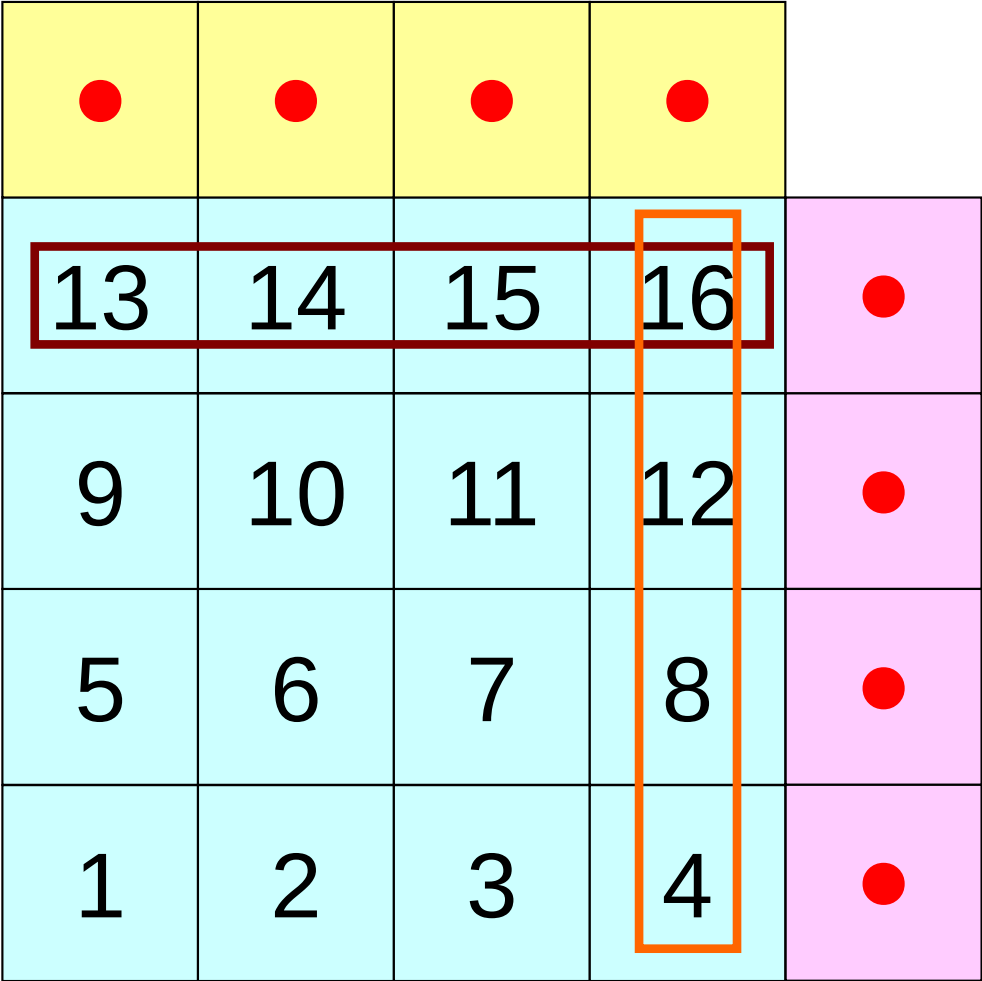
- Sleeves
- Halo



# 2D FDM: PE#0

Information at each domain (3/4)

PE#2



PE#1

Internal Points

Meshes originally assigned to the domain

External Points

Meshes originally assigned to different domain, but required for computation of meshes in the domain (meshes in overlapped regions)

Boundary Points

Internal points, which are also external points of other domains (used in computations of meshes in other domains)

# 2D FDM: PE#0

## Information at each domain (4/4)

PE#2

|    |    |    |    |  |
|----|----|----|----|--|
|    |    |    |    |  |
|    |    |    |    |  |
| 13 | 14 | 15 | 16 |  |
| 9  | 10 | 11 | 12 |  |
| 5  | 6  | 7  | 8  |  |
| 1  | 2  | 3  | 4  |  |

PE#1

Internal Points

Meshes originally assigned to the domain

External Points

Meshes originally assigned to different domain, but required for computation of meshes in the domain (meshes in overlapped regions)

Boundary Points

Internal points, which are also external points of other domains (used in computations of meshes in other domains)

Relationships between Domains

Communication Table: External/Boundary Points  
Neighbors

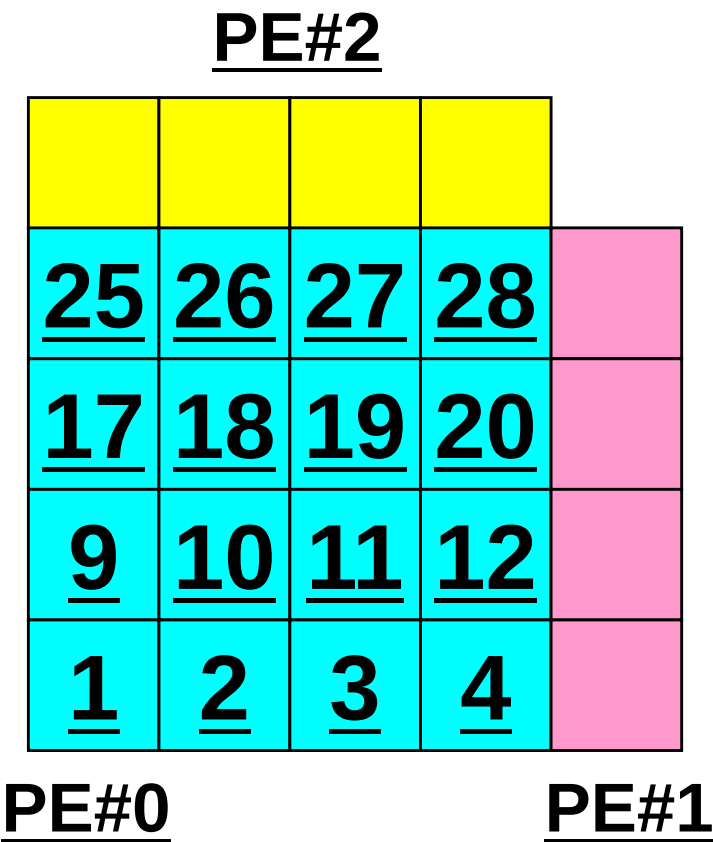
# Description of Distributed Local Data

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

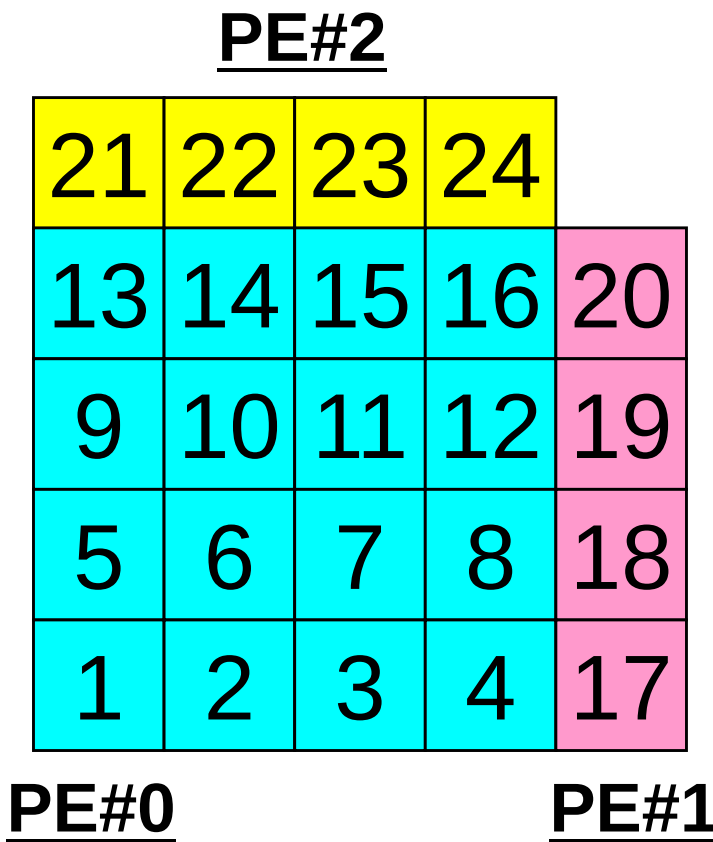
- Internal/External Points
  - Numbering: Starting from internal pts, then external pts after that
- Neighbors
  - Shares overlapped meshes
  - Number and ID of neighbors
- Import Table (Receive)
  - From where, how many, and which external points are received/imported ?
- Export Table (Send)
  - To where, how many and which boundary points are sent/exported ?

# Overview of Distributed Local Data

Example on PE#0



Value at each mesh (= Global ID)



Local ID

# Generalized Comm. Table: Send

|   |           |             |             |              |              |
|---|-----------|-------------|-------------|--------------|--------------|
| ① | 1.1<br>①  | 2.4<br>②,1  | 3.2<br>⑤,2  |              |              |
| ② | 3.6<br>②  | 4.3<br>①,3  | 2.5<br>④,4  | 3.7<br>⑥,5   | 9.1<br>⑧,6   |
| ③ | 5.7<br>③  | 1.5<br>⑤,7  | 3.1<br>⑦,8  |              |              |
| ④ | 9.8<br>④  | 4.1<br>②,9  | 2.5<br>⑤,10 | 2.7<br>⑥,11  |              |
| ⑤ | 11.5<br>⑤ | 3.1<br>①,12 | 9.5<br>②,13 | 10.4<br>③,14 | 4.3<br>⑦,15  |
| ⑥ | 12.4<br>⑥ | 6.5<br>③,16 | 9.5<br>⑦,17 |              |              |
| ⑦ | 23.1<br>⑦ | 6.4<br>②,18 | 2.5<br>③,19 | 1.4<br>⑥,20  | 13.1<br>⑧,21 |
| ⑧ | 51.3<br>⑧ | 9.5<br>②,22 | 1.3<br>③,23 | 9.6<br>④,24  | 3.1<br>⑥,25  |

**Diag (i)** Diagonal Components (REAL, i=1~N)  
**Index(i)** Number of Non-Zero Off-Diagonals at Each ROW (INT, i=0~N)  
**Item(k)** Off-Diagonal Components (Corresponding Column ID) (INT, k=1, index(N))  
**AMat(k)** Off-Diagonal Components (Value) (REAL, k=1, index(N))

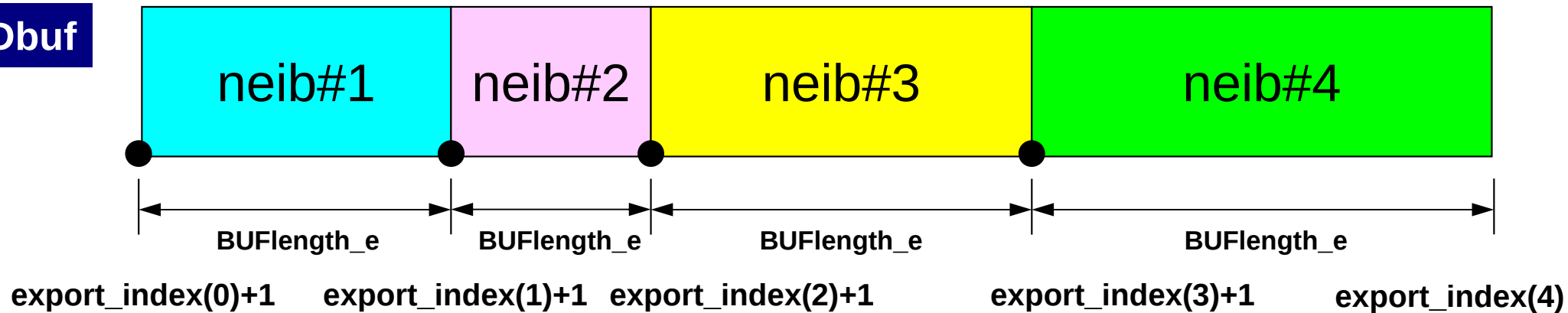
$\{Y\} = [A] \{X\}$

```
do i= 1, N
  Y(i)= D(i)*X(i)
  do k= index(i-1)+1, index(i)
    Y(i)= Y(i) + AMAT(k)*X(item(k))
  enddo
enddo
```

- Neighbors
  - NEIBPETOT, NEIBPE(NEIBPETOT)
- Message size for each neighbor
  - export\_index(neib), neib= 0, NEIBPETOT
- ID of boundary points
  - export\_item(k), k= 1, export\_index(NEIBPETOT)
- Messages to each neighbor
  - SENDbuf(k), k= 1, export\_index(NEIBPETOT)

# SEND: MPI\_Isend/Irecv/Waitall Fortran

**SENDbuf**



```

do neib= 1, NEIBPETOT
  do k= export_index(neib-1)+1, export_index(neib)
    kk= export_item(k)
    SENDbuf(k)= VAL(kk)
  enddo
enddo

```

Copied to sending buffers

```

do neib= 1, NEIBPETOT
  iS_e= export_index(neib-1) + 1
  iE_e= export_index(neib)
  BUFlength_e= iE_e + 1 - iS_e

  call MPI_ISEND
&      (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&      MPI_COMM_WORLD, request_send(neib), ierr)
enddo

call MPI_WAITALL (NEIBPETOT, request_send, stat_send, ierr)

```

# Generalized Comm. Table: Receive

- Neighbors
  - NEIBPETOT, NEIBPE(NEIBPETOT)
- Message size for each neighbor
  - import\_index(neib), neib= 0, NEIBPETOT
- ID of **external** points
  - import\_item(k), k= 1, import\_index(NEIBPETOT)
- Messages from each neighbor
  - RECVbuf(k), k= 1, import\_index(NEIBPETOT)

# RECV: MPI\_Isend/Irecv/Waitall Fortran

```

do neib= 1, NEIBPETOT
  iS_i= import_index(neib-1) + 1
  iE_i= import_index(neib )
  BUFlength_i= iE_i + 1 - iS_i

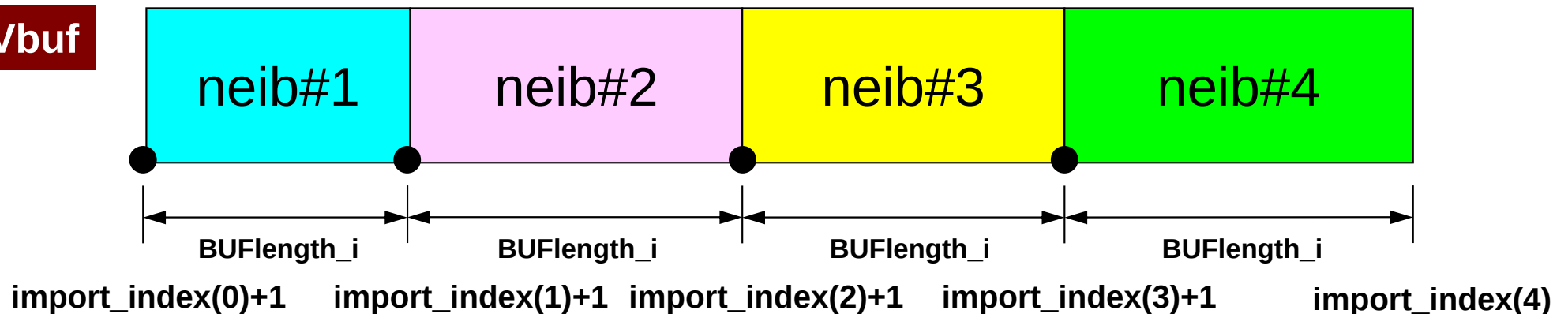
  call MPI_IRECV
&      (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&
&      MPI_COMM_WORLD, request_recv(neib), ierr)
enddo

call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

do neib= 1, NEIBPETOT
  do k= import_index(neib-1)+1, import_index(neib)
    kk= import_item(k)
    VAL(kk)= RECVbuf(k)
  enddo
enddo
    
```

Copied from receiving buffer

RECVbuf



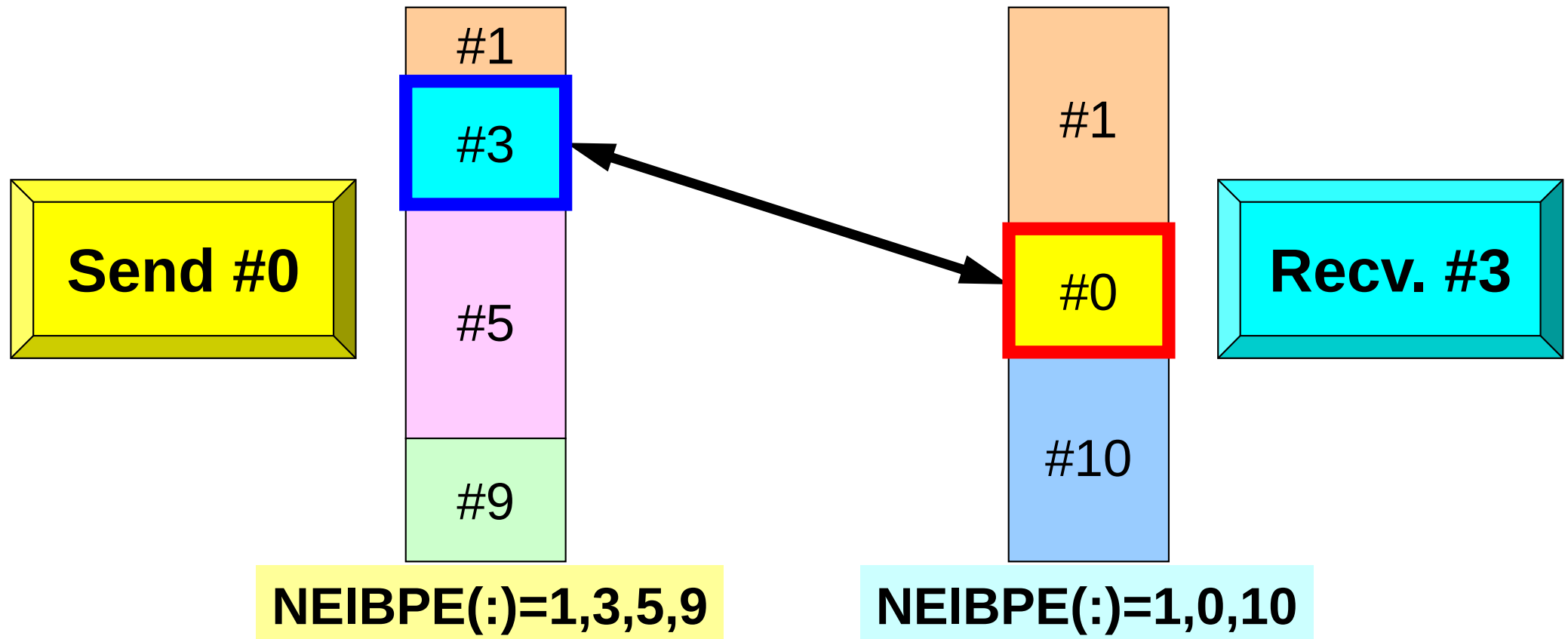
# Relationship SEND/RECV

```
do neib= 1, NEIBPETOT  
  iS_e= export_index(neib-1) + 1  
  iE_e= export_index(neib )  
  BUFlength_e= iE_e + 1 - iS_e  
  
  call MPI_ISEND  
&      (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&  
&      MPI_COMM_WORLD, request_send(neib), ierr)  
enddo
```

```
do neib= 1, NEIBPETOT  
  iS_i= import_index(neib-1) + 1  
  iE_i= import_index(neib )  
  BUFlength_i= iE_i + 1 - iS_i  
  
  call MPI_Irecv  
&      (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&  
&      MPI_COMM_WORLD, request_recv(neib), ierr)  
enddo
```

- Consistency of ID's of sources/destinations, size and contents of messages !
- Communication occurs when NEIBPE(neib) matches

# Relationship SEND/RECV (#0 to #3)



- Consistency of ID's of sources/destinations, size and contents of messages !
- Communication occurs when NEIBPE(neib) matches

# Generalized Comm. Table (1/6)

PE#2

| 21 | 22 | 23 | 24 |    |
|----|----|----|----|----|
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORT_index
4 8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4 8
#EXPORT_items
4
8
12
16
13
14
15
16
```

# Generalized Comm. Table (2/6)

PE#2

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

#NEIBPEtot      Number of neighbors  
2  
#NEIBPE            ID of neighbors  
1   2  
#NODE  
24 16              Ext/Int Pts, Int Pts  
#IMPORT\_index  
4   8  
#IMPORT\_items  
17  
18  
19  
20  
21  
22  
23  
24  
#EXPORT\_index  
4   8  
#EXPORT\_items  
4  
8  
12  
16  
13  
14  
15  
16

# Generalized Comm. Table (3/6)

PE#2

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORT_index
4 8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4 8
#EXPORT_items
4
8
12
16
13
14
15
16
```

Four ext pts (1<sup>st</sup>-4<sup>th</sup> items) are imported from 1<sup>st</sup> neighbor (PE#1), and four (5<sup>th</sup>-8<sup>th</sup> items) are from 2<sup>nd</sup> neighbor (PE#2).

# Generalized Comm. Table (4/6)

PE#2

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORT_index
4 8
#IMPORT_items
17
18 imported from 1st Neighbor
19 (PE#1) (1st-4th items)
20
21 imported from 2nd Neighbor
22 (PE#2) (5th-8th items)
23
24
#EXPORT_index
4 8
#EXPORT_items
4
8
12
16
13
14
15
16
```

# Generalized Comm. Table (5/6)

PE#2

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORT_index
4 8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4 8
#EXPORT_items
4
8
12
16
13
14
15
16
```

Four boundary pts (1<sup>st</sup>-4<sup>th</sup> items) are exported to 1<sup>st</sup> neighbor (PE#1), and four (5<sup>th</sup>-8<sup>th</sup> items) are to 2<sup>nd</sup> neighbor (PE#2).

# Generalized Comm. Table (6/6)

PE#2

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORT_index
4 8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4 8
#EXPORT_items
4
8
12
16
13
14
15
16
```

exported to 1<sup>st</sup> Neighbor  
(PE#1) (1<sup>st</sup>-4<sup>th</sup> items)

exported to 2<sup>nd</sup> Neighbor  
(PE#2) (5<sup>th</sup>-8<sup>th</sup> items)

# Generalized Comm. Table (6/6)

PE#2

|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#1

An external point is only sent from its original domain.

A boundary point could be referred from more than one domain, and sent to multiple domains (e.g. 16<sup>th</sup> mesh).

# Notice: Send/Recv Arrays

**#PE0**

send:

VEC(start\_send)~  
VEC(start\_send+length\_send-1)

**#PE1**

send:

VEC(start\_send)~  
VEC(start\_send+length\_send-1)

**#PE0**

recv:

VEC(start\_recv)~  
VEC(start\_recv+length\_recv-1)

**#PE1**

recv:

VEC(start\_recv)~  
VEC(start\_recv+length\_recv-1)

- “length\_send” of sending process must be equal to “length\_recv” of receiving process.
  - PE#0 to PE#1, PE#1 to PE#0
- “sendbuf” and “recvbuf”: different address

# Point-to-Point Communication

- What is PtoP Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

# Sample Program for 2D FDM

```
$ cd /work/gt36/t36XXX/pFEM/mpi/S2  
$ module load fj
```

```
$ mpifrtpx -Kfast sq-sr1.f  
$ mpifccpx -Nclang -Kfast sq-sr1.c
```

```
(modify go4.sh for 4 processes)  
$ pjsub go4.sh
```

# go4.sh

```
#!/bin/sh
#PJM -N "test"
#PJM -L rscgrp=lecture6-o
#PJM -L node=1
#PJM --mpi proc=4
#PJM -L elapse=00:15:00
#PJM -g gt36
#PJM -j
#PJM -e err
#PJM -o test.lst

module load fj
module load fjmpi

mpiexec ./a.out
```

# Example: sq-sr1.f (1/6)

Fortran

## Initialization

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'

integer(kind=4) :: my_rank, PETOT
integer(kind=4) :: N, NP, NEIBPETOT, BUFlength

integer(kind=4), dimension(:), allocatable :: VAL
integer(kind=4), dimension(:), allocatable :: SENDbuf, RECVbuf
integer(kind=4), dimension(:), allocatable :: NEIBPE

integer(kind=4), dimension(:), allocatable :: import_index, import_item
integer(kind=4), dimension(:), allocatable :: export_index, export_item

integer(kind=4), dimension(:, :), allocatable :: stat_send, stat_recv
integer(kind=4), dimension(: ), allocatable :: request_send
integer(kind=4), dimension(: ), allocatable :: request_recv

character(len=80)          :: filename, line

!C
!C +-----+
!C | INIT. MPI |
!C +-----+
!C===
call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )
```

# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
  if (my_rank.eq.0) filename= 'sqm.0'
  if (my_rank.eq.1) filename= 'sqm.1'
  if (my_rank.eq.2) filename= 'sqm.2'
  if (my_rank.eq.3) filename= 'sqm.3'
  open (21, file= filename, status= 'unknown')
    read (21,*) NEIBPETOT
      allocate (NEIBPE(NEIBPETOT))
      allocate (import_index(0:NEIBPETOT))
      allocate (export_index(0:NEIBPETOT))
      import_index= 0
      export_index= 0

    read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
    read (21,*) NP, N
    read (21,'(a80)') line
    read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
      nn= import_index(NEIBPETOT)
      allocate (import_item(nn))

    do i= 1, nn
      read (21,*) import_item(i)
    enddo
    read (21,'(a80)') line
    read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
      nn= export_index(NEIBPETOT)
      allocate (export_item(nn))

    do i= 1, nn
      read (21,*) export_item(i)
    enddo
  close (21)
```

# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
         read (21,*) NEIBPETOT
                allocate (NEIBPE(NEIBPETOT))
                allocate (import_index(0:NEIBPETOT))
                allocate (export_index(0:NEIBPETOT))
                        import_index= 0
                        export_index= 0

         read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
         read (21,*) NP, N

         read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                        nn= import_index(NEIBPETOT)
                        allocate (import_item(nn))

         do i= 1, nn
            read (21,*) import_item(i)
         enddo

         read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                        nn= export_index(NEIBPETOT)
                        allocate (export_item(nn))

         do i= 1, nn
            read (21,*) export_item(i)
         enddo
      close (21)
```

```
#NEIBPETot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```

# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
      read (21,*) NEIBPETOT
      allocate (NEIBPE(NEIBPETOT))
      allocate (import_index(0:NEIBPETOT))
      allocate (export_index(0:NEIBPETOT))
      import_index= 0
      export_index= 0

      read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
      read (21,*) NP, N
      read (21,*) line

      NP  Number of all meshes (internal + external)
      N   Number of internal meshes

      do i= 1, nn
        read (21,*) import_item(i)
      enddo
      read (21, '(a80)') line
      read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
      nn= export_index(NEIBPETOT)
      allocate (export_item(nn))

      do i= 1, nn
        read (21,*) export_item(i)
      enddo
      close (21)
```

```
#NEIBPETot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```

# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
      read (21,*) NEIBPETOT
      allocate (NEIBPE(NEIBPETOT))
      allocate (import_index(0:NEIBPETOT))
      allocate (export_index(0:NEIBPETOT))
      import_index= 0
      export_index= 0

      read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
      read (21,*) NP, N

      read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
      nn= import_index(NEIBPETOT)
      allocate (import_item(nn))

      do i= 1, nn
        read (21,*) import_item(i)
      enddo

      read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
      nn= export_index(NEIBPETOT)
      allocate (export_item(nn))

      do i= 1, nn
        read (21,*) export_item(i)
      enddo
      close (21)
```

```
#NEIBPETot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```

# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
      read (21,*) NEIBPETOT
      allocate (NEIBPE(NEIBPETOT))
      allocate (import_index(0:NEIBPETOT))
      allocate (export_index(0:NEIBPETOT))
      import_index= 0
      export_index= 0

      read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
      read (21,*) NP, N

      read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
      nn= import_index(NEIBPETOT)
      allocate (import_item(nn))

      do i= 1, nn
        read (21,*) import_item(i)
      enddo

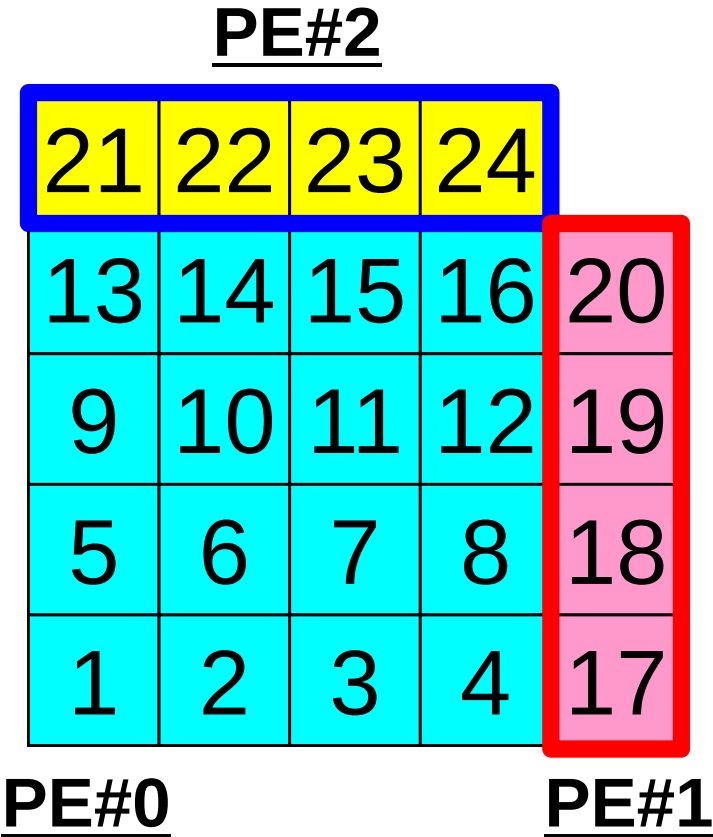
      read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
      nn= export_index(NEIBPETOT)
      allocate (export_item(nn))

      do i= 1, nn
        read (21,*) export_item(i)
      enddo
      close (21)
```

```
#NEIBPETot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```

# RECV/Import: PE#0

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```



# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
      read (21,*) NEIBPETOT
      allocate (NEIBPE(NEIBPETOT))
      allocate (import_index(0:NEIBPETOT))
      allocate (export_index(0:NEIBPETOT))
      import_index= 0
      export_index= 0

      read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
      read (21,*) NP, N

      read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
      nn= import_index(NEIBPETOT)
      allocate (import_item(nn))

      do i= 1, nn
        read (21,*) import_item(i)
      enddo

      read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
      nn= export_index(NEIBPETOT)
      allocate (export_item(nn))

      do i= 1, nn
        read (21,*) export_item(i)
      enddo
      close (21)
```

```
#NEIBPETot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```

# Example: sq-sr1.f (2/6)

Fortran

## Reading distributed local data files (sqm.\*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
      read (21,*) NEIBPETOT
      allocate (NEIBPE(NEIBPETOT))
      allocate (import_index(0:NEIBPETOT))
      allocate (export_index(0:NEIBPETOT))
      import_index= 0
      export_index= 0

      read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
      read (21,*) NP, N

      read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
      nn= import_index(NEIBPETOT)
      allocate (import_item(nn))

      do i= 1, nn
        read (21,*) import_item(i)
      enddo

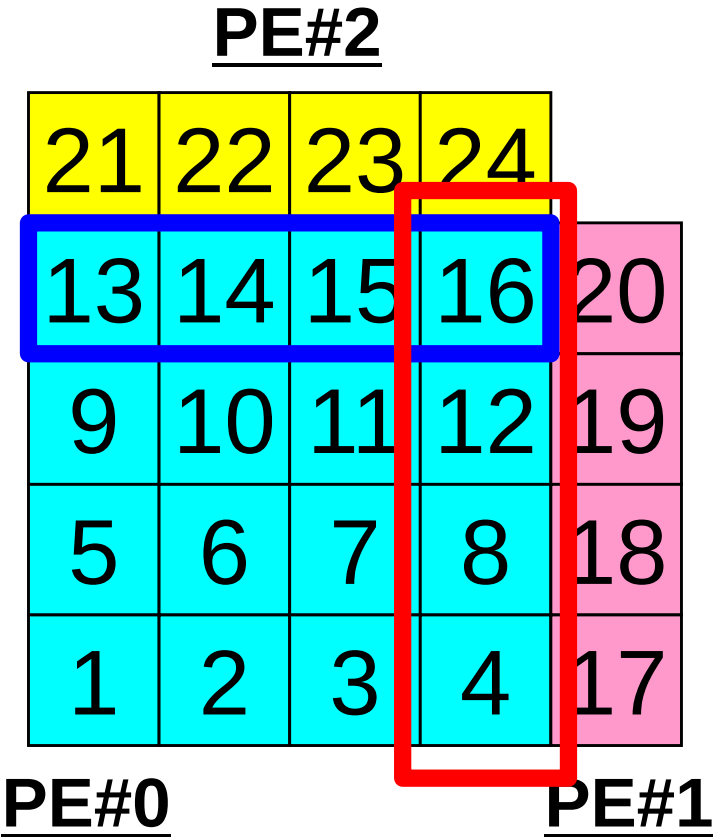
      read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
      nn= export_index(NEIBPETOT)
      allocate (export_item(nn))

      do i= 1, nn
        read (21,*) export_item(i)
      enddo
      close (21)
```

```
#NEIBPETot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```

# SEND/Export: PE#0

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```



# Example: sq-sr1.f (3/6)

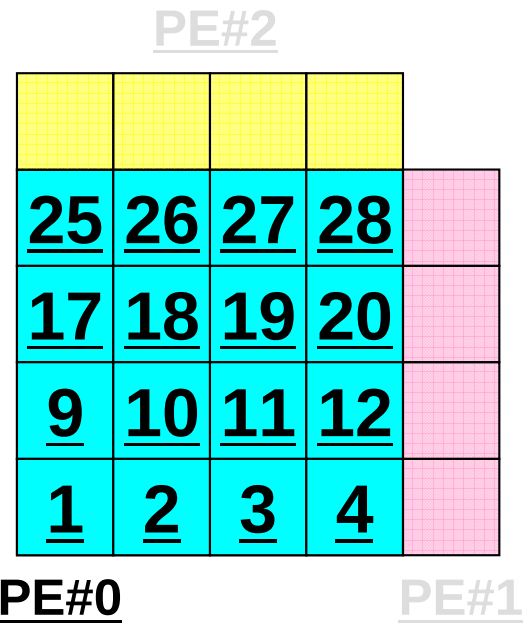
Reading distributed local data files (sq.\*)

```
!C
!C-- VAL.
      if (my_rank.eq.0) filename= 'sq.0'
      if (my_rank.eq.1) filename= 'sq.1'
      if (my_rank.eq.2) filename= 'sq.2'
      if (my_rank.eq.3) filename= 'sq.3'

      allocate (VAL(NP))
      VAL= 0
      open (21, file= filename, status= 'unknown')
        do i= 1, N
          read (21, *) VAL(i)
        enddo
      close (21)
!C==
```

**N** : Number of internal points  
**VAL**: Global ID of meshes

**VAL** on external points are unknown at this stage.



- 1
- 2
- 3
- 4
- 9
- 10
- 11
- 12
- 17
- 18
- 19
- 20
- 25
- 26
- 27
- 28

# Example: sq-sr1.f (4/6)

Fortran

## Preparation of sending/receiving buffers

```
!C
!C +-----+
!C | BUFFER |
!C +-----+
!C===
      allocate (SENDbuf(export_index(NEIBPETOT)))
      allocate (RECVbuf(import_index(NEIBPETOT)))
```

```
      SENDbuf= 0
      RECVbuf= 0
```

```
      do neib= 1, NEIBPETOT
        iS= export_index(neib-1) + 1
        iE= export_index(neib  )
        do i= iS, iE
          SENDbuf(i)= VAL(export_item(i))
        enddo
      enddo
```

```
!C===
```

Info. of boundary points is written into sending buffer (**SendBuf**).  
 Info. sent to **NEIBPE(neib)** is stored in **export\_index(neib-1)+1:export\_index(neib)**

# Sending Buffer is nice ...

Fortran

```

do neib= 1, NEIBPETOT
  iS_e= export_index(neib-1) + 1
  iE_e= export_index(neib )
  BUFlength_e= iE_e + 1 - iS_e

  call MPI_ISEND
&      (VAL(...), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&      MPI_COMM_WORLD, request_send(neib), ierr)
enddo

```

PE#2

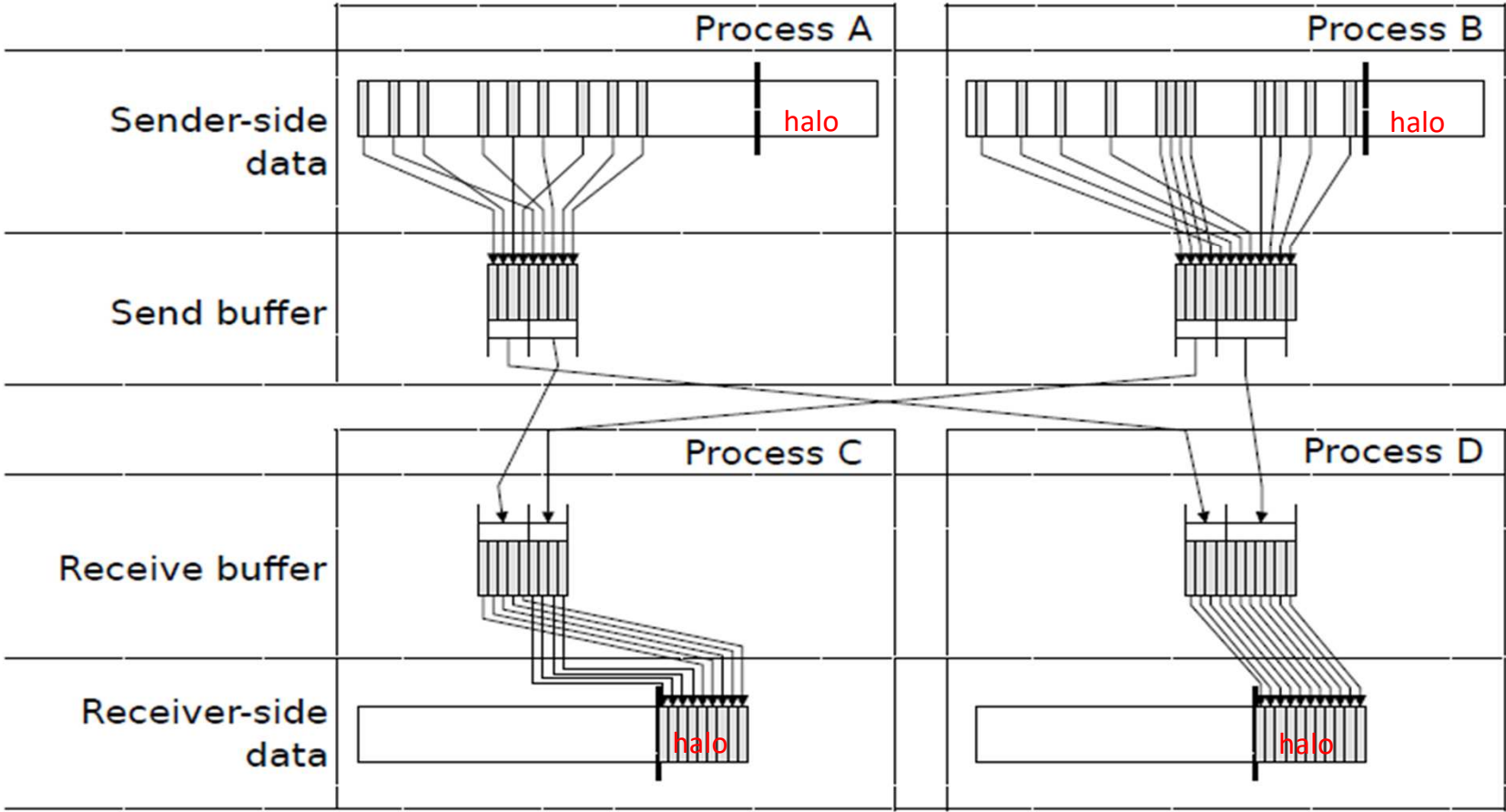
|    |    |    |    |    |
|----|----|----|----|----|
| 21 | 22 | 23 | 24 |    |
| 13 | 14 | 15 | 16 | 20 |
| 9  | 10 | 11 | 12 | 19 |
| 5  | 6  | 7  | 8  | 18 |
| 1  | 2  | 3  | 4  | 17 |

PE#0 PE#1

Numbering of these boundary nodes is not continuous, therefore the following procedure of MPI\_Isend is not applied directly:

- Starting address of sending buffer
- XX-messages from that address

# Communication Pattern using 1D Structure



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(Lawrence Berkeley National  
Laboratory) より借用

# Example: sq-sr1.f (5/6)

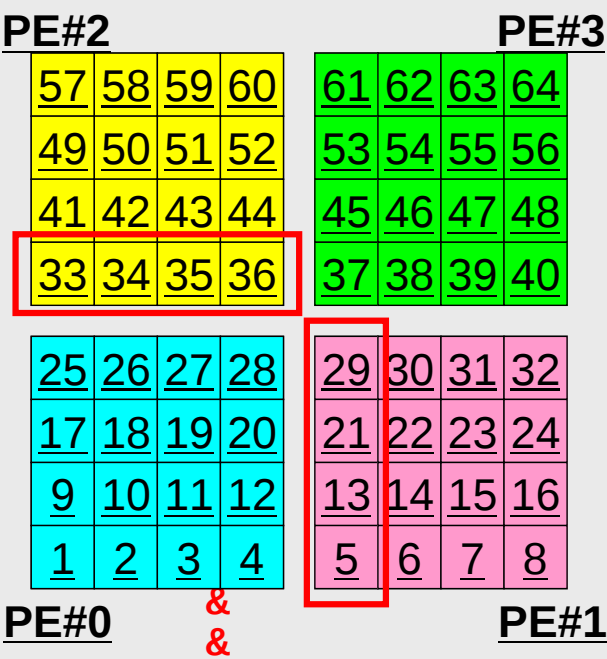
Fortran

SEND/Export: MPI\_Isend

```
!C
!C +-----+
!C | SEND-RECV |
!C +-----+
!C===
      allocate (stat_send(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (stat_recv(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (request_send(NEIBPETOT))
      allocate (request_recv(NEIBPETOT))

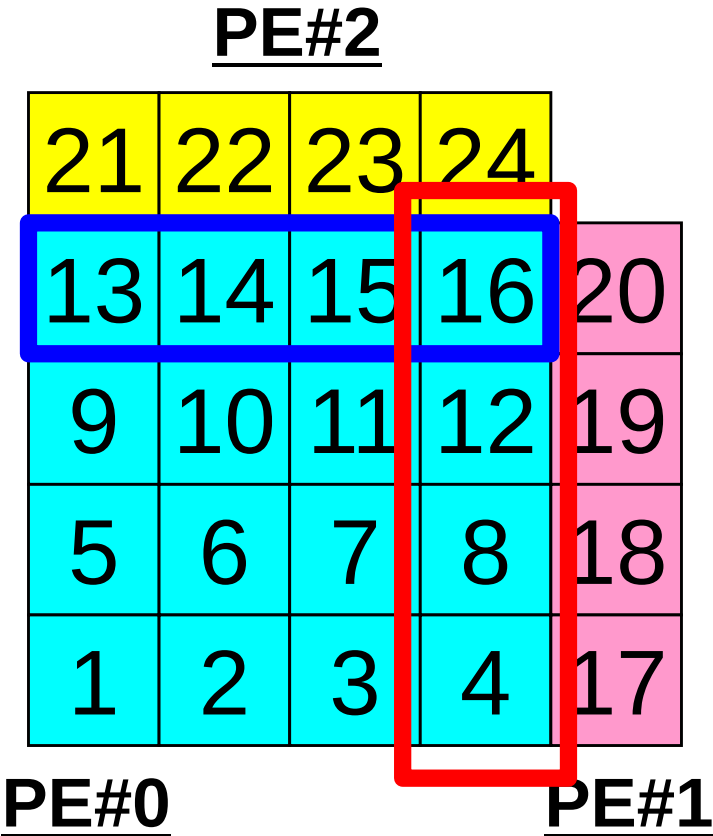
      do neib= 1, NEIBPETOT
        iS= export_index(neib-1) + 1
        iE= export_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_ISEND (SENDbuf(iS), BUFlength, MPI_INTEGER,
&                      NEIBPE(neib), 0, MPI_COMM_WORLD,
&                      request_send(neib), ierr)
      enddo

      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_IRECV (RECVbuf(iS), BUFlength, MPI_INTEGER,
&                      NEIBPE(neib), 0, MPI_COMM_WORLD,
&                      request_recv(neib), ierr)
      enddo
```



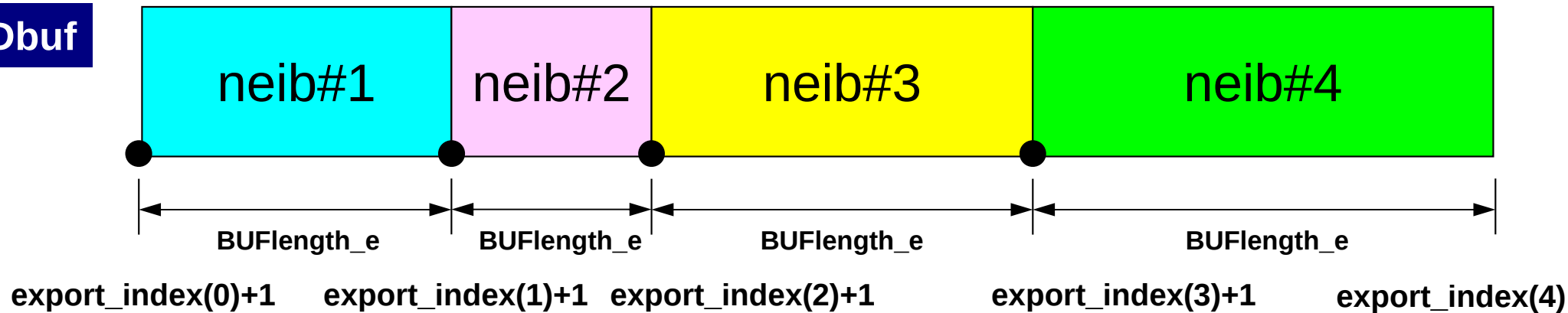
# SEND/Export: PE#0

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```



# SEND: MPI\_Isend/Irecv/Waitall Fortran

**SENDbuf**



```

do neib= 1, NEIBPETOT
  do k= export_index(neib-1)+1, export_index(neib)
    kk= export_item(k)
    SENDbuf(k)= VAL(kk)
  enddo
enddo

```

Copies to sending buffers

```

do neib= 1, NEIBPETOT
  iS_e= export_index(neib-1) + 1
  iE_e= export_index(neib)
  BUFlength_e= iE_e + 1 - iS_e

  call MPI_ISEND
&      (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&      MPI_COMM_WORLD, request_send(neib), ierr)
enddo

call MPI_WAITALL (NEIBPETOT, request_send, stat_recv, ierr)

```

# Example: sq-sr1.f (5/6)

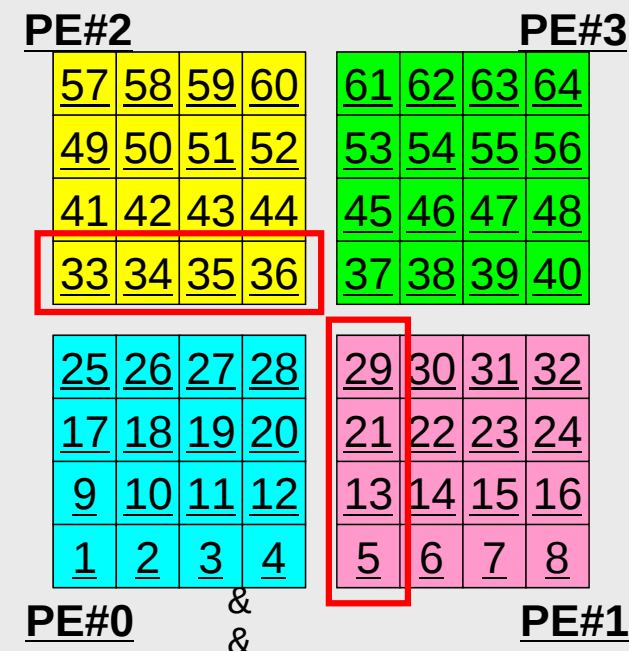
Fortran

RECV/Import: MPI\_Irecv

```
!C
!C +-----+
!C | SEND-RECV |
!C +-----+
!C===
      allocate (stat_send(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (stat_recv(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (request_send(NEIBPETOT))
      allocate (request_recv(NEIBPETOT))

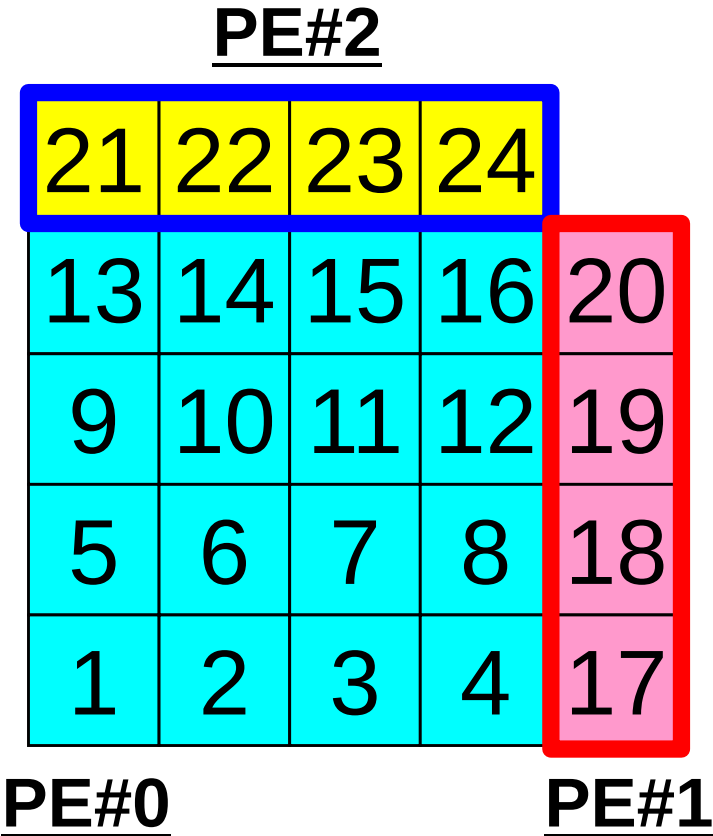
      do neib= 1, NEIBPETOT
        iS= export_index(neib-1) + 1
        iE= export_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_ISEND (SENDbuf(iS), BUFlength, MPI_INTEGER,
&                        NEIBPE(neib), 0, MPI_COMM_WORLD,
&                        request_send(neib), ierr)
      enddo

      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_IRECV (RECVbuf(iS), BUFlength, MPI_INTEGER,
&                        NEIBPE(neib), 0, MPI_COMM_WORLD,
&                        request_recv(neib), ierr)
      enddo
```



# RECV/Import: PE#0

```
#NEIBPEtot
2
#NEIBPE
1 2
#NODE
24 16
#IMPORTindex
4 8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4 8
#EXPORTitems
4
8
12
16
13
14
15
16
```



# RECV: MPI\_Isend/Irecv/Waitall Fortran

```

do neib= 1, NEIBPETOT
  iS_i= import_index(neib-1) + 1
  iE_i= import_index(neib )
  BUFlength_i= iE_i + 1 - iS_i

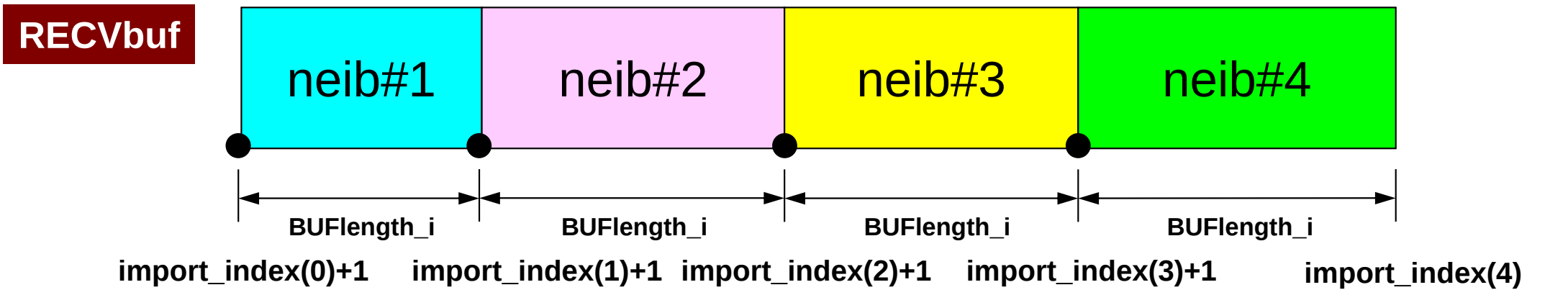
  call MPI_IRECV
&      (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&
&      MPI_COMM_WORLD, request_recv(neib), ierr)
enddo

call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

do neib= 1, NEIBPETOT
  do k= import_index(neib-1)+1, import_index(neib)
    kk= import_item(k)
    VAL(kk)= RECVbuf(k)
  enddo
enddo

```

Copies from receiving buffers



# Example: sq-sr1.f (6/6)

Fortran

## Reading info of ext pts from receiving buffers

```
call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)
```

```
do neib= 1, NEIBPETOT
  iS= import_index(neib-1) + 1
  iE= import_index(neib  )
  do i= iS, iE
    VAL(import_item(i))= RECVbuf(i)
  enddo
enddo
```

Contents of **RecvBuf** are copied to values at external points.

```
call MPI_WAITALL (NEIBPETOT, request_send, stat_send, ierr)
```

```
!C==
```

```
!C
```

```
!C +-----+
```

```
!C | OUTPUT |
```

```
!C +-----+
```

```
!C==
```

```
do neib= 1, NEIBPETOT
  iS= import_index(neib-1) + 1
  iE= import_index(neib  )
  do i= iS, iE
    in= import_item(i)
    write (*,'(a, 3i8)') 'RECVbuf', my_rank, NEIBPE(neib), VAL(in)
  enddo
enddo
```

```
!C==
```

```
call MPI_FINALIZE (ierr)
stop
```

```
end
```

# Example: sq-sr1.f (6/6)

Fortran

## Writing values at external points

```
call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

do neib= 1, NEIBPETOT
  iS= import_index(neib-1) + 1
  iE= import_index(neib  )
  do i= iS, iE
    VAL(import_item(i))= RECVbuf(i)
  enddo
enddo

call MPI_WAITALL (NEIBPETOT, request_send, stat_send, ierr)
!C===

!C
!C +-----+
!C | OUTPUT |
!C +-----+
!C===
      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        do i= iS, iE
          in= import_item(i)
          write (*,'(a, 3i8)') 'RECVbuf', my_rank, NEIBPE(neib), VAL(in)
        enddo
      enddo
!C===
call MPI_FINALIZE (ierr)
stop

end
```

# Results (PE#0)

PE#2

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |

PE#0

PE#3

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

PE#1

|         |   |   |    |
|---------|---|---|----|
| RECVbuf | 0 | 1 | 5  |
| RECVbuf | 0 | 1 | 13 |
| RECVbuf | 0 | 1 | 21 |
| RECVbuf | 0 | 1 | 29 |
| RECVbuf | 0 | 2 | 33 |
| RECVbuf | 0 | 2 | 34 |
| RECVbuf | 0 | 2 | 35 |
| RECVbuf | 0 | 2 | 36 |
| RECVbuf | 1 | 0 | 4  |
| RECVbuf | 1 | 0 | 12 |
| RECVbuf | 1 | 0 | 20 |
| RECVbuf | 1 | 0 | 28 |
| RECVbuf | 1 | 3 | 37 |
| RECVbuf | 1 | 3 | 38 |
| RECVbuf | 1 | 3 | 39 |
| RECVbuf | 1 | 3 | 40 |
| RECVbuf | 2 | 3 | 37 |
| RECVbuf | 2 | 3 | 45 |
| RECVbuf | 2 | 3 | 53 |
| RECVbuf | 2 | 3 | 61 |
| RECVbuf | 2 | 0 | 25 |
| RECVbuf | 2 | 0 | 26 |
| RECVbuf | 2 | 0 | 27 |
| RECVbuf | 2 | 0 | 28 |
| RECVbuf | 3 | 2 | 36 |
| RECVbuf | 3 | 2 | 44 |
| RECVbuf | 3 | 2 | 52 |
| RECVbuf | 3 | 2 | 60 |
| RECVbuf | 3 | 1 | 29 |
| RECVbuf | 3 | 1 | 30 |
| RECVbuf | 3 | 1 | 31 |
| RECVbuf | 3 | 1 | 32 |

# Results (PE#1)

PE#2

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |

PE#3

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

PE#0

PE#1

|         |   |   |    |
|---------|---|---|----|
| RECVbuf | 0 | 1 | 5  |
| RECVbuf | 0 | 1 | 13 |
| RECVbuf | 0 | 1 | 21 |
| RECVbuf | 0 | 1 | 29 |
| RECVbuf | 0 | 2 | 33 |
| RECVbuf | 0 | 2 | 34 |
| RECVbuf | 0 | 2 | 35 |
| RECVbuf | 0 | 2 | 36 |
| RECVbuf | 1 | 0 | 4  |
| RECVbuf | 1 | 0 | 12 |
| RECVbuf | 1 | 0 | 20 |
| RECVbuf | 1 | 0 | 28 |
| RECVbuf | 1 | 3 | 37 |
| RECVbuf | 1 | 3 | 38 |
| RECVbuf | 1 | 3 | 39 |
| RECVbuf | 1 | 3 | 40 |
| RECVbuf | 2 | 3 | 37 |
| RECVbuf | 2 | 3 | 45 |
| RECVbuf | 2 | 3 | 53 |
| RECVbuf | 2 | 3 | 61 |
| RECVbuf | 2 | 0 | 25 |
| RECVbuf | 2 | 0 | 26 |
| RECVbuf | 2 | 0 | 27 |
| RECVbuf | 2 | 0 | 28 |
| RECVbuf | 3 | 2 | 36 |
| RECVbuf | 3 | 2 | 44 |
| RECVbuf | 3 | 2 | 52 |
| RECVbuf | 3 | 2 | 60 |
| RECVbuf | 3 | 1 | 29 |
| RECVbuf | 3 | 1 | 30 |
| RECVbuf | 3 | 1 | 31 |
| RECVbuf | 3 | 1 | 32 |

# Results (PE#2)

PE#2

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |

PE#3

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

PE#0

PE#1

|         |   |   |    |
|---------|---|---|----|
| RECVbuf | 0 | 1 | 5  |
| RECVbuf | 0 | 1 | 13 |
| RECVbuf | 0 | 1 | 21 |
| RECVbuf | 0 | 1 | 29 |
| RECVbuf | 0 | 2 | 33 |
| RECVbuf | 0 | 2 | 34 |
| RECVbuf | 0 | 2 | 35 |
| RECVbuf | 0 | 2 | 36 |
| RECVbuf | 1 | 0 | 4  |
| RECVbuf | 1 | 0 | 12 |
| RECVbuf | 1 | 0 | 20 |
| RECVbuf | 1 | 0 | 28 |
| RECVbuf | 1 | 3 | 37 |
| RECVbuf | 1 | 3 | 38 |
| RECVbuf | 1 | 3 | 39 |
| RECVbuf | 1 | 3 | 40 |
| RECVbuf | 2 | 3 | 37 |
| RECVbuf | 2 | 3 | 45 |
| RECVbuf | 2 | 3 | 53 |
| RECVbuf | 2 | 3 | 61 |
| RECVbuf | 2 | 0 | 25 |
| RECVbuf | 2 | 0 | 26 |
| RECVbuf | 2 | 0 | 27 |
| RECVbuf | 2 | 0 | 28 |
| RECVbuf | 3 | 2 | 36 |
| RECVbuf | 3 | 2 | 44 |
| RECVbuf | 3 | 2 | 52 |
| RECVbuf | 3 | 2 | 60 |
| RECVbuf | 3 | 1 | 29 |
| RECVbuf | 3 | 1 | 30 |
| RECVbuf | 3 | 1 | 31 |
| RECVbuf | 3 | 1 | 32 |

# Results (PE#3)

PE#2

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>57</u> | <u>58</u> | <u>59</u> | <u>60</u> |
| <u>49</u> | <u>50</u> | <u>51</u> | <u>52</u> |
| <u>41</u> | <u>42</u> | <u>43</u> | <u>44</u> |
| <u>33</u> | <u>34</u> | <u>35</u> | <u>36</u> |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>25</u> | <u>26</u> | <u>27</u> | <u>28</u> |
| <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>9</u>  | <u>10</u> | <u>11</u> | <u>12</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  |

PE#0

PE#3

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>61</u> | <u>62</u> | <u>63</u> | <u>64</u> |
| <u>53</u> | <u>54</u> | <u>55</u> | <u>56</u> |
| <u>45</u> | <u>46</u> | <u>47</u> | <u>48</u> |
| <u>37</u> | <u>38</u> | <u>39</u> | <u>40</u> |

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>29</u> | <u>30</u> | <u>31</u> | <u>32</u> |
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>13</u> | <u>14</u> | <u>15</u> | <u>16</u> |
| <u>5</u>  | <u>6</u>  | <u>7</u>  | <u>8</u>  |

PE#1

|         |   |   |    |
|---------|---|---|----|
| RECVbuf | 0 | 1 | 5  |
| RECVbuf | 0 | 1 | 13 |
| RECVbuf | 0 | 1 | 21 |
| RECVbuf | 0 | 1 | 29 |
| RECVbuf | 0 | 2 | 33 |
| RECVbuf | 0 | 2 | 34 |
| RECVbuf | 0 | 2 | 35 |
| RECVbuf | 0 | 2 | 36 |
| RECVbuf | 1 | 0 | 4  |
| RECVbuf | 1 | 0 | 12 |
| RECVbuf | 1 | 0 | 20 |
| RECVbuf | 1 | 0 | 28 |
| RECVbuf | 1 | 3 | 37 |
| RECVbuf | 1 | 3 | 38 |
| RECVbuf | 1 | 3 | 39 |
| RECVbuf | 1 | 3 | 40 |
| RECVbuf | 2 | 3 | 37 |
| RECVbuf | 2 | 3 | 45 |
| RECVbuf | 2 | 3 | 53 |
| RECVbuf | 2 | 3 | 61 |
| RECVbuf | 2 | 0 | 25 |
| RECVbuf | 2 | 0 | 26 |
| RECVbuf | 2 | 0 | 27 |
| RECVbuf | 2 | 0 | 28 |
| RECVbuf | 3 | 2 | 36 |
| RECVbuf | 3 | 2 | 44 |
| RECVbuf | 3 | 2 | 52 |
| RECVbuf | 3 | 2 | 60 |
| RECVbuf | 3 | 1 | 29 |
| RECVbuf | 3 | 1 | 30 |
| RECVbuf | 3 | 1 | 31 |
| RECVbuf | 3 | 1 | 32 |

# Distributed Local Data Structure for Parallel Computation

- Distributed local data structure for domain-to-domain communications has been introduced, which is appropriate for such applications with sparse coefficient matrices (e.g. FDM, FEM, FVM etc.).
  - SPMD
  - Local Numbering: Internal pts to External pts
  - Generalized communication table
- Everything is easy, if proper data structure is defined:
  - Values at boundary pts are copied into sending buffers
  - Send/Recv
  - Values at external pts are updated through receiving buffers

# Initial Mesh

t2

|           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> | <u>25</u> |
| <u>16</u> | <u>17</u> | <u>18</u> | <u>19</u> | <u>20</u> |
| <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> | <u>15</u> |
| <u>6</u>  | <u>7</u>  | <u>8</u>  | <u>9</u>  | <u>10</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u>  | <u>5</u>  |

# Three Domains

t2

#PE2

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>21</u> | <u>22</u> | <u>23</u> | <u>24</u> |
| <u>16</u> | <u>17</u> | <u>18</u> | <u>19</u> |
| <u>11</u> | <u>12</u> | <u>13</u> | <u>14</u> |
| <u>6</u>  | <u>7</u>  | <u>8</u>  |           |

#PE1

|           |           |           |
|-----------|-----------|-----------|
| <u>23</u> | <u>24</u> | <u>25</u> |
| <u>18</u> | <u>19</u> | <u>20</u> |
| <u>13</u> | <u>14</u> | <u>15</u> |
| <u>8</u>  | <u>9</u>  | <u>10</u> |
|           | <u>4</u>  | <u>5</u>  |

#PE0

|           |           |           |          |           |
|-----------|-----------|-----------|----------|-----------|
| <u>11</u> | <u>12</u> | <u>13</u> |          |           |
| <u>6</u>  | <u>7</u>  | <u>8</u>  | <u>9</u> | <u>10</u> |
| <u>1</u>  | <u>2</u>  | <u>3</u>  | <u>4</u> | <u>5</u>  |

# Three Domains

t2

#PE2

|                       |                       |                       |                        |
|-----------------------|-----------------------|-----------------------|------------------------|
| <b>7</b><br><u>21</u> | <b>8</b><br><u>22</u> | <b>9</b><br><u>23</u> | <b>15</b><br><u>24</u> |
| <b>4</b><br><u>16</u> | <b>5</b><br><u>17</u> | <b>6</b><br><u>18</u> | <b>14</b><br><u>19</u> |
| <b>1</b><br><u>11</u> | <b>2</b><br><u>12</u> | <b>3</b><br><u>13</u> | <b>13</b><br><u>14</u> |
| <b>10</b><br><u>6</u> | <b>11</b><br><u>7</u> | <b>12</b><br><u>8</u> |                        |

#PE1

|                        |                       |                       |
|------------------------|-----------------------|-----------------------|
| <b>14</b><br><u>23</u> | <b>7</b><br><u>24</u> | <b>8</b><br><u>25</u> |
| <b>13</b><br><u>18</u> | <b>5</b><br><u>19</u> | <b>6</b><br><u>20</u> |
| <b>12</b><br><u>13</u> | <b>3</b><br><u>14</u> | <b>4</b><br><u>15</u> |
| <b>11</b><br><u>8</u>  | <b>1</b><br><u>9</u>  | <b>2</b><br><u>10</u> |
|                        | <b>9</b><br><u>4</u>  | <b>10</b><br><u>5</u> |

#PE0

|                        |                        |                        |                      |                        |
|------------------------|------------------------|------------------------|----------------------|------------------------|
| <b>11</b><br><u>11</u> | <b>12</b><br><u>12</u> | <b>13</b><br><u>13</u> |                      |                        |
| <b>6</b><br><u>6</u>   | <b>7</b><br><u>7</u>   | <b>8</b><br><u>8</u>   | <b>9</b><br><u>9</u> | <b>10</b><br><u>10</u> |
| <b>1</b><br><u>1</u>   | <b>2</b><br><u>2</u>   | <b>3</b><br><u>3</u>   | <b>4</b><br><u>4</u> | <b>5</b><br><u>5</u>   |

# PE#0: sqm.0: fill O's

#PE2

|                |                |                |                 |
|----------------|----------------|----------------|-----------------|
| <u>7</u><br>21 | <u>8</u><br>22 | <u>9</u><br>23 | <u>15</u><br>24 |
| <u>4</u><br>16 | <u>5</u><br>17 | <u>6</u><br>18 | <u>14</u><br>19 |
| <u>1</u><br>11 | <u>2</u><br>12 | <u>3</u><br>13 | <u>13</u><br>14 |
| <u>10</u><br>6 | <u>11</u><br>7 | <u>12</u><br>8 |                 |

#PE1

|                 |                |                |
|-----------------|----------------|----------------|
| <u>14</u><br>23 | <u>7</u><br>24 | <u>8</u><br>25 |
| <u>13</u><br>18 | <u>5</u><br>19 | <u>6</u><br>20 |
| <u>12</u><br>13 | <u>3</u><br>14 | <u>4</u><br>15 |
| <u>11</u><br>8  | <u>1</u><br>9  | <u>2</u><br>10 |
|                 | <u>9</u><br>4  | <u>10</u><br>5 |

#PE0

|                 |                 |                 |               |                 |
|-----------------|-----------------|-----------------|---------------|-----------------|
| <u>11</u><br>11 | <u>12</u><br>12 | <u>13</u><br>13 |               |                 |
| <u>6</u><br>6   | <u>7</u><br>7   | <u>8</u><br>8   | <u>9</u><br>9 | <u>10</u><br>10 |
| <u>1</u><br>1   | <u>2</u><br>2   | <u>3</u><br>3   | <u>4</u><br>4 | <u>5</u><br>5   |

```
#NEIBPEtot
    2
#NEIBPE
    1      2
#NODE
    13      8 (int+ext, int pts)
#IMPORTindex
    O      O
#IMPORTitems
    O...
#EXPORTindex
    O      O
#EXPORTitems
    O...
```

# PE#1: sqm.1: fill O's

#PE2

|                |                |                |                 |
|----------------|----------------|----------------|-----------------|
| <u>7</u><br>21 | <u>8</u><br>22 | <u>9</u><br>23 | <u>15</u><br>24 |
| <u>4</u><br>16 | <u>5</u><br>17 | <u>6</u><br>18 | <u>14</u><br>19 |
| <u>1</u><br>11 | <u>2</u><br>12 | <u>3</u><br>13 | <u>13</u><br>14 |
| <u>10</u><br>6 | <u>11</u><br>7 | <u>12</u><br>8 |                 |

#PE1

|                 |                |                |
|-----------------|----------------|----------------|
| <u>14</u><br>23 | <u>7</u><br>24 | <u>8</u><br>25 |
| <u>13</u><br>18 | <u>5</u><br>19 | <u>6</u><br>20 |
| <u>12</u><br>13 | <u>3</u><br>14 | <u>4</u><br>15 |
| <u>11</u><br>8  | <u>1</u><br>9  | <u>2</u><br>10 |
|                 | <u>9</u><br>4  | <u>10</u><br>5 |

#PE0

|                 |                 |                 |               |                 |
|-----------------|-----------------|-----------------|---------------|-----------------|
| <u>11</u><br>11 | <u>12</u><br>12 | <u>13</u><br>13 |               |                 |
| <u>6</u><br>6   | <u>7</u><br>7   | <u>8</u><br>8   | <u>9</u><br>9 | <u>10</u><br>10 |
| <u>1</u><br>1   | <u>2</u><br>2   | <u>3</u><br>3   | <u>4</u><br>4 | <u>5</u><br>5   |

```
#NEIBPEtot
    2
#NEIBPE
    0      2
#NODE
    14      8 (int+ext, int pts)
#IMPORTindex
    ○      ○
#IMPORTitems
    ○...
#EXPORTindex
    ○      ○
#EXPORTitems
    ○...
```

# PE#2: sqm.2: fill O's

#PE2

|                |                |                |                 |
|----------------|----------------|----------------|-----------------|
| <u>7</u><br>21 | <u>8</u><br>22 | <u>9</u><br>23 | <u>15</u><br>24 |
| <u>4</u><br>16 | <u>5</u><br>17 | <u>6</u><br>18 | <u>14</u><br>19 |
| <u>1</u><br>11 | <u>2</u><br>12 | <u>3</u><br>13 | <u>13</u><br>14 |
| <u>10</u><br>6 | <u>11</u><br>7 | <u>12</u><br>8 |                 |

#PE1

|                 |                |                |
|-----------------|----------------|----------------|
| <u>14</u><br>23 | <u>7</u><br>24 | <u>8</u><br>25 |
| <u>13</u><br>18 | <u>5</u><br>19 | <u>6</u><br>20 |
| <u>12</u><br>13 | <u>3</u><br>14 | <u>4</u><br>15 |
| <u>11</u><br>8  | <u>1</u><br>9  | <u>2</u><br>10 |
|                 | <u>9</u><br>4  | <u>10</u><br>5 |

#PE0

|                 |                 |                 |               |                 |
|-----------------|-----------------|-----------------|---------------|-----------------|
| <u>11</u><br>11 | <u>12</u><br>12 | <u>13</u><br>13 |               |                 |
| <u>6</u><br>6   | <u>7</u><br>7   | <u>8</u><br>8   | <u>9</u><br>9 | <u>10</u><br>10 |
| <u>1</u><br>1   | <u>2</u><br>2   | <u>3</u><br>3   | <u>4</u><br>4 | <u>5</u><br>5   |

```
#NEIBPEtot
    2
#NEIBPE
    1      0
#NODE
    15      9 (int+ext, int pts)
#IMPORTindex
    ○      ○
#IMPORTitems
    ○...
#EXPORTindex
    ○      ○
#EXPORTitems
    ○...
```

t2

#PE2

|                |                |                |                 |
|----------------|----------------|----------------|-----------------|
| 7<br><u>21</u> | 8<br><u>22</u> | 9<br><u>23</u> | 15<br><u>24</u> |
| 4<br><u>16</u> | 5<br><u>17</u> | 6<br><u>18</u> | 14<br><u>19</u> |
| 1<br><u>11</u> | 2<br><u>12</u> | 3<br><u>13</u> | 13<br><u>14</u> |
| 10<br><u>6</u> | 11<br><u>7</u> | 12<br><u>8</u> |                 |

#PE1

|                 |                |                |
|-----------------|----------------|----------------|
| 14<br><u>23</u> | 7<br><u>24</u> | 8<br><u>25</u> |
| 13<br><u>18</u> | 5<br><u>19</u> | 6<br><u>20</u> |
| 12<br><u>13</u> | 3<br><u>14</u> | 4<br><u>15</u> |
| 11<br><u>8</u>  | 1<br><u>9</u>  | 2<br><u>10</u> |
|                 | 9<br><u>4</u>  | 10<br><u>5</u> |

#PE0

|                 |                 |                 |               |                 |
|-----------------|-----------------|-----------------|---------------|-----------------|
| 11<br><u>11</u> | 12<br><u>12</u> | 13<br><u>13</u> |               |                 |
| 6<br><u>6</u>   | 7<br><u>7</u>   | 8<br><u>8</u>   | 9<br><u>9</u> | 10<br><u>10</u> |
| 1<br><u>1</u>   | 2<br><u>2</u>   | 3<br><u>3</u>   | 4<br><u>4</u> | 5<br><u>5</u>   |

# Procedures

- Number of Internal/External Points
- Where do External Pts come from ?
  - **IMPORTindex, IMPORTitems**
  - Sequence of **NEIBPE**
- Then check destinations of Boundary Pts.
  - **EXPORTindex, EXPORTitems**
  - Sequence of **NEIBPE**
- “sq.\*” are in **<\$0-S2>/ex**
- Create “sqm.\*” by yourself
- copy <\$0-S2>/a.out (by sq-sr1.f) to <\$0-S2>/ex
- pjsb go3.sh

# Report S2 (1/2)

- Parallelize 1D code (1d.c) using MPI
- Read entire element number, and decompose into sub-domains in your program
- Validate the results
  - Answer of Original Code = Answer of Parallel Code
  - Explain why number of iterations does not change, as number of MPI processes changes.
- Measure parallel performance

# Report S2 (2/2)

- ~~• Deadline: January 24<sup>th</sup> (Wed), 2024, 17:00@ITC-LMS~~
- Problem
  - Apply “Generalized Communication Table”
  - Read entire elem. #, decompose into sub-domains in your program
  - Evaluate parallel performance
    - You need huge number of elements, to get excellent performance.
    - Fix number of iterations (e.g. 100), if computations cannot be completed.
- ~~• Report~~
  - ~~– Cover Page: Name, ID, and Problem ID (S2) must be written.~~
  - ~~– Less than eight pages including figures and tables (A4).~~
    - ~~• Strategy, Structure of the Program, Remarks~~
  - ~~– Source list of the program (if you have bugs)~~
  - ~~– Output list (as small as possible)~~

### a012.sh

```
#!/bin/sh
#PJM -N "test"
#PJM -L rscgrp=lecture6-o
#PJM -L node=1
#PJM --mpi proc=12
#PJM -L elapse=00:15:00
#PJM -g gt36
#PJM -j
#PJM -e err
#PJM -o test.lst
```

```
module load fj
module load fjmpi
mpiexec ./a.out
mpiexec numactl -l ./a.out
```

### a048.sh

```
#!/bin/sh
#PJM -N "test"
#PJM -L rscgrp=lecture6-o
#PJM -L node=1
#PJM --mpi proc=48
#PJM -L elapse=00:15:00
#PJM -g gt36
#PJM -j
#PJM -e err
#PJM -o test.lst
```

```
module load fj
module load fjmpi
mpiexec ./a.out
mpiexec numactl -l ./a.out
```

### a384.sh

```
#!/bin/sh
#PJM -N "test"
#PJM -L rscgrp=lecture6-o
#PJM -L node=8
#PJM --mpi proc=384
#PJM -L elapse=00:15:00
#PJM -g gt36
#PJM -j
#PJM -e err
#PJM -o test.lst
```

```
module load fj
module load fjmpi
mpiexec ./a.out
mpiexec numactl -l ./a.out
```

### a576.sh

```
#!/bin/sh
#PJM -N "test"
#PJM -L rscgrp=lecture6-o
#PJM -L node=12
#PJM --mpi proc=576
#PJM -L elapse=00:15:00
#PJM -g gt36
#PJM -j
#PJM -e err
#PJM -o test.lst
```

```
module load fj
module load fjmpi
mpiexec ./a.out
mpiexec numactl -l ./a.out
```

**numactl -l/--localalloc for utilizing local memory (no effects)**

# Number of Processes

|      |            |      |               |                            |
|------|------------|------|---------------|----------------------------|
| #PJM | -L node=1; | #PJM | --mpi proc= 1 | 1-node, 1-proc, 1-proc/n   |
| #PJM | -L node=1; | #PJM | --mpi proc= 4 | 1-node, 4-proc, 4-proc/n   |
| #PJM | -L node=1; | #PJM | --mpi proc=12 | 1-node, 12-proc, 12-proc/n |
| #PJM | -L node=1; | #PJM | --mpi proc=24 | 1-node, 24-proc, 24-proc/n |
| #PJM | -L node=1; | #PJM | --mpi proc=48 | 1-node, 48-proc, 48-proc/n |

|      |             |      |                |                              |
|------|-------------|------|----------------|------------------------------|
| #PJM | -L node= 4; | #PJM | --mpi proc=192 | 4-node, 192-proc, 48-proc/n  |
| #PJM | -L node= 8; | #PJM | --mpi proc=384 | 8-node, 384-proc, 48-proc/n  |
| #PJM | -L node=12; | #PJM | --mpi proc=576 | 12-node, 576-proc, 48-proc/n |

