

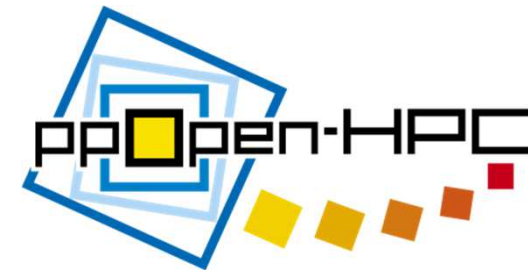
# **Communication-Computation Overlapping with Dynamic Loop Scheduling for Preconditioned Parallel Iterative Solvers on Multicore/Manycore Clusters**

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Processing (ICPP 2017)  
August 14, 2017, Bristol, UK**

# Acknowledgements

- JST-CREST, Japan
  - ppOpen-HPC Project
- DFG-SPPEXA, Germany
  - ESSEX-II Project
- JCAHPC (Joint Center for Advanced High Performance Computing)
  - CCS, University of Tsukuba
  - ITC, The University of Tokyo
- Prof. Scott Baden (LBNL)
- Dr. Jack Deslippe (LBNL)



**FY**

Category	Supercomputer Name	Hardware	Performance
Peta	Hitachi SR11K/J2	IBM Power-5+	18.8TFLOPS, 16.4TB
K	Yayoi: Hitachi SR16000/M1	IBM Power-7	54.9 TFLOPS, 11.2 TB
K computer	Hitachi HA8000 (T2K)	AMD Opteron	140TFLOPS, 31.3TB
GPU Cluster	Oakforest-PACS	Fujitsu, Intel KNL	25PFLOPS, 919.3TB
Post-K ?	JCAHPC:	Tsukuba, Tokyo	
	Oakleaf-FX: Fujitsu PRIMEHPC	FX10, SPARC64 IXfx	1.13 PFLOPS, 150 TB
	BDEC System		50+ PFLOPS (?)
	Oakbridge-FX		136.2 TFLOPS, 18.4 TB
	Big Data & Extreme Computing		
	Integrated Supercomputer System for Data Analyses & Scientific Simulations		
	Reedbush, SGI	Broadwell + Pascal	1.80-1.93 PFLOPS
	GPU Cluster		1.40+ PFLOPS

# Oakforest-PACS (OFP)

- Full Operation started on December 1, 2016
- 8,208 Intel Xeon/Phi (KNL), 25 PF Peak Performance
  - Fujitsu
- **TOP 500 #7 (#1 in Japan), HPCG #5 (#2) (June 2017)**
- **JCAHPC: Joint Center for Advanced High Performance Computing**
  - University of Tsukuba
  - University of Tokyo
    - New system will installed in Kashiwa-no-Ha (Leaf of Oak) Campus/U.Tokyo, which is between Tokyo and Tsukuba
  - <http://jcahpc.jp>



東京大学  
THE UNIVERSITY OF TOKYO



筑波大学  
University of Tsukuba

# Features of Oakforest-PACS

- Computing Node
  - 68 cores/node, 3 TFLOPS x 8,208= 25 PFLOPS
  - 2 Types of Memory
    - MCDRAM: High-Speed, Large-Latency, 16GB
    - DDR4: Medium-Speed, 96GB
  - Variety of Selections for Memory-Mode/Cluster-Mode
- Node-to-Node Communication
  - Fat-Tree Network with Full Bi-Section Bandwidth
  - Intel's Omni-Path Architecture
    - High Efficiency for Applications with Full Nodes of the System
    - Flexible and Efficient Operations for Multiple Jobs

- Introduction
- Dynamic Loop Scheduling
- Hardware Environment
- Preliminary Results by Parallel FEM (GeoFEM/Cube)
- Strong Scaling
- SAI Preconditioning
- Summary

# Overview of the Present Work

- Communication-Computation Overlapping (CC-Overlapping) in Sparse Matrix-Vector Multiplication (SpMV)
- Dynamic Loop Scheduling of OpenMP
- Performance Evaluation by Parallel FEM Application (GeoFEM/Cube) on multicore/manycore clusters.
- Performance Improvement by 40%-50% for Preconditioned CG Solvers in Strong Scaling up to 16,384 cores of Fujitsu PRIMEHPC FX10 (FX10) and KNL Cluster (Oakforest-PACS, OFP).
- 15%-20% improvement for GeoFEM/Cube with SAI-BiCGSTAB using 12,288 cores of Fujitsu FX10 and OFP.

# Communication/Synchronization

## Avoiding/Reducing/Hiding

### for Parallel Preconditioned Krylov Iterative Methods

- Dot Products
  - Pipelined Methods [Ghysels et al. 2014]
  - Gropp's Algorithm
  - Utilization of asynchronous collective communications (e.g. MPI\_allreduce) supported in MPI-3 for hiding such overhead.
- SpMV
  - Overlapping of Comp. & Comm. (CC-Overlapping)
  - + Dynamic Loop Scheduling
  - Matrix Powers Kernels [Hoemmen et al. 2010]

```

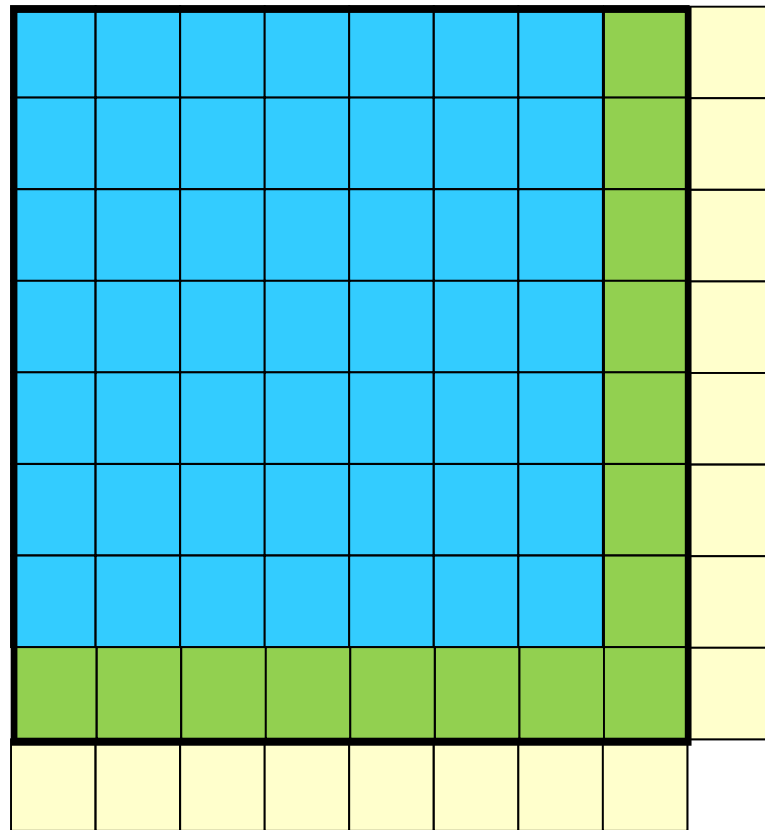
Compute  $r^{(0)} = b - [A]x^{(0)}$ 
for  $i = 1, 2, \dots$ 
  solve  $[M]z^{(i-1)} = r^{(i-1)}$ 
   $\rho_{i-1} = r^{(i-1)} z^{(i-1)}$ 
  if  $i = 1$ 
     $p^{(1)} = z^{(0)}$ 
  else
     $\beta_{i-1} = \rho_{i-1} / \rho_{i-2}$ 
     $p^{(i)} = z^{(i-1)} + \beta_{i-1} p^{(i-1)}$ 
  endif
   $q^{(i)} = [A]p^{(i)}$ 
   $\alpha_i = \rho_{i-1} / p^{(i)} q^{(i)}$ 
   $x^{(i)} = x^{(i-1)} + \alpha_i p^{(i)}$ 
   $r^{(i)} = r^{(i-1)} - \alpha_i q^{(i)}$ 
  check convergence  $|r|$ 
end

```



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# Comm.-Comp. Overlapping (CC-Overlapping): Static



Pure Internal Meshes



External (HALO) Meshes



Internal Meshes on  
Boundary's  
(Boundary Meshes)

```
call MPI_Isend
call MPI_Irecv
```

```
do i= 1, Ninn
  (calculations)
enddo
call MPI_Waitall
```

```
do i= Ninn+1, Nall
  (calculations)
enddo
```

Good for Stencil  
Not so Effective SpMV

# Dynamic Loop Scheduling (1/2)

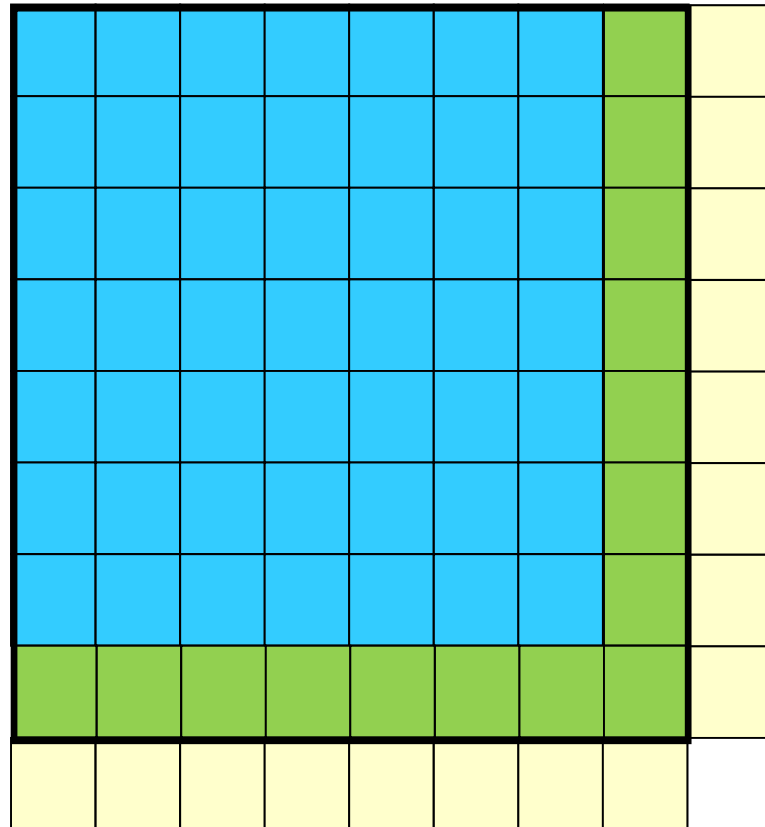
- CC-Overlapping in HALO Exchange
  - HALO exchange including sending buffer copy is done by the *master* thread
  - Dynamic loop scheduling is applied to the computations for *pure* internal nodes/meshes
  - The computations for pure internal nodes/meshes starts without master thread, while the master thread is doing communications.
  - The master thread can join the computations for pure internal nodes/meshes after completion of the communication.
- There are four different loop scheduling types (*kinds*) (*static*, *dynamic*, *guided*, *auto*), and the optional parameter (*chunk*) must be a positive integer:

**C: #pragma omp parallel for schedule (kind [, chunk])**  
**Fortran: !\$omp parallel do schedule (kind [,chunk])**

# Dynamic Loop Scheduling (2/2)

- The kind “*static*” is the default, and loops are divided into equal-sized chunks (or as equal as possible)
  - By default, chunk size is loop-count/number-of-threads.
- If the kind “*dynamic*” is applied, the internal work queue is used for giving a chunk-sized block of loop iterations to each thread.
  - When operations of a thread have finished, that retrieves the next block of loop iterations from the top of the work queue.
  - The chunk size is equal to 1 by default.
  - Extra overhead for scheduling is involved for this type of scheduling.
- (Next Page) Pseudo Code with Dynamic Loop Scheduling
  - Global communications are done by the master thread between “!\$omp master” and “!\$omp end master”.
  - The loop for computations of pure inner nodes/meshes with dynamic scheduling starts without the master thread, and that join the loop operations after the completion of communications.
  - Smaller value of *chunk size* may prevent *load imbalance* among threads, but extra operations related to the internal work occur more frequently for smaller *chunk size*, which may lead to very significant overhead.

# Comm.-Comp. Overlapping + Dynamic Loop Scheduling: Dynamic



Pure Internal Meshes



External (HALO) Meshes



Internal Meshes on  
Boundary's  
(Boundary Meshes)

```
call MPI_Isend
call MPI_Irecv
call MPI_Waitall
```

Master

```
do i= 1, Ninn
  (calculations)
enddo
```

Dynamic

```
do i= Ninn+1, Nall
  (calculations)
enddo
```

Static

# Dynamic Loop Scheduling

- “dynamic”
- “!\$omp master~!\$omp end master”

```
!$omp parallel private (neib, j, k, i, X1, X2, X3, WVAL1, WVAL2, WVAL3)
!$omp&                private (istart, inum, ii, ierr)
```

```
!$omp master           Communication is done by the master thread (#0)
!C
!C- Send & Recv.
(...)
    call MPI_WAITALL (2*NEIBPETOT, req1, stal, ierr)
!$omp end master
```

```
!C
!C-- Pure Internal Nodes    The master thread can join computing of internal
                           nodes after the completion of communication
```

```
!$omp do schedule (dynamic,200)    Chunk Size= 200
  do j= 1, Ninn
    (...)
  enddo
```

```
!C
!C-- Boundary Nodes        Computing for boundary nodes are by all threads
```

```
!$omp do                default: !$omp do schedule (static)
  do j= Ninn+1, N
    (...)
  enddo
```

```
!$omp end parallel
```

Ina, T., Asahi, Y., Idomura, Y., Development of optimization of stencil calculation on Tera-flops many-core architecture, IPSJ SIG Technical Reports 2015-HPC-152-10, 2015 (in Japanese)

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# 3 of 5 used for the present work

- Yayoi (Hitachi SR16000, IBM Power7)
  - 54.9 TF, Nov. 2011 – Oct. 2017
- Oakleaf-FX (Fujitsu PRIMEHPC FX10)
  - 1.135 PF, Commercial Version of K, Apr.2012 – Mar.2018
- Oakbridge-FX (Fujitsu PRIMEHPC FX10)
  - 136.2 TF, for long-time use (up to 168 hr), Apr.2014 – Mar.2018
- **Reedbush (SGI, Intel BDW + NVIDIA P100 (Pascal))**
  - Integrated Supercomputer System for Data Analyses & Sc Simulations
  - 1.93 PF, Jul.2016-Jun.2020
  - Our first GPU System (Mar.2017), DDN IME (Burst Buffer)
- **Oakforest-PACS (OFP) (Fujitsu, Intel Xeon Phi (KNL))**
  - JCAHPC (U.Tsukuba & U.Tokyo)
  - 25 PF, #6 in 48<sup>th</sup> TOP 500 (Nov.2016) (#1 in Japan)
  - Omni-Path Architecture, DDN IME (Burst Buffer)





Code Name	KNL	BDW	FX10
Architecture	Intel Xeon Phi 7250 (Knights Landing)	Intel Xeon E5-2695 v4 (Broadwell-EP)	SPARC IX fx
Frequency (GHz)	1.40	2.10	1.848
Core # (Max Thread #)	68 (272)	18 (18)	16 (16)
Peak Performance (GFLOPS)	3,046.4	604.8	236.5
Memory (GB)	MCDRAM: 16 DDR4: 96	128	32
Memory Bandwidth(GB/sec., Stream Triad)	MCDRAM: 490 DDR4: 80.1	65.5	64.7
Out-of-Order	Y	Y	N
System	Oakforest-PACS	Reedbush-U	Oakleaf-FX

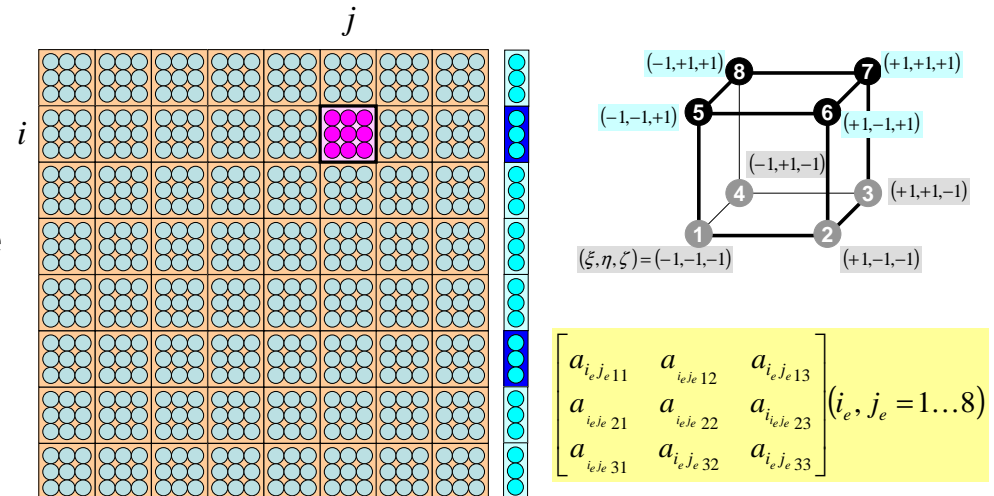
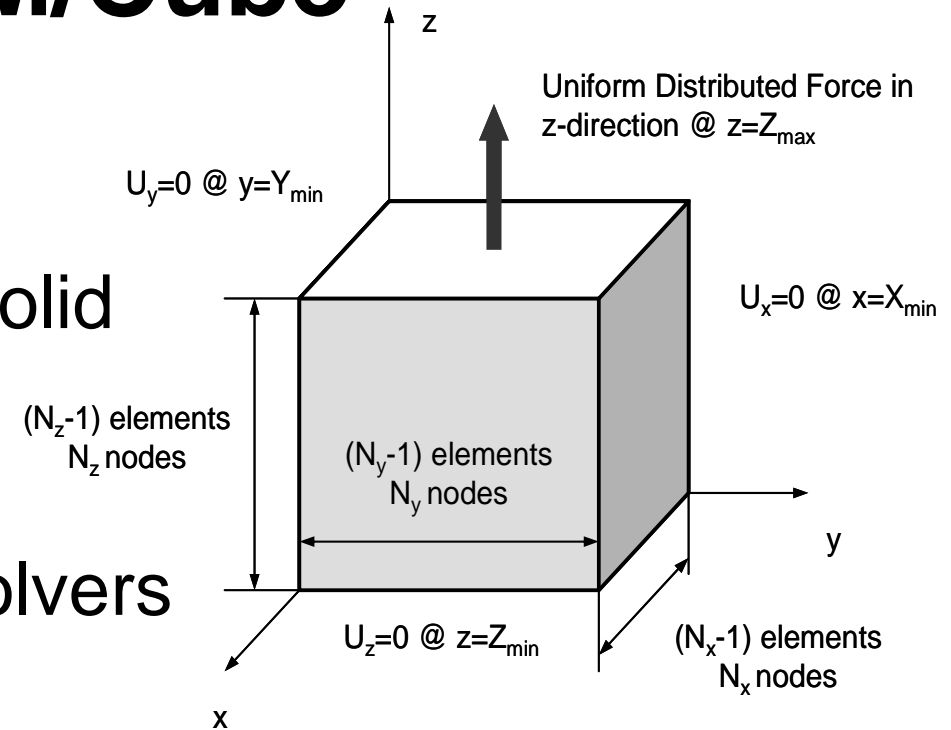
Code Name	KNL	BDW	FX10
Architecture	Intel Xeon Phi 7250 (Knights Landing)	Intel Xeon E5-2695 v4 (Broadwell-EP)	SPARC IX fx
Frequency (GHz)	1.40	2.10	1.848
Core # (Max Thread #)	68 (272)	18 (18)	16 (16)
<b>Peak Performance (GFLOPS)/core</b>	<b>44.8</b>	<b>33.6</b>	<b>14.8</b>
<b>Memory Bandwidth(GB/sec., Stream Triad)/core</b>	<b>MCDRAM: 7.21 DDR4: 1.24</b>	<b>3.64</b>	<b>4.04</b>
Out-of-Order	Y	Y	N
Network	Omni-Path Architecture	Mellanox EDR Infiniband	Tofu 6D Torus

- Introduction
- Dynamic Loop Scheduling
- Hardware Environment
- **Preliminary Results by Parallel FEM**
- Strong Scaling
- SAI Preconditioning
- Summary



# GeoFEM/Cube

- Parallel FEM Code (& Benchmarks)
- 3D-Static-Elastic-Linear (Solid Mechanics)
- Performance of Parallel Preconditioned Iterative Solvers
  - 3D Tri-linear Hexahedral Elements
  - **Block Diagonal LU + CG**
  - Fortran90+MPI+OpenMP
  - Distributed Data Structure
  - MPI, OpenMP, OpenMP/MPI Hybrid
  - **Block CRS Format**



# Configurations (1/2)

- Parallel Programming Model
  - Hybrid  $M \times N$  (HB  $M \times N$ )
    - “M”: Number of OpenMP threads for each MPI process,
    - “N”: Number of MPI processes on each CPU/socket.
  - FX10 and BDW: Flat MPI, HB  $2 \times 8$ ,  $4 \times 4$ ,  $8 \times 2$ ,  $16 \times 1$ .
    - 16 of 18 cores on each socket used for BDW
  - Because each core of KNL can host up to four threads, we applied three configurations, 1T (1 thread per core), 2T (2 threads per core) and 4T (4 threads per core).
    - Therefore,  $M \times N = 64$  for 1T, 128 for 2T, and 256 for 4T.
    - (1T) Flat MPI, HB  $2 \times 32$ ,  $4 \times 16$ ,  $8 \times 8$ ,  $16 \times 4$ ,  $32 \times 2$ ,  $64 \times 1$
    - (2T) HB  $2 \times 64$ ,  $4 \times 32$ ,  $8 \times 16$ ,  $16 \times 8$ ,  $32 \times 4$ ,  $64 \times 2$ ,  $128 \times 1$
    - (4T) only HB  $32 \times 8$  has been applied to limited cases.
    - Flat/Quadrant, Only MCDRAM
  - Each core of BDW can host two threads by hyper-threading, but this capability is deactivated on the Reedbush-U.

# Configurations (2/2)

- **Original**
  - Original code without any *CC-Overlapping*. Local computation of SpMV starts after completion of HALO exchange.
- **Static**
  - *CC-Overlapping* with *static* loop scheduling is applied.
- **Dynamic**
  - *CC-Overlapping* with *dynamic* loop scheduling is applied.
  - *Chunk size* has been changed from 10 to 500.
- **Measurement: 5 times, Median's (and error-bar's) are shown**

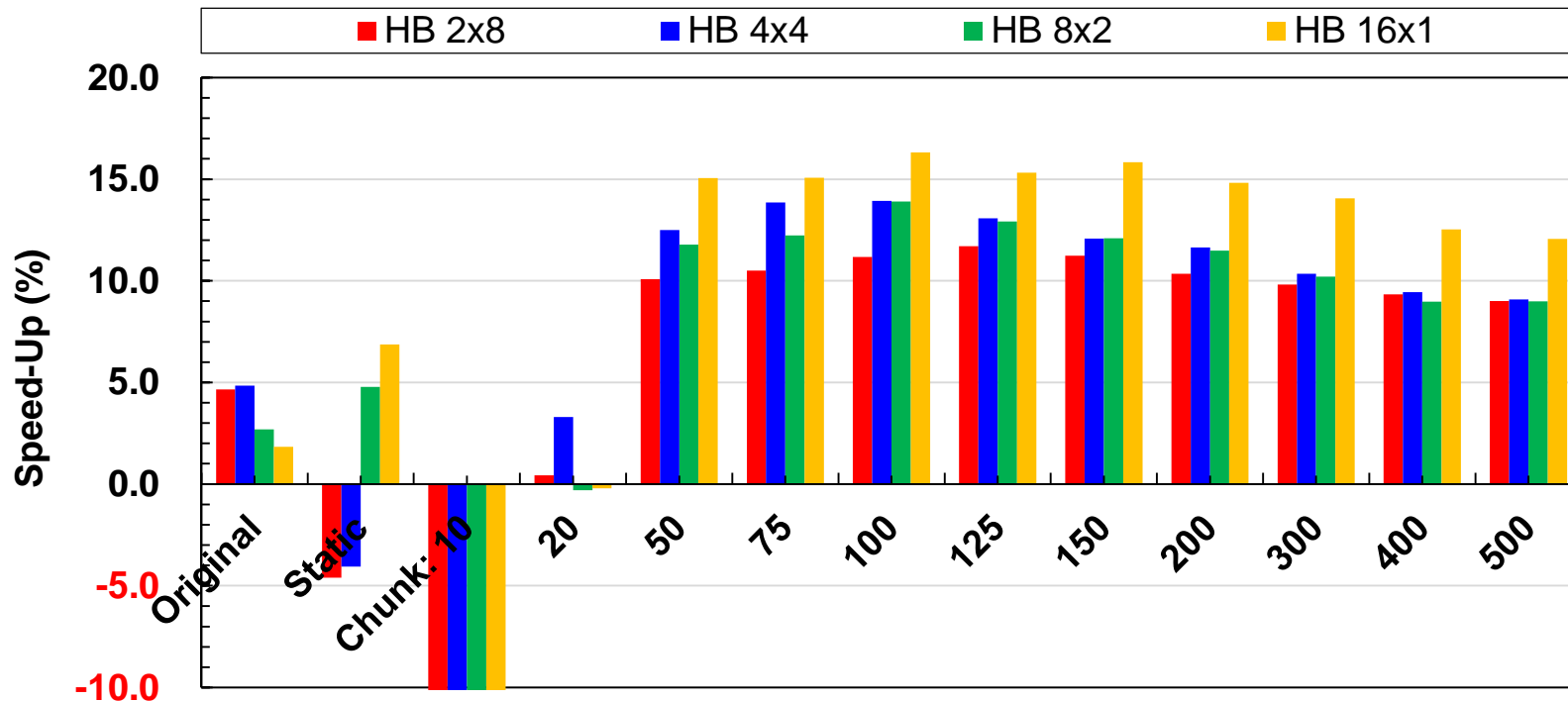
# Target Problem

- Performance of GeoFEM/Cube with 3,840 cores of each system
  - 240 nodes of FX10
  - 120 nodes (240 sockets) of BDW
  - 60 nodes of KNL
- The 1<sup>st</sup> problem includes 122,880,000 FEM nodes ( $=640 \times 480 \times 400$ ), and 368,640,000 DOF
  - each CPU/socket of FX10 and BDW has 512,000 nodes ( $=80 \times 80 \times 80$ ), and 1,536,000 DOF.
- The 2nd problem includes  $800 \times 600 \times 500$  nodes, and 720,000,000 DOF
  - $100^3$  nodes for each CPU/socket of FX10 and BDW

# Preliminary Results: FX10

240 nodes, 3,840 cores, 368,640,000 DOF  
(=640×480×400×3),

Improvement of CG from Original Flat MPI





# FX10: 240 nodes, 368,640,000 DOF

## HB 16x1, Performance Analysis by Fujitsu's Profiler (single node)

	Original	Static	Dynamic: Chunk Size=100	Dynamic: Chunk Size=500
GFLOPS/node	12.59	13.33	14.47	13.82
Memory Throughput (GB/sec)	61.61	64.86	69.44	68.07
L2 Throughput (GB/sec)	71.13	75.03	84.15	79.03
sec./(100 iterations)	2.21	2.10	1.93	2.00
Synchronous waiting time between threads (sec) Averaged	.229	.122	.073	.061
L2 waiting for FP Load (sec) Averaged	.655	.657	.540	.614

[sec]

2.5E+00

2.0E+00

1.5E+00

1.0E+00

0.5E+00

0.0E+00

-5.0E-01

Thread 0 Thread 1 Thread 2 Thread 3 Thread 4 Thread 5 Thread 6 Thread 7 Thread 8 Thread 9 Thread 10 Thread 11 Thread 12 Thread 13 Thread 14 Thread 15

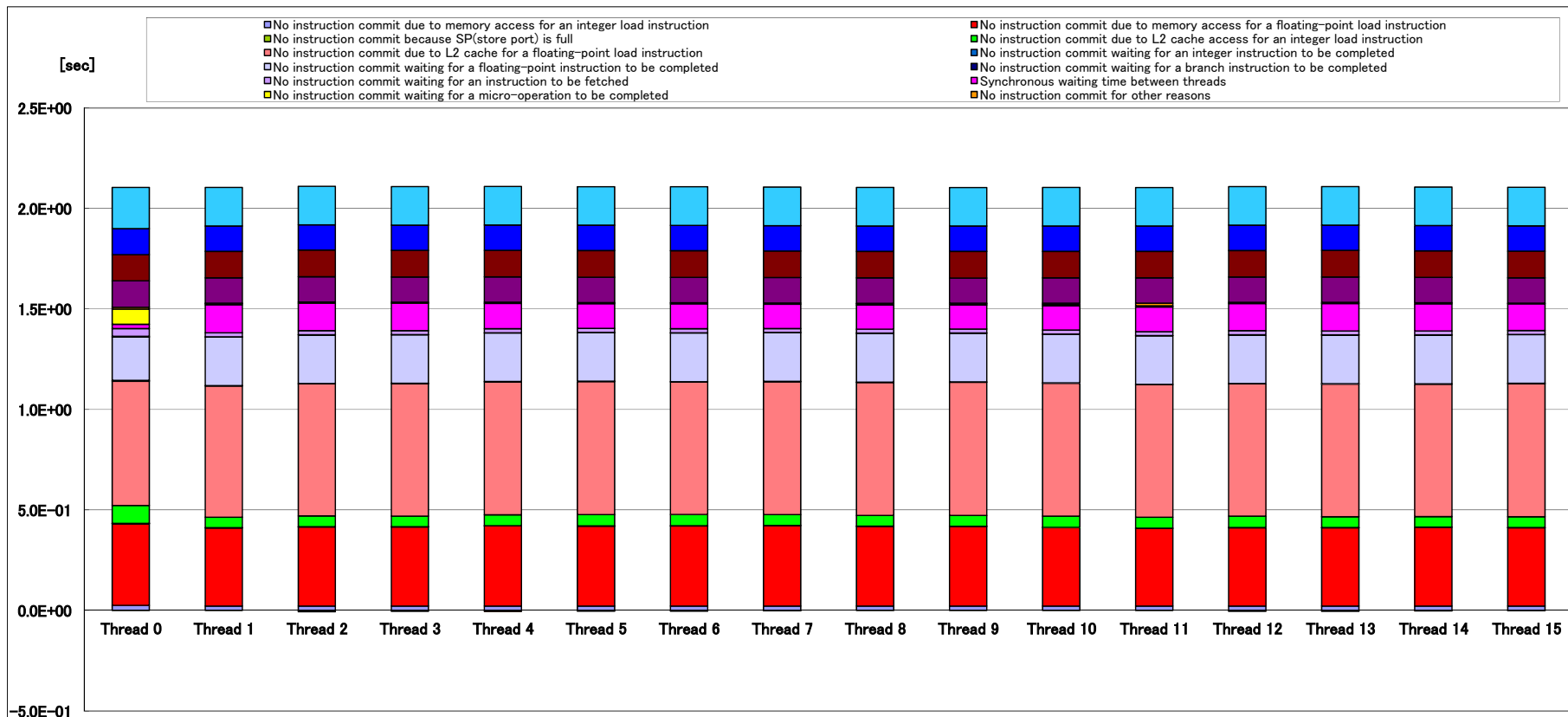
- No instruction commit due to memory access for an integer load instruction
- No instruction commit because SP(store port) is full
- No instruction commit due to L2 cache for a floating-point load instruction
- No instruction commit waiting for a floating-point instruction to be completed
- No instruction commit waiting for an instruction to be fetched
- No instruction commit waiting for a micro-operation to be completed
- No instruction commit due to memory access for a floating-point load instruction
- No instruction commit due to L2 cache access for an integer load instruction
- No instruction commit waiting for an integer instruction to be completed
- No instruction commit waiting for a branch instruction to be completed
- Synchronous waiting time between threads
- No instruction commit for other reasons

# 3,840 cores, PA Profiler

## FX10: 240 nodes, 368,640,000 DOF

### “Static”: 2.10 sec.

■ Synchronization Waiting, ■ L2 Load

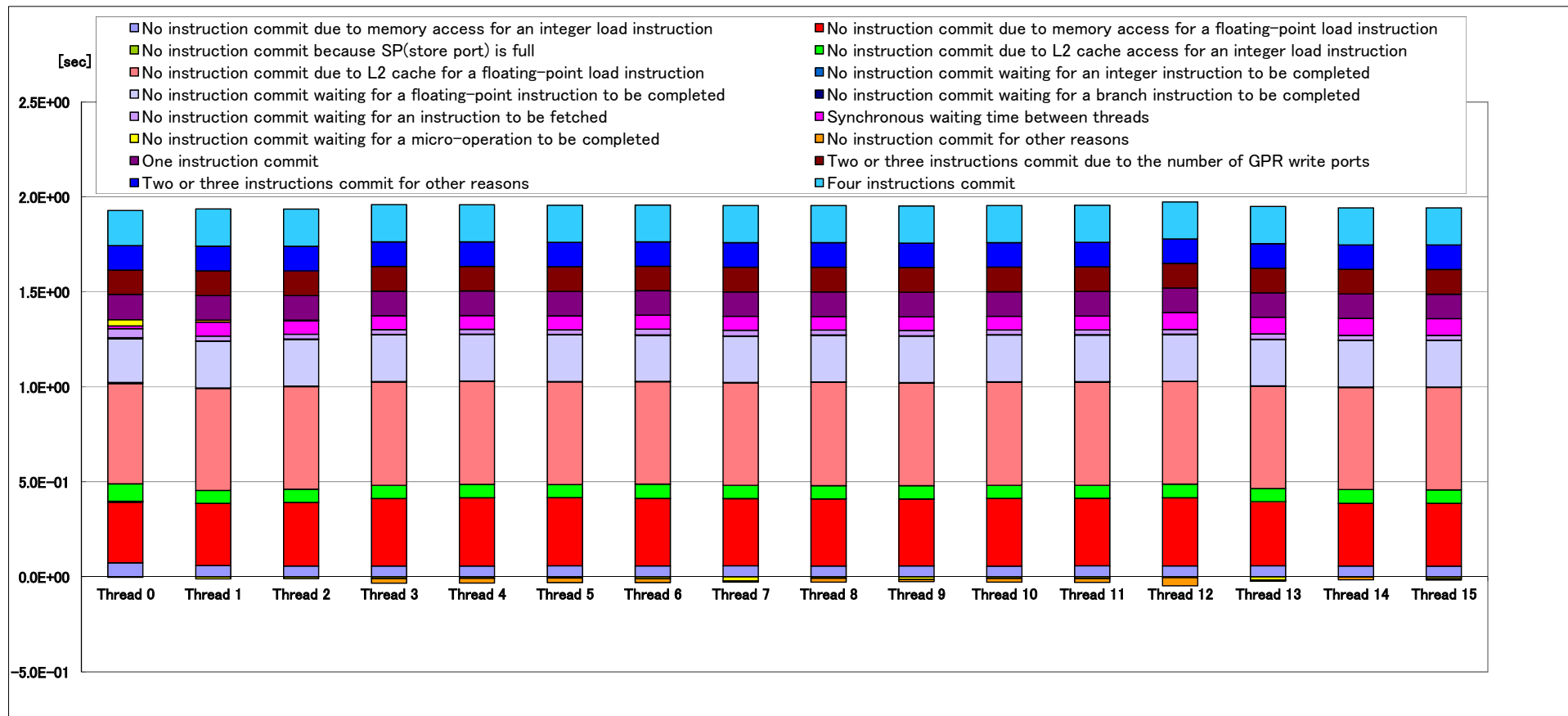


# 3,840 cores, PA Profiler

## FX10: 240 nodes, 368,640,000 DOF

### “Dynamic, Csz=100”: 1.93 sec.

■ Synchronization Waiting, ■ L2 Load

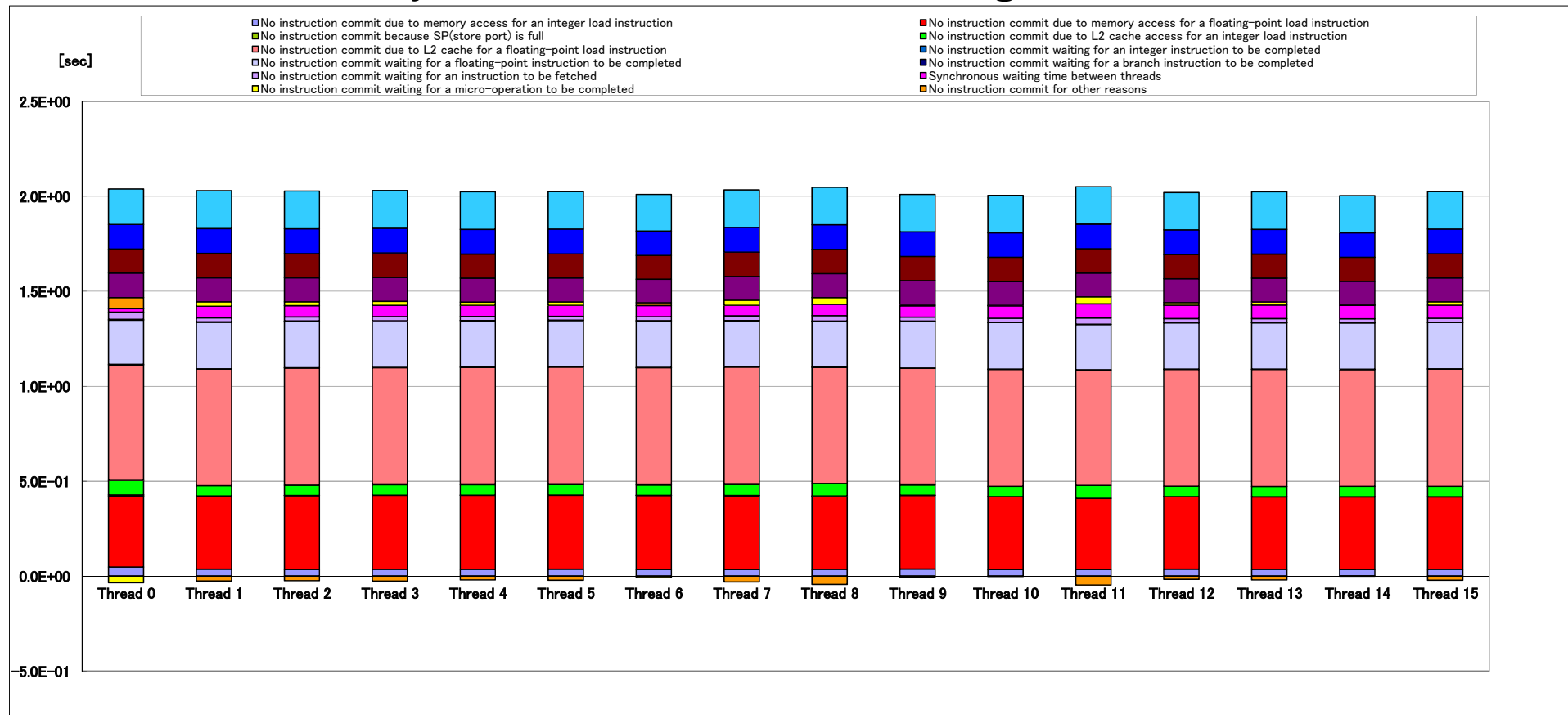


# 3,840 cores, PA Profiler

## FX10: 240 nodes, 368,640,000 DOF

### “Dynamic, Csz=500”: 2.00 sec.

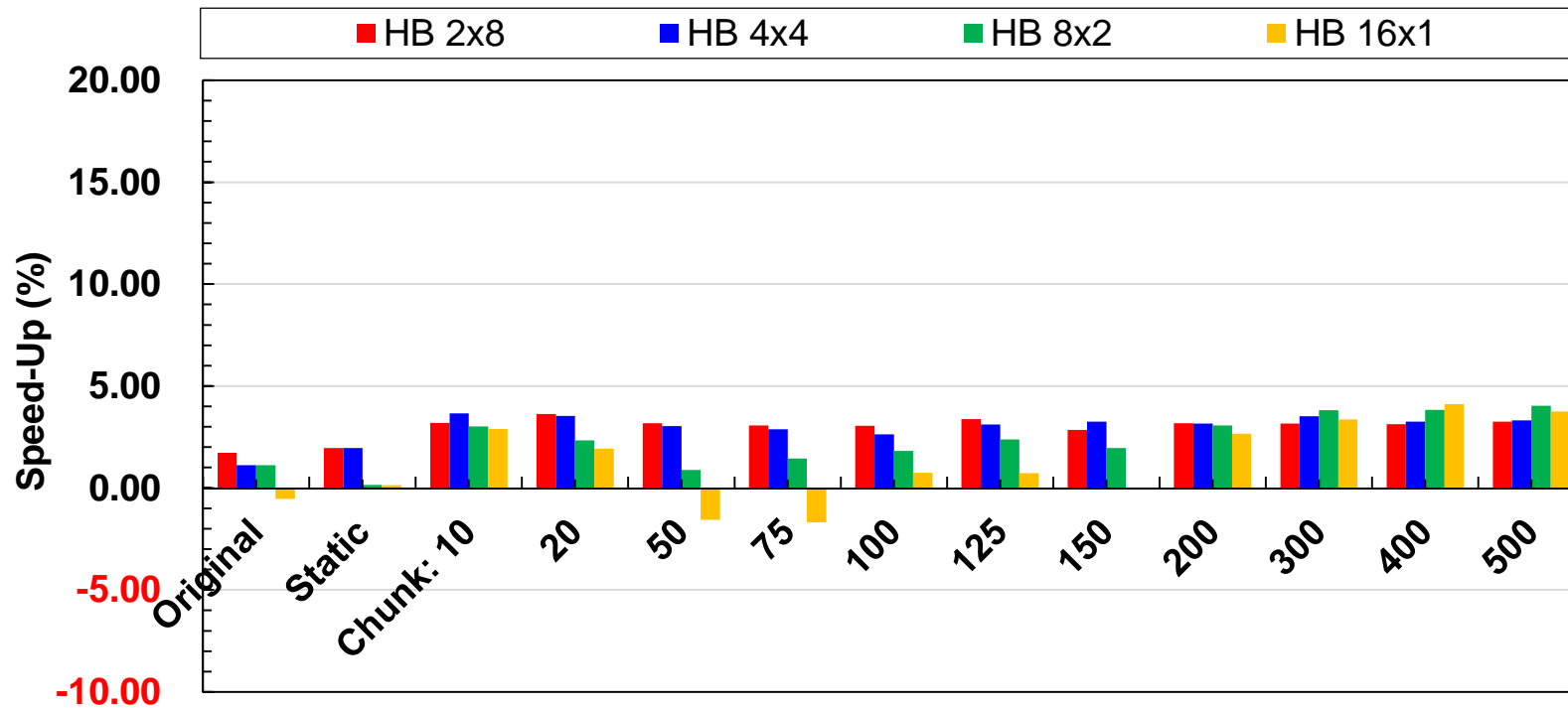
■ Synchronization Waiting, ■ L2 Load



# Preliminary Results: BDW

120 nodes, 3,840 cores, 368,640,000 DOF  
(=640×480×400×3),

Improvement of CG from Original Flat MPI

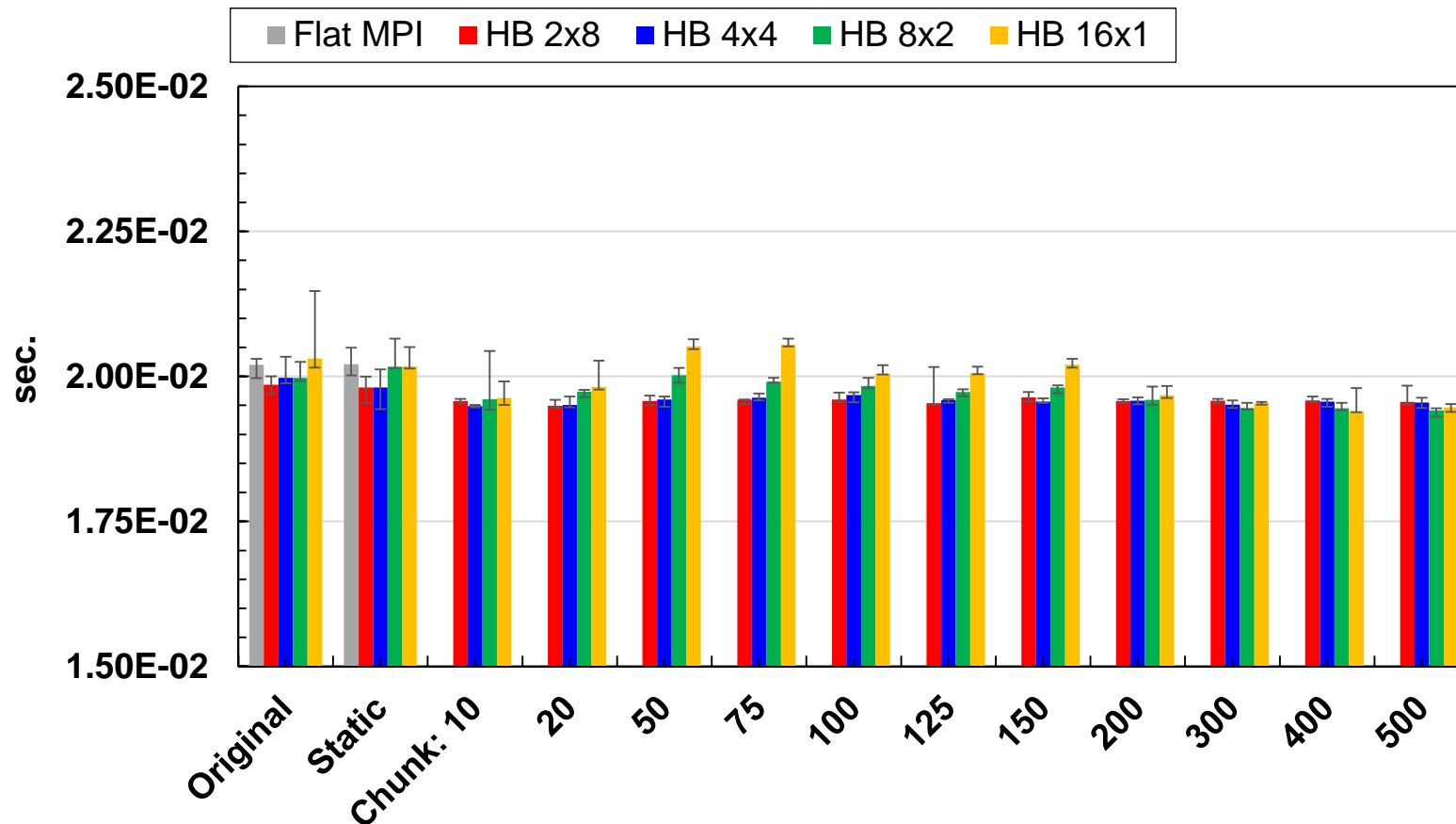


# Preliminary Results: BDW

120 nodes, 3,840 cores, 368,640,000 DOF  
(=640×480×400×3),

Computation of Time of CG/Iteration

Error-bar shows max/min values of 5 measurements

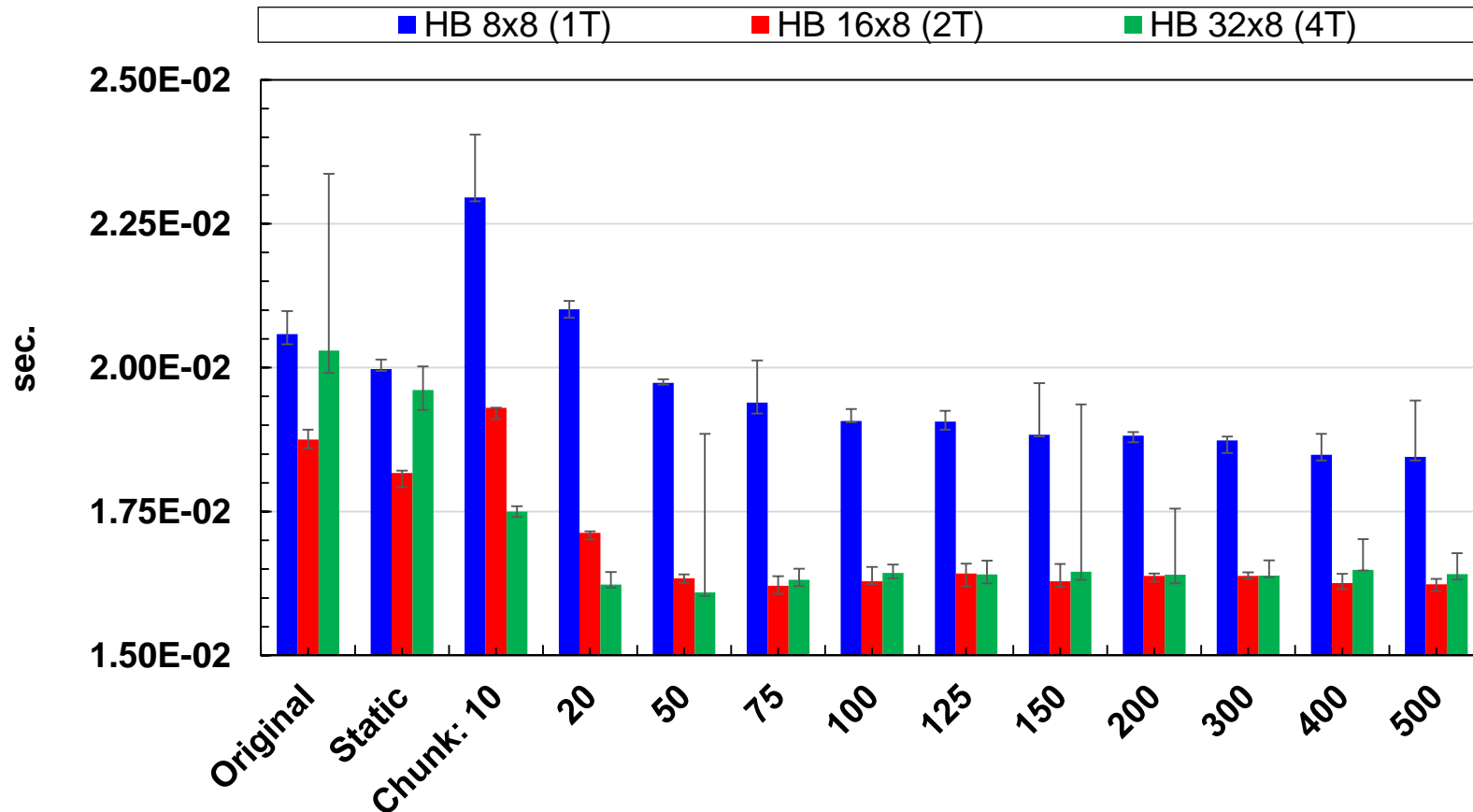


# Preliminary Results: KNL

60 nodes, 3,840 cores, 368,640,000 DOF

Computation of Time of CG/Iteration

Error-bar shows max/min values of 5 measurements  
8 cores/MPI proc, Effects of Thread/Core (1T, 2T, 4T)

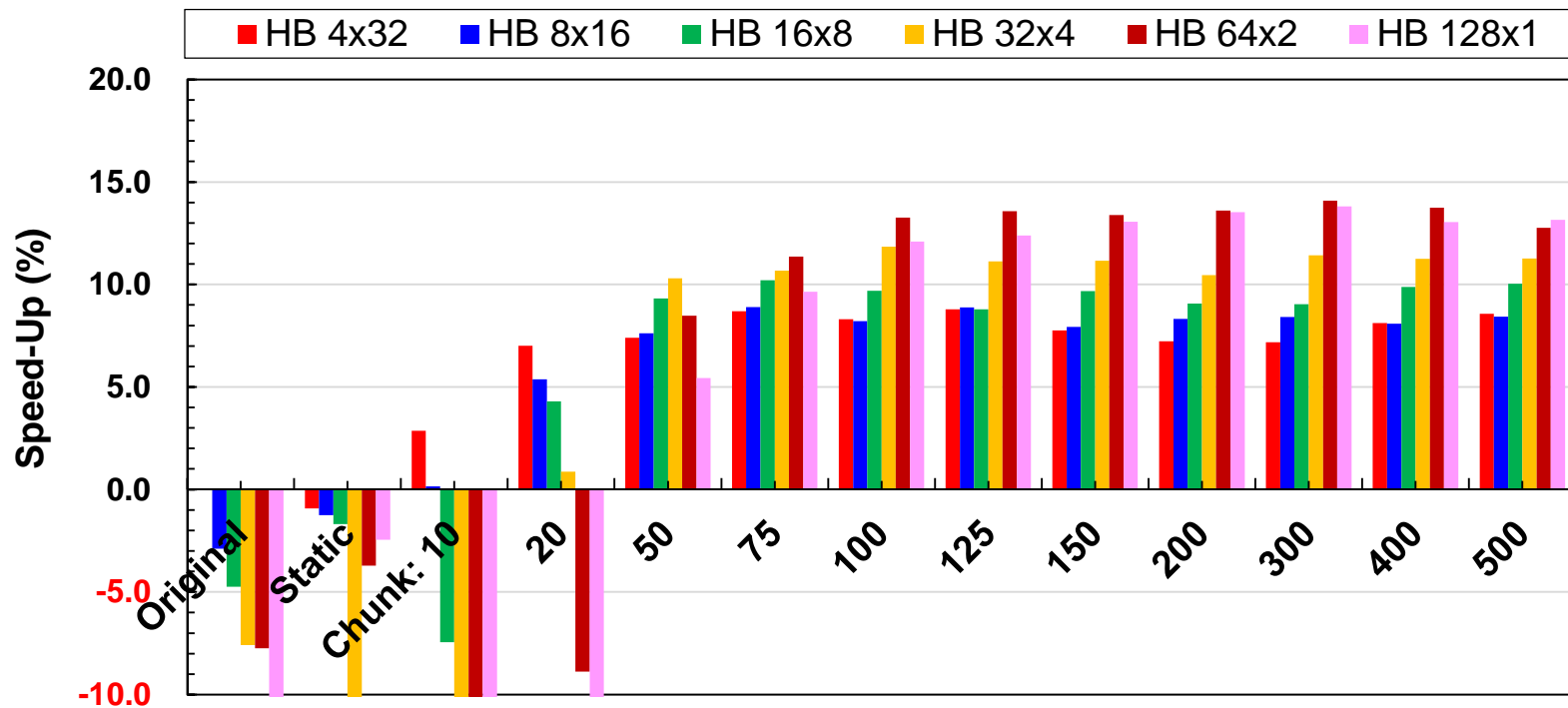




# Preliminary Results: KNL/2T

60 nodes, 3,840 cores, 368,640,000 DOF

Improvement of CG from Original HB 2x64

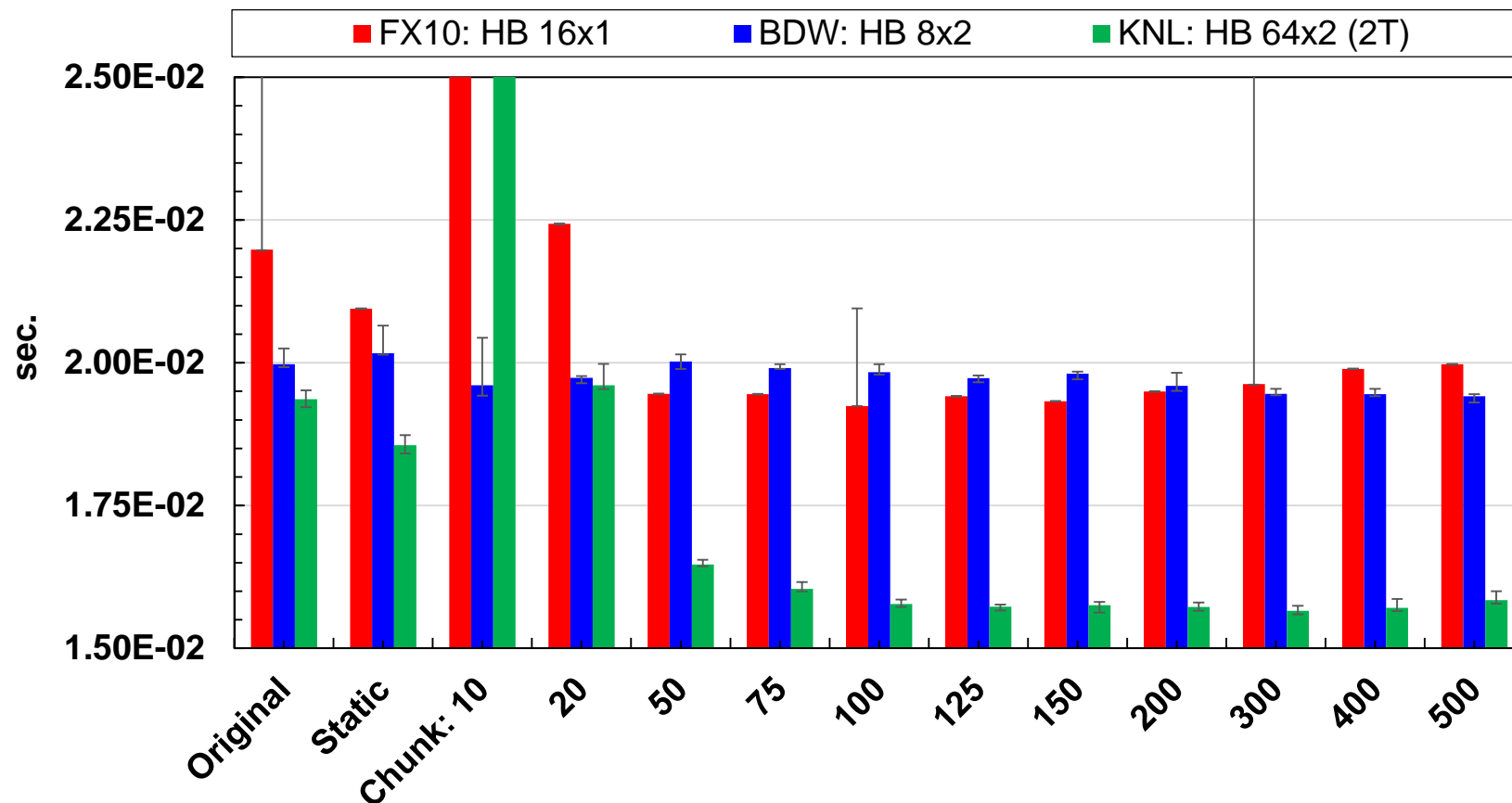


# Preliminary Results: Best Cases

3,840 cores, 368,640,000 DOF

Computation of Time of CG/Iteration

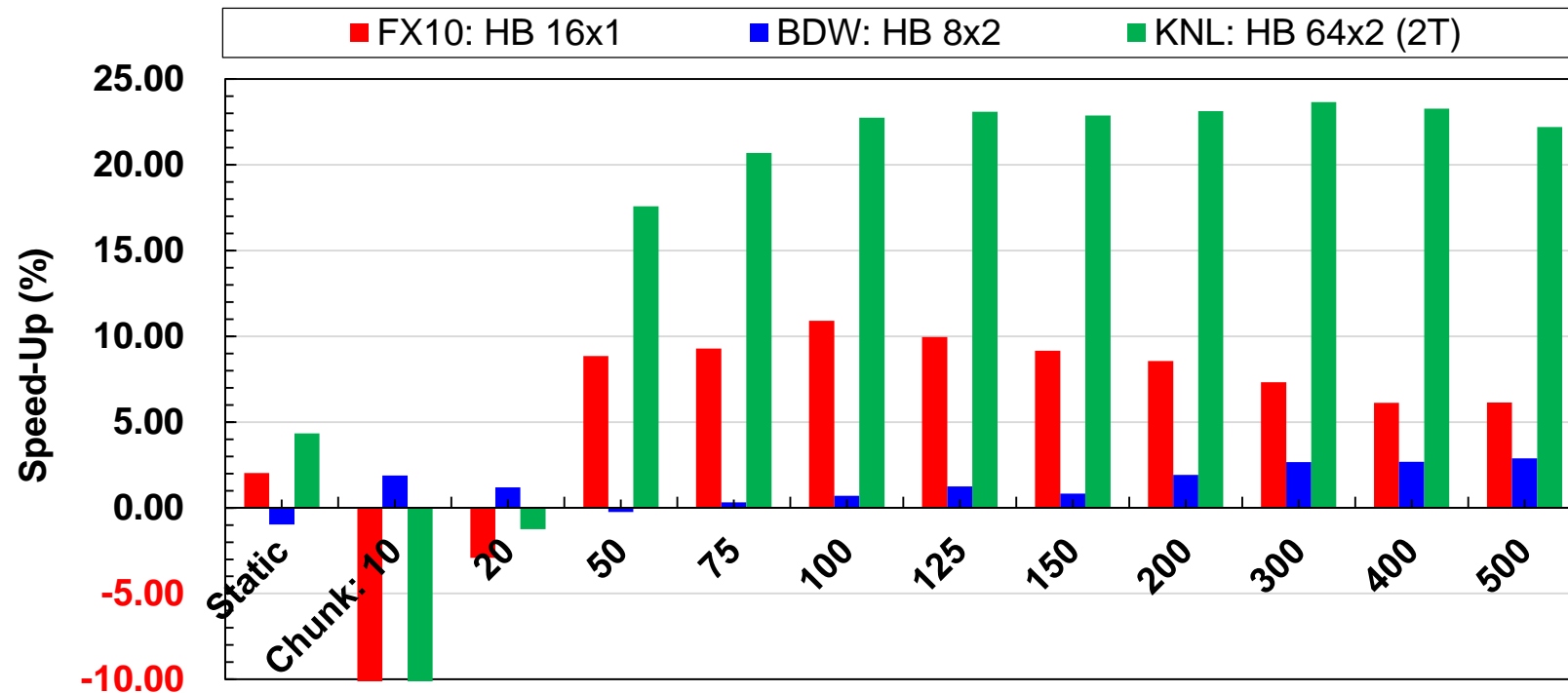
Error-bar shows max/min values of 5 measurements



# Preliminary Results: Best Cases

3,840 cores, 368,640,000 DOF

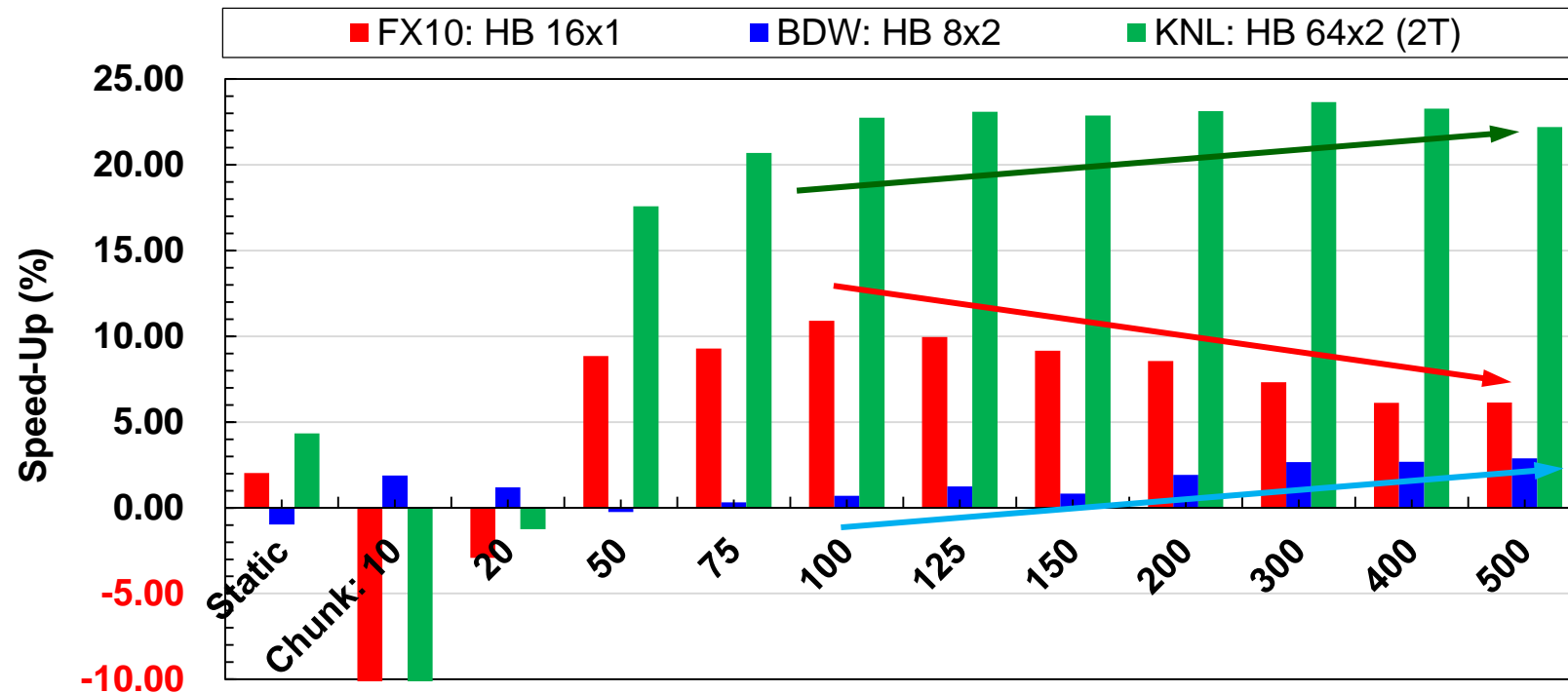
Improvement of CG from Original Cases



# Preliminary Results: Best Cases

3,840 cores, 368,640,000 DOF

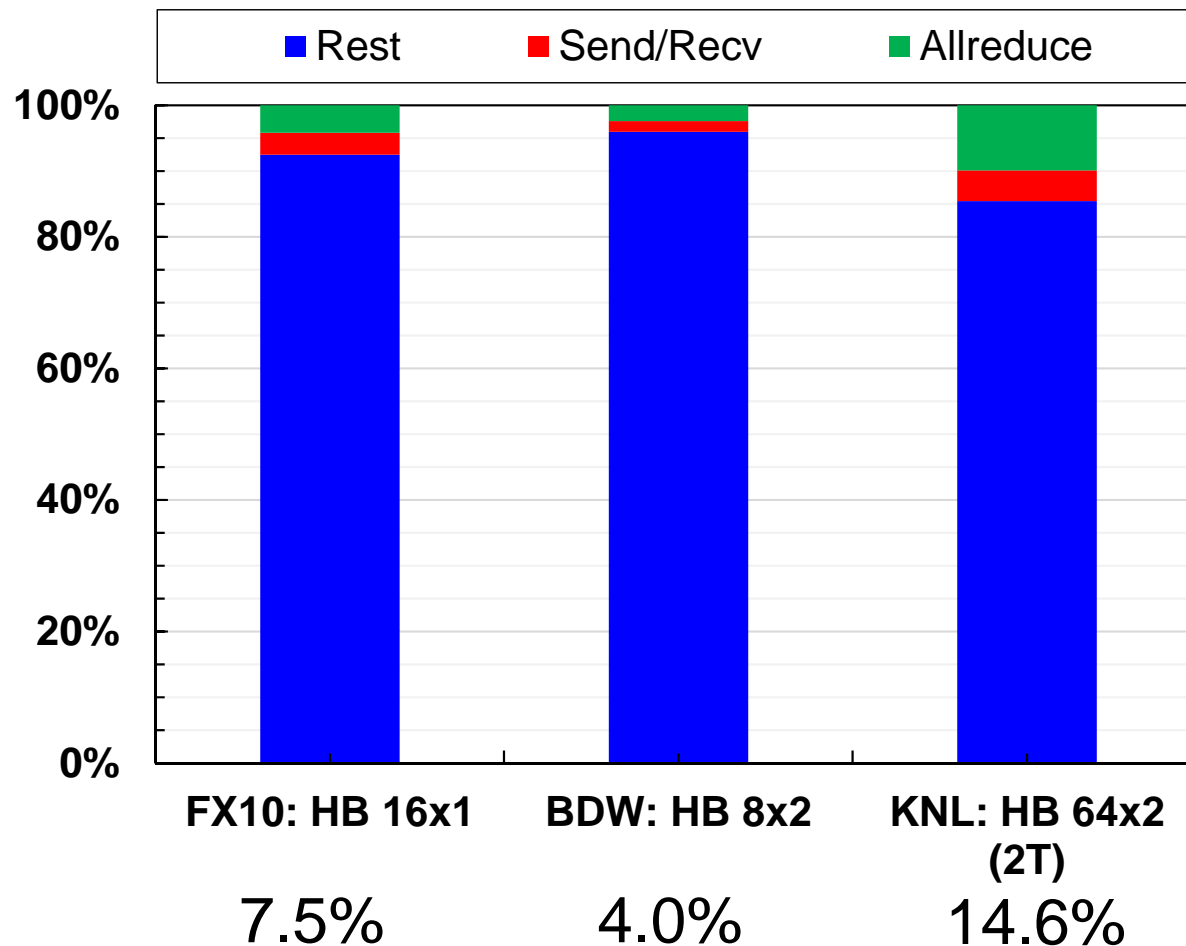
Improvement of CG from Original Cases



# Preliminary Results: Original Cases

3,840 cores, 368,640,000 DOF

Communication Overhead by Collective/Point-to-Point Communications



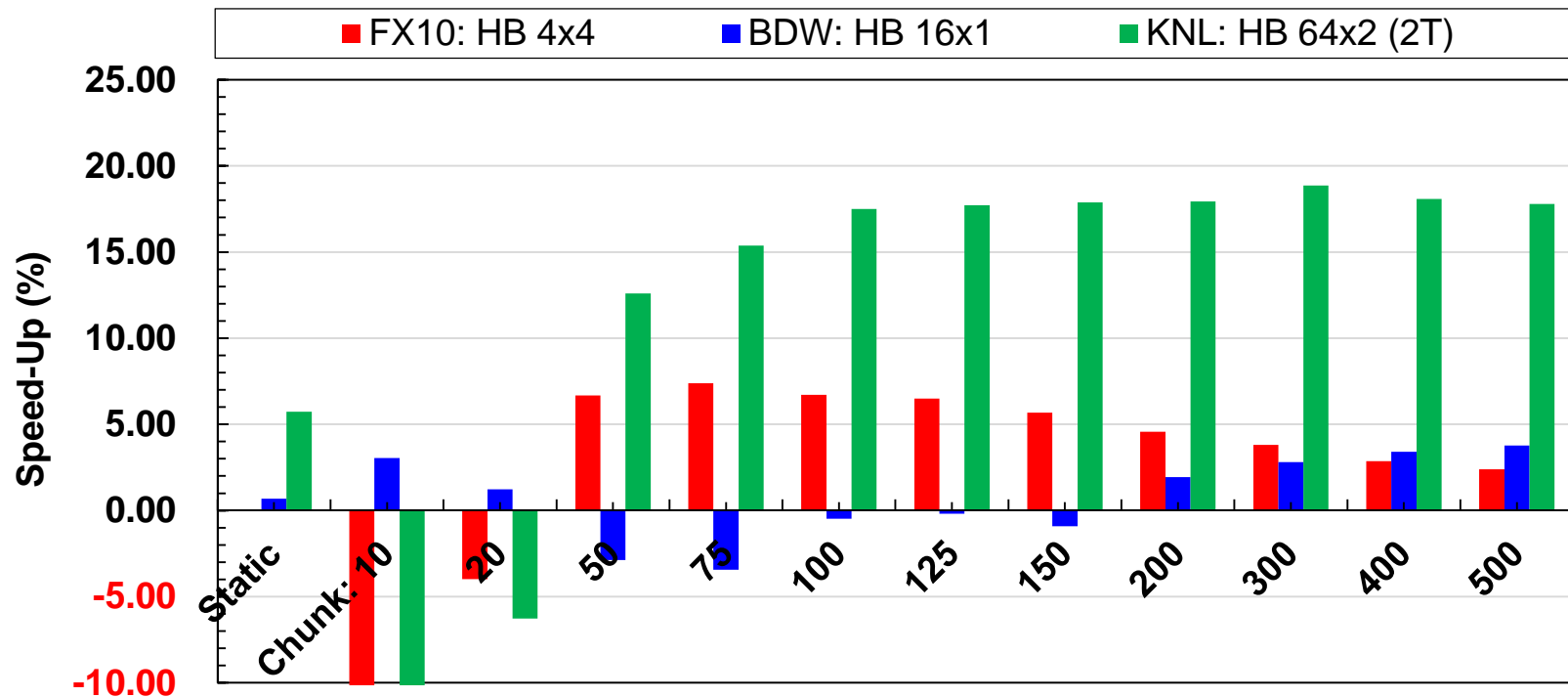
# Features

	Effect of Dynamic Scheduling	Optimum Chunk Size	Notes
FX10	Medium	100	Memory Throughput
BDW	Small	500+	Low Comm. Overhead Small number of threads.
KNL	Large	300-500	Effects are significant for HB 64x2, 128x1, where loss of performance by communications on master thread is rather smaller.

# Preliminary Results: Best Cases

3,840 cores, 720,000,000 DOF

Improvement of CG from Original Cases  
Effects are Smaller (DOF/MPI Proc. is larger)

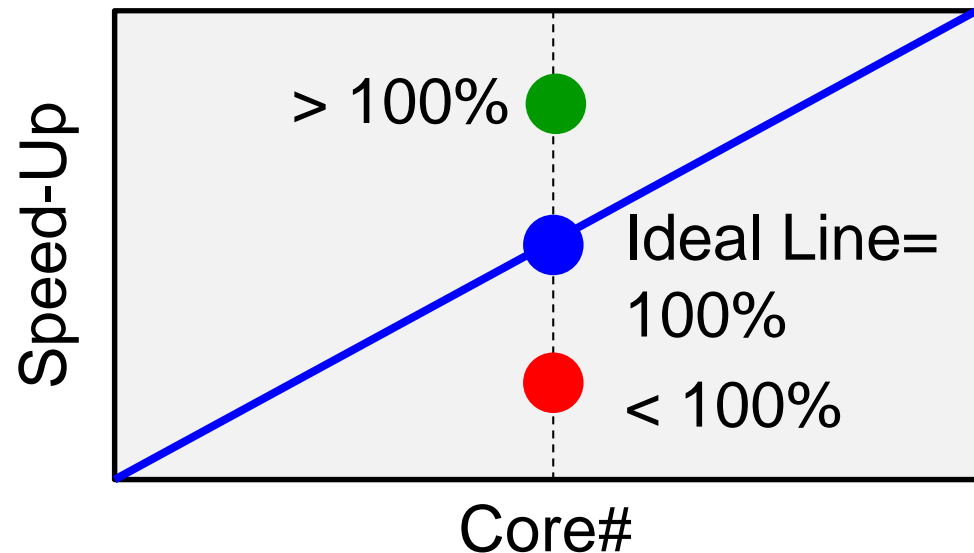


- Introduction
- Dynamic Loop Scheduling
- Hardware Environment
- Preliminary Results by Parallel FEM (GeoFEM/Cube)
- **Strong Scaling**
- SAI Preconditioning
- Summary



# Target Problem

- 256<sup>3</sup> FEM Nodes, 50,331,648 DOF
- Strong Scaling
  - FX10: 2-1,024 nodes (32-16,384 cores)
  - BDW: 2-512 sockets, 1-256 nodes (32-8,192 cores)
    - Reedbush-U has only 420 nodes of BDW
  - KNL: 4-256 nodes (256-16,384 cores)
- Parallel Performance
  - 100%: on the ideal line
  - < 100%: BELOW
  - > 100%: ABOVE



# Strong Scaling: KNL

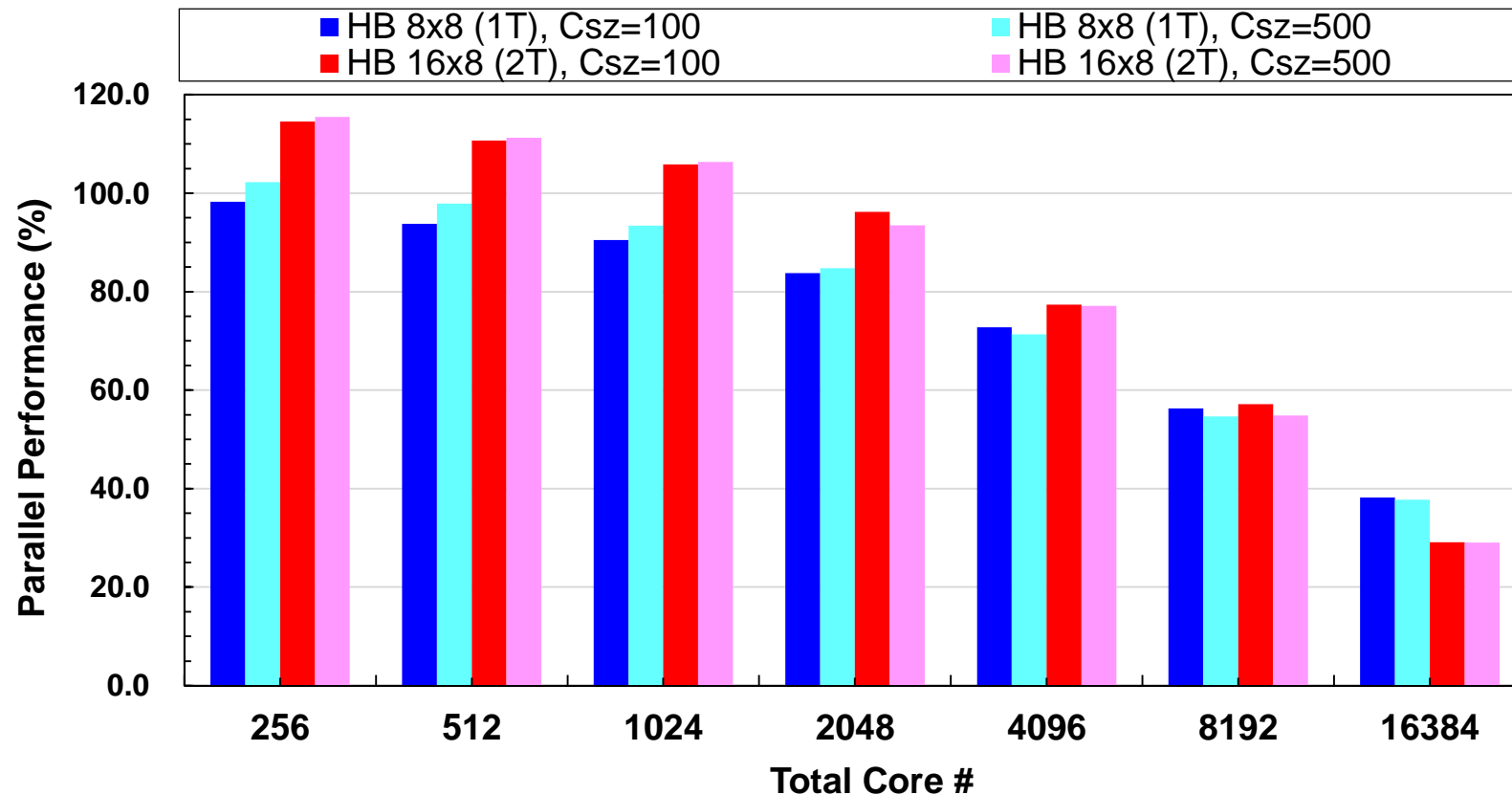
## Parallel Performance (%)

50,331,648 DOF, 256-16,384 cores

Computation Time of Flat MPI at 256 cores: 100%

HB 8x8 (1T) and HB 16x8 (2T)

1T is better, if Core# increases



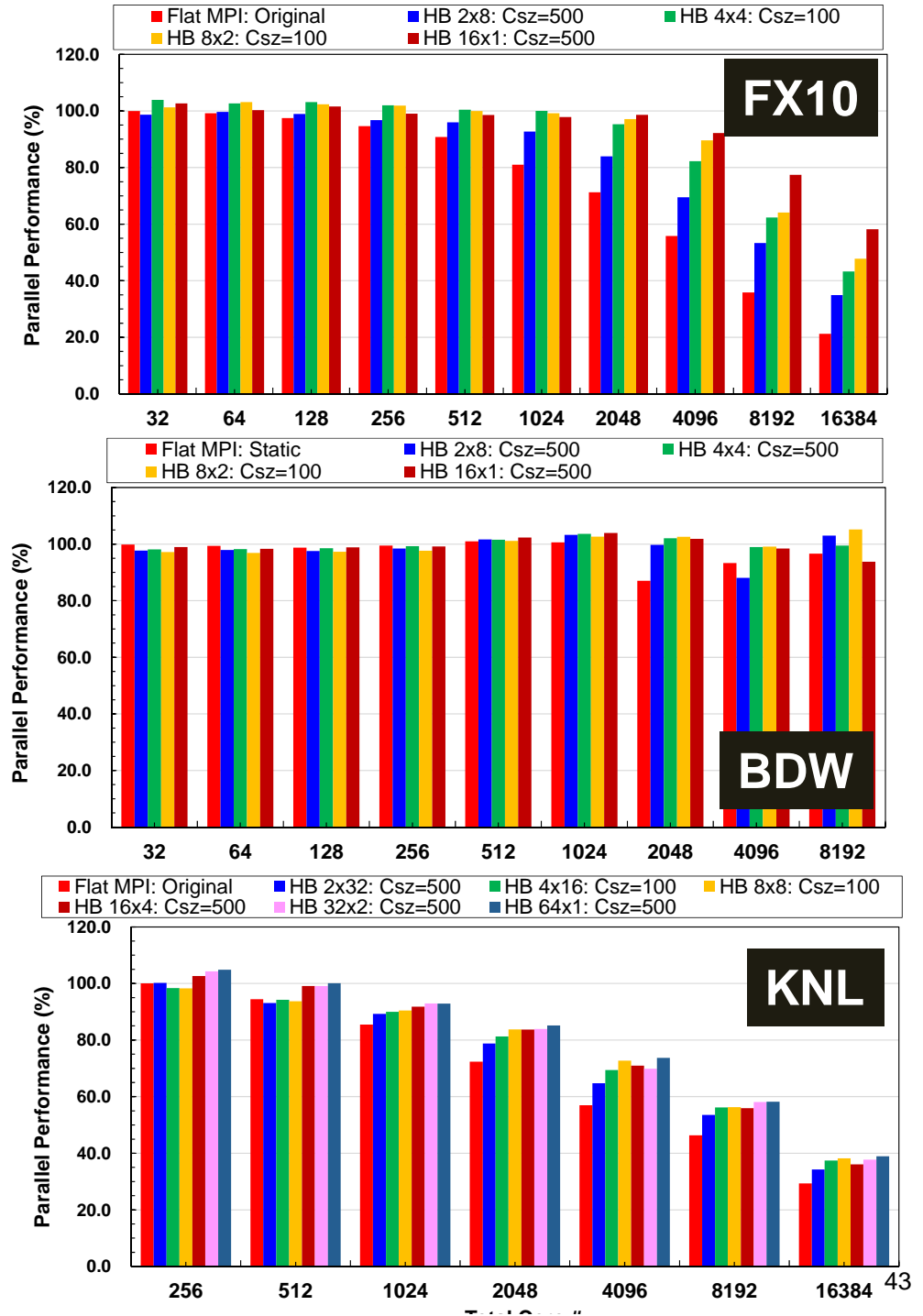
# Strong Scaling Parallel Performance (%)

# BEST case for each HB MxN

# 50,331,648 DOF

# Computation Time of Flat MPI at Min.# cores: 100%

**This difference between BDW and KNL might be because difference of performance between Infiniband EDR and Omni-Path Architecture.**



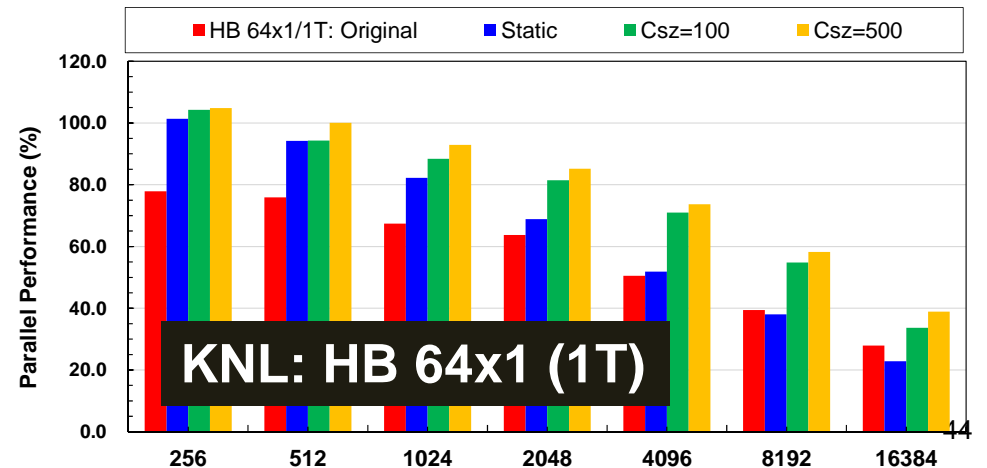
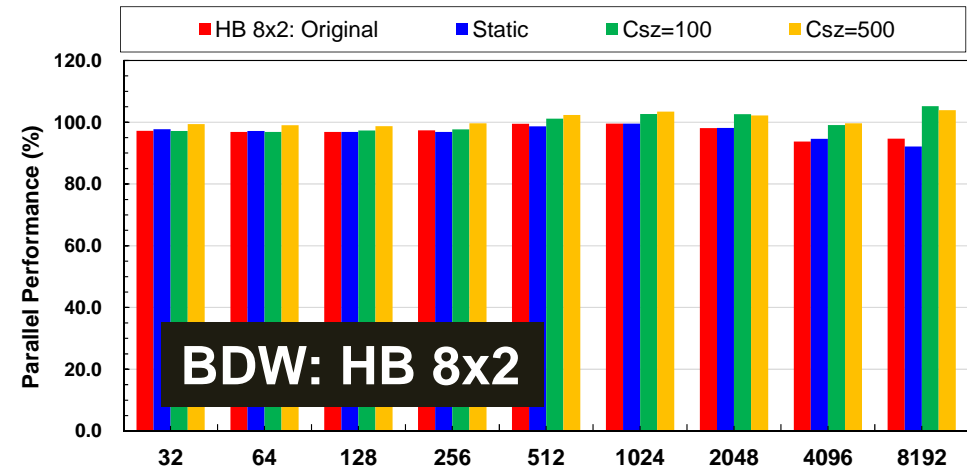
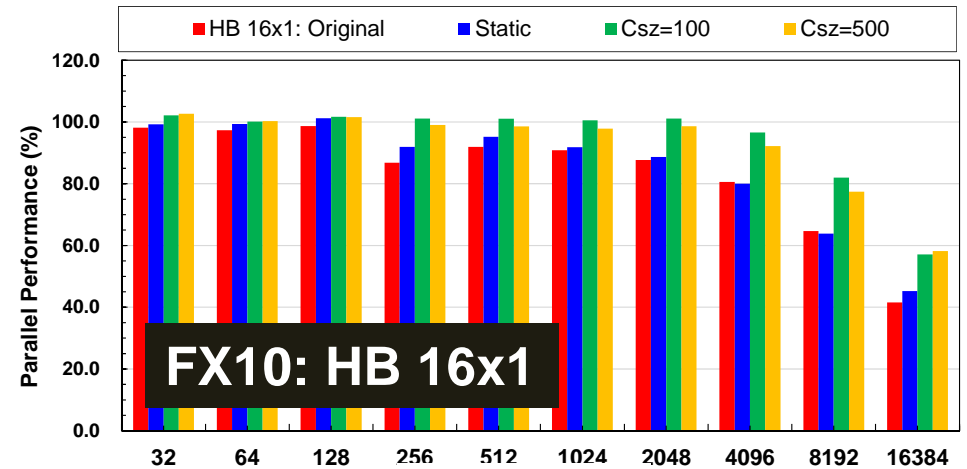
# Strong Scaling Parallel Performance (%)

## Effect of Dynamic Loop Scheduling

50,331,648 DOF  
Computation Time of Flat  
MPI at Min.# cores:  
100%

Effect of Dynamic Loop Scheduling  
with more than 8,192 cores

- FX10: 20%-40%
- BDW: 6%-10%
- KNL with HB 8×8 (1T): 20%-30%
- KNL with HB 64×1 (1T): 40%-50%



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# Next Target

- SAI (Sparse Approximate Inverse)
  - Mat-Vec. Multiplication for Sparse Approximate Inverse Matrix
  - Much Easier than ILU (failed)
  - Old, but not so bad. Suitable for GPU.
  - SAI: Various Approaches: SPAI (Explicit SAI) adopted

# SAI (Sparse Approx. Inverse)

- Preconditioning method for sparse matrices derived from localized-type scientific applications, such as FEM, FDM, FVM etc.
- **Define inverse (preconditioned) matrix  $[M]$  explicitly.**
- Even if original matrix  $[A]$  is sparse, inverse is usually dense due to *fill-in*.
- **Sparse approximate inverse (SAI)** is an *approximate* inverse matrix, which has as similar sparsity as the original matrix has.

$$sparsity(M) \approx sparsity(A)$$

# GeoFEM-SAI/Cube

- Parallel FEM Code (& Benchmarks)
- 3D-Static-Elastic-Linear (Solid Mechanics)
- Performance of Parallel Preconditioned Iterative Solvers

- 3D Tri-linear Hex. Elements

- **SAI + BiCGSTAB**

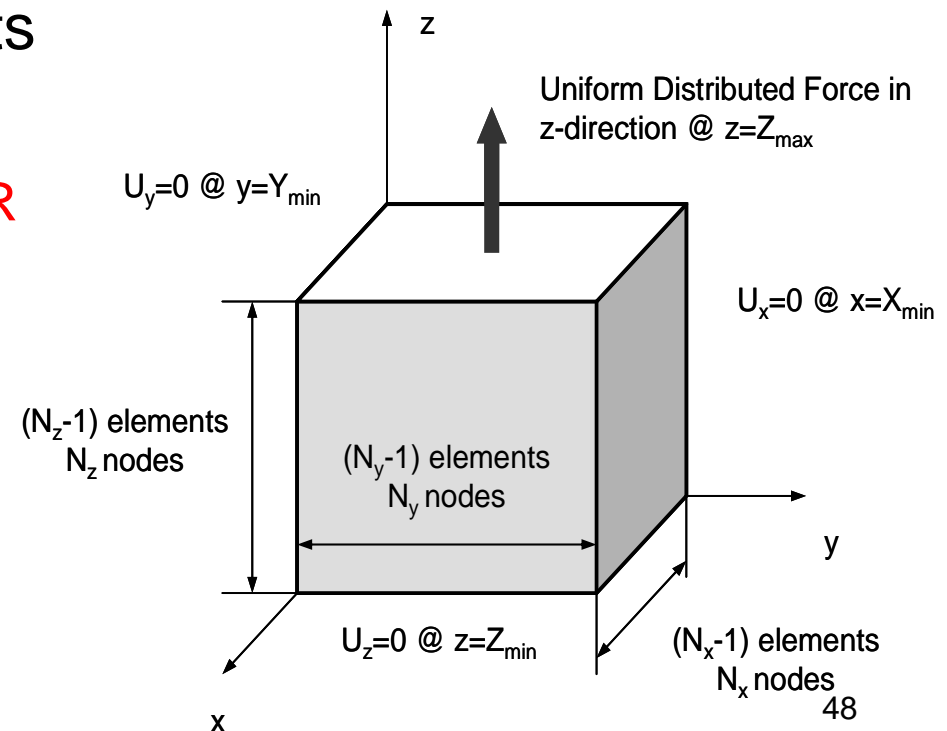
- Dropping Tolerance after QR Factorization:  $t$

- Fortran90+MPI+OpenMP

- Distributed Data Structure

- MPI, OpenMP,  
OpenMP/MPI Hybrid

- **Block CRS Format**





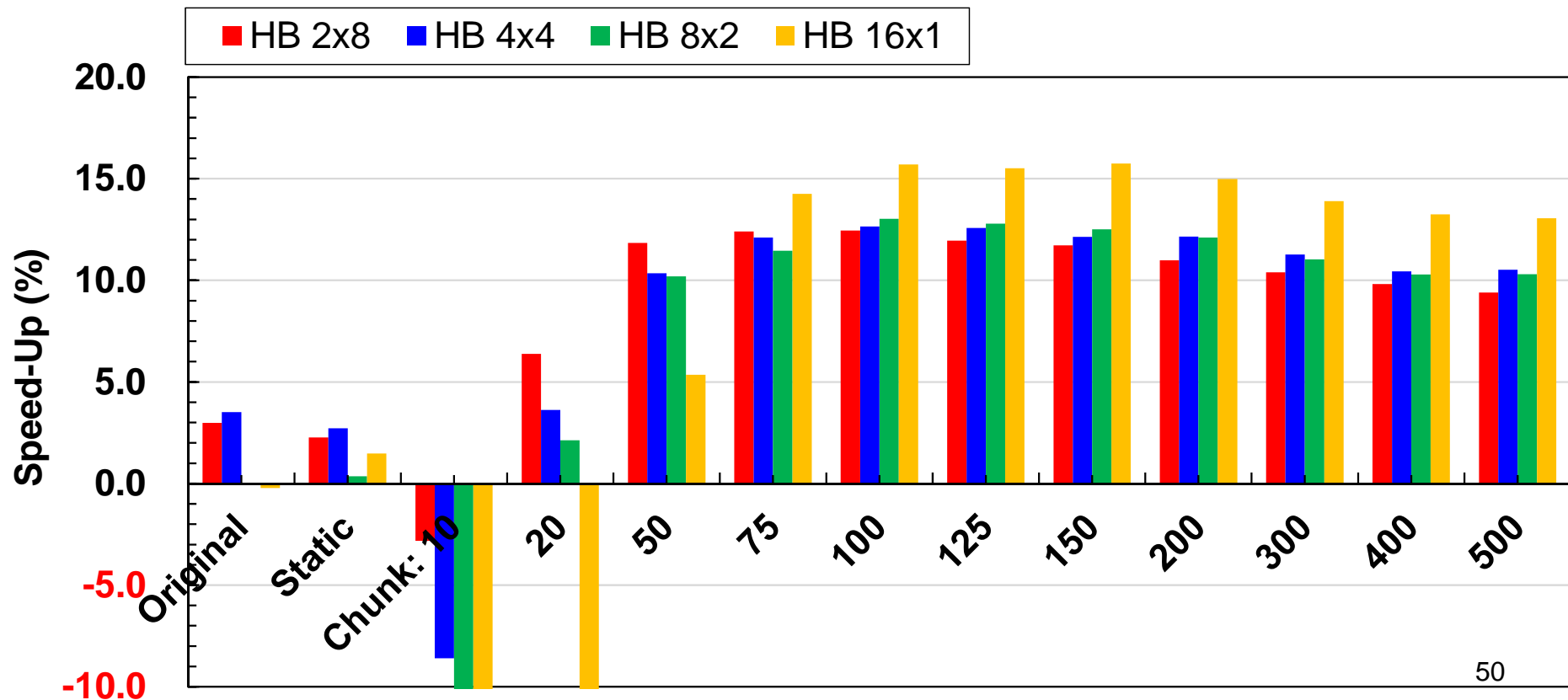
# Target Problem

- 393,216,000 FEM nodes ( $=960 \times 640 \times 640$ ),  
1,179,648,000 DOF
  - each node of FX10 has 512,000 nodes ( $=80 \times 80 \times 80$ ), and  
1,536,000 DOF
  - Dropping tolerance  $\epsilon$  is set to 0.10.
  - Number of non-zero components of  $M$  is 25.8% of that of  
original  $A$ .
- Using 12,288 cores
  - FX10: 768 nodes
  - BDW: 768 sockets, 384 nodes
  - KNL: 192 nodes, 2 threads per core (2T)

# FX10: 1,179,648,000 DOF

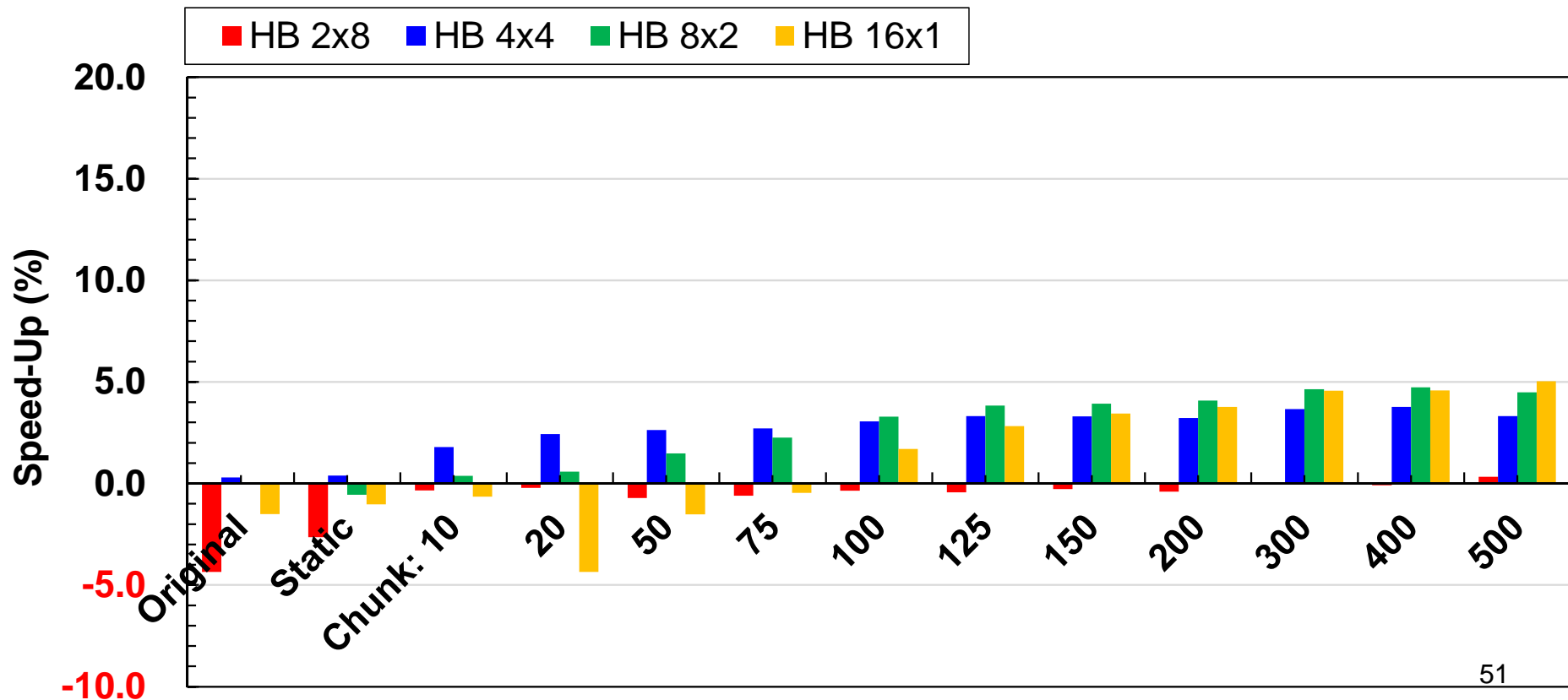
## 768 nodes, 12,288 cores

### Speed-Up compared to “Original” HB 8x2, t=0.10



# Reedbush-U (BDW): 1,179,648,000 DOF 384 nodes, 12,288 cores

Speed-Up compared to “Original” HB 8x2, t=0.10

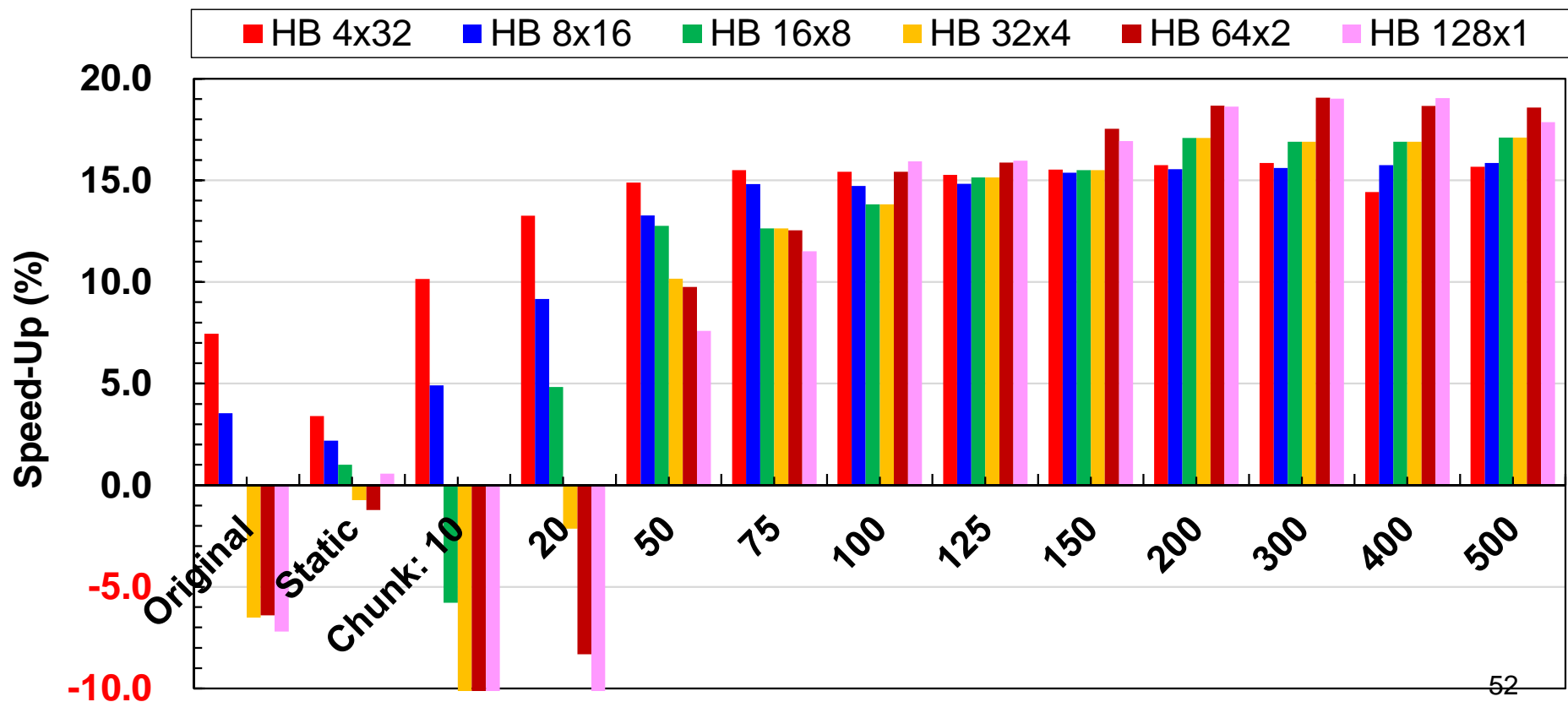


# Oakforest-PACS (KNL):

## 1,179,648,000 DOF

### 192 nodes, 12,288 cores, 2T/core

Speed-Up compared to “Original” HB 16x8, t=0.10



- Introduction
- Dynamic Loop Scheduling
- Hardware Environment
- Preliminary Results by Parallel FEM (GeoFEM/Cube)
- Strong Scaling
- SAI Preconditioning
- **Summary**

# Summary (1/2)

- CC-Overlapping by Dyn. Loop Scheduling of OpenMP
- SpMV of CG/BiCGSTAB in Parallel FEM (GeoFEM)
  - Significant Effects by Dynamic Loop Scheduling
  - Improvement of Performance by 40%-50% in strong scaling using up to 16,384 cores of FX10 and KNL Clusters.
  - On the contrast, improvement of performance is very small on Intel Broadwell (BDW) cluster.
  - Generally, effect of CC-Overlapping with dynamic loop scheduling is significant, if thread number for each MPI process is larger.
  - Therefore, developed method is expected to be useful for manycore architectures with  $O(10^2)$  cores, such as Intel Xeon Phi.

# Summary (2/2)

- SAI-BiCGSTAB
  - 15%-20% improvement of performance has been obtained on 12,288 cores of Fujitsu FX10 and KNL cluster.
- CC-Overlapping with dynamic loop scheduling improves the performance of parallel iterative solvers significantly, although algorithm is very simple.
- Future Work
  - More complicated preconditioning method, such as ILU, MG
  - Combination with Pipelined Method
  - Automatic selection of optimum Chunk Size
  - Further Optimization: Strong Scaling on KNL Cluster
  - The developed method might not work on NUMA
    - Appropriate runtime software will be needed.