Introduction to Programming by MPI for Parallel FEM Report S1 & S2 in Fortran

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Programming for Parallel Computing (616-2057)
Seminar on Advanced Computing (616-4009)

Motivation for Parallel Computing (and this class)

- Large-scale parallel computer enables fast computing in large-scale scientific simulations with detailed models. Computational science develops new frontiers of science and engineering.
- Why parallel computing ?
  - faster & larger
  - “larger” is more important from the view point of “new frontiers of science & engineering”, but “faster” is also important.
  - + more complicated
  - Ideal: Scalable
    - Solving N^x scale problem using N^x computational resources during same computation time.

Overview

- What is MPI ?
- Your First MPI Program: Hello World
- Global/Local Data
- Collective Communication
- Peer-to-Peer Communication

What is MPI ? (1/2)

- Message Passing Interface
- “Specification” of message passing API for distributed memory environment
  - Not a program, Not a library
    - http://www.mcs.anl.gov/mpi/www/
- History
  - 1992 MPI Forum
  - 1994 MPI-1
  - 1997 MPI-2: MPI I/O
  - 2012 MPI-3: Fault Resilience, Asynchronous Collective
- Implementation
  - mpich ANL (Argonne National Laboratory), OpenMPI, MVAPICH
  - H/W vendors
  - C/C++, FOTRAN, Java ; Unix, Linux, Windows, Mac OS

What is MPI ? (2/2)

- “mpich” (free) is widely used
  - supports MPI-2 spec. (partially)
  - MPICH2 after Nov. 2005.
  - http://www.mcs.anl.gov/mpi/
- Why MPI is widely used as *de facto standard* ?
  - Uniform interface through MPI forum
    - Portable, can work on any types of computers
    - Can be called from Fortran, C, etc.
  - mpich
    - free, supports every architecture
- PVM (Parallel Virtual Machine) was also proposed in early 90’s but not so widely used as MPI

References

- W.Gropp et al., Using MPI second edition, MIT Press, 1999.
- M.J.Quinn, Parallel Programming in C with MPI and OpenMP, McGrawhill, 2003.
- W.Gropp et al., MPI：The Complete Reference Vol.I, II, MIT Press, 1998.
- http://www.mcs.anl.gov/mpi/www/
  - API (Application Interface) of MPI

How to learn MPI (1/2)

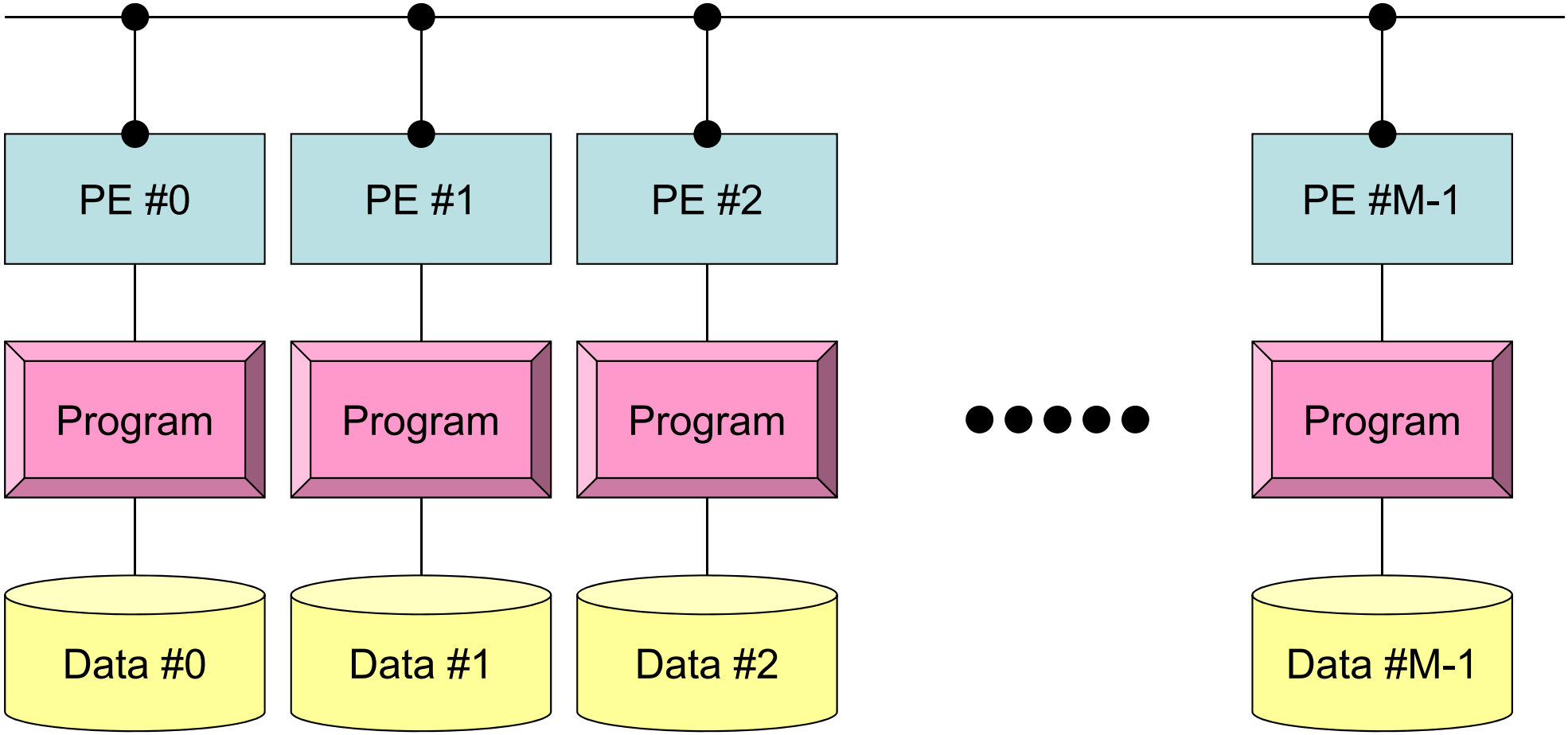
- Grammar
  - 10-20 functions of MPI-1 will be taught in the class
    - although there are many convenient capabilities in MPI-2
  - If you need further information, you can find information from web, books, and MPI experts.
- Practice is important
  - Programming
  - "Running the codes" is the most important
- Be familiar with or "grab" the idea of SPMD/SIMD op's
  - Single Program/Instruction Multiple Data
  - Each process does same operation for different data
    - Large-scale data is decomposed, and each part is computed by each process
  - Global/Local Data, Global/Local Numbering

PE: Processing Element
Processor, Domain, Process

SPMD

You understand 90% MPI, if you understand this figure.

```
mpirun -np M <Program>
```



Each process does same operation for different data

Large-scale data is decomposed, and each part is computed by each process

It is ideal that parallel program is not different from serial one except communication.

Some Technical Terms

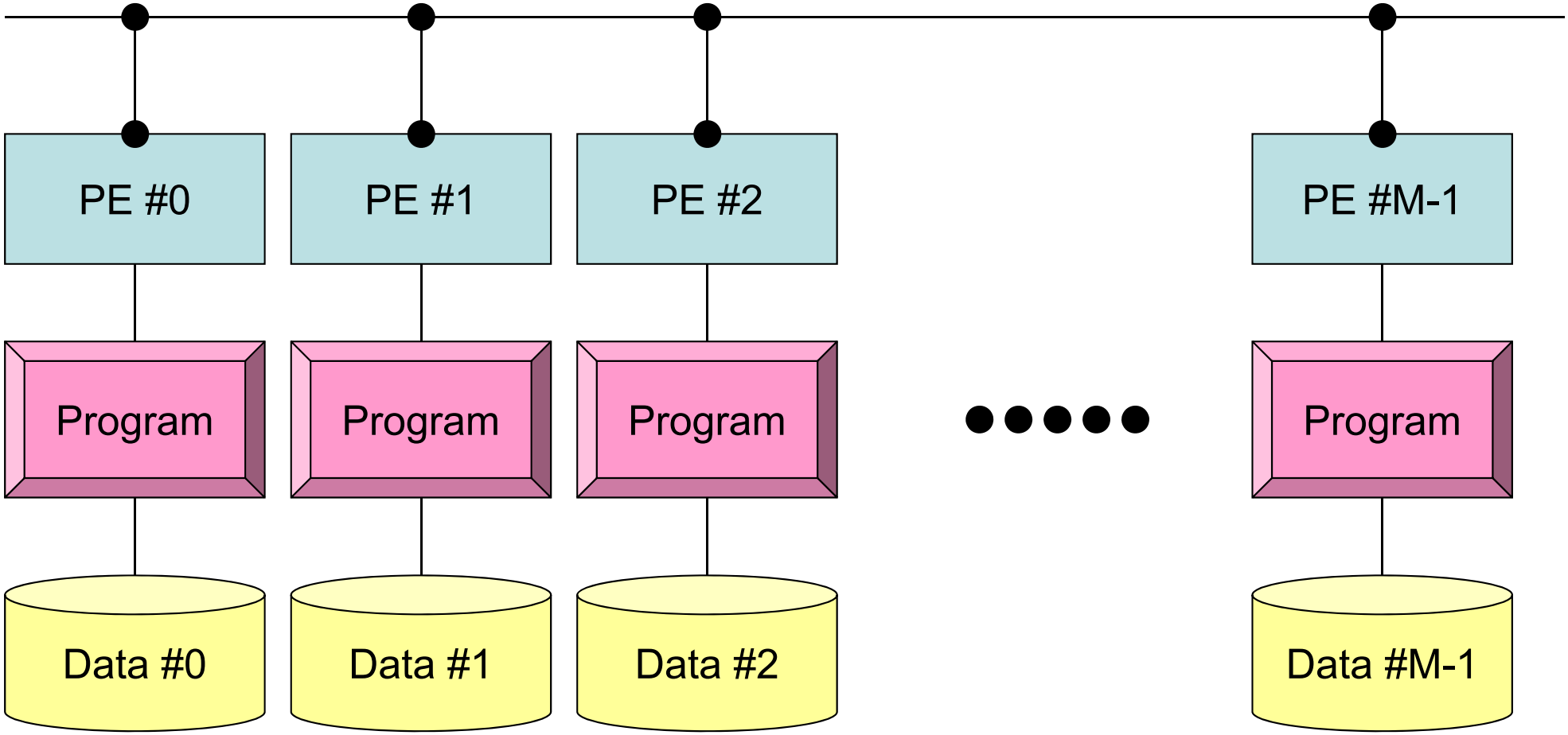
- Processor, Core
  - Processing Unit (H/W), Processor=Core for single-core proc's
- Process
  - Unit for MPI computation, nearly equal to "core"
  - Each core (or processor) can host multiple processes (but not efficient)
- PE (Processing Element)
  - PE originally mean "processor", but it is sometimes used as "process" in this class. Moreover it means "domain" (next)
    - In multicore proc's: PE generally means "core"
- Domain
  - domain=process (=PE), each of "MD" in "SPMD", each data set
- Process ID of MPI (ID of PE, ID of domain) starts from "0"
  - if you have 8 processes (PE's, domains), ID is 0~7

PE: Processing Element
Processor, Domain, Process

SPMD

You understand 90% MPI, if you understand this figure.

```
mpirun -np M <Program>
```



Each process does same operation for different data

Large-scale data is decomposed, and each part is computed by each process

It is ideal that parallel program is not different from serial one except communication.

How to learn MPI (2/2)

- NOT so difficult.
- Therefore, 2-3 lectures are enough for just learning grammar of MPI.

- Grab the idea of SPMD !

Schedule

- MPI
  - Basic Functions
  - Collective Communication
  - Point-to-Point (or Peer-to-Peer) Communication

- 90 min. x 4-5 lectures
  - Collective Communication
    - Report S1
  - Point-to-Point/Peer-to-Peer Communication
    - Report S2: Parallelization of 1D code
  - At this point, you are almost an expert of MPI programming.

- What is MPI ?
- **Your First MPI Program: Hello World**
- Global/Local Data
- Collective Communication
- Peer-to-Peer Communication

Login to Oakleaf-FX

```
ssh t91**@oakleaf-fx.cc.u-tokyo.ac.jp
```

Create directory

```
>$ cd
>$ mkdir 2015summer  (your favorite name)
>$ cd 2015summer
```

In this class this top-directory is called **<$O-TOP>**.
Files are copied to this directory.

Under this directory, **S1, S2, S1-ref** are created:

```
<$O-S1> = <$O-TOP>/mpi/S1
<$O-S2> = <$O-TOP>/mpi/S2
```

Oakleaf-FX

ECCS2012

Copying files on Oakleaf-FX

Fortan

```
>$ cd <$O-TOP>
>$ cp /home/z30088/class_eps/F/s1-f.tar .
>$ tar xvf s1-f.tar
```

C

```
>$ cd <$O-TOP>
>$ cp /home/z30088/class_eps/C/s1-c.tar .
>$ tar xvf s1-c.tar
```

Confirmation

```
>$ ls
   mpi

>$ cd mpi/S1
```

This directory is called as <$O-S1>.

<$O-S1> = <$O-TOP>/mpi/S1

First Example

hello.f

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h‘
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

hello.c

```
#include "mpi.h"
#include <stdio.h>
int main(int argc, char **argv)
{
    int n, myid, numprocs, i;

    MPI_Init(&argc,&argv);
    MPI_Comm_size(MPI_COMM_WORLD,&numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD,&myid);
    printf ("Hello World %d¥n", myid);
    MPI_Finalize();
}
```

Compiling hello.f/c

```
>$ cd <$O-S1>
>$ mpifrtpx –Kfast hello.f
>$ mpifccpx –Kfast hello.c
```

FORTRAN

```
$> mpifrtpx –Kfast hello.f
```

“mpifrtpx”:
FORTRAN90＋MPIによってプログラムをコンパイルする際に
必要な，コンパイラ，ライブラリ等がバインドされている

C言語

```
$> mpifccpx –Kfast hello.c
```

“mpifccpx”:
C＋MPIによってプログラムをコンパイルする際に
必要な，コンパイラ，ライブラリ等がバインドされている

Running Job

- Batch Jobs
  - Only batch jobs are allowed.
  - Interactive executions of jobs are not allowed.
- How to run
  - writing job script
  - submitting job
  - checking job status
  - checking results
- Utilization of computational resources
  - 1-node (16 cores) is occupied by each job.
  - Your node is not shared by other jobs.

Job Script

- **<$O-S1>/hello.sh**
- Scheduling + Shell Script

```
#!/bin/sh
#PJM -L “node=1“                    Number of Nodes
#PJM -L “elapse=00:10:00“           Computation Time
#PJM -L “rscgrp=lecture1“           Name of “QUEUE”
#PJM -g “gt91“                      Group Name (Wallet)
#PJM -j
#PJM -o “hello.lst“                 Standard Output
#PJM --mpi “proc=4“                 MPI Process #

mpiexec ./a.out                     Execs
```

8プロセス	16プロセス	32プロセス	64プロセス	192プロセス
“node=1“ “proc=8”	“node=1“ “proc=16”	“node=2“ “proc=32”	“node=4“ “proc=64”	“node=12“ “proc=192”

Submitting Jobs

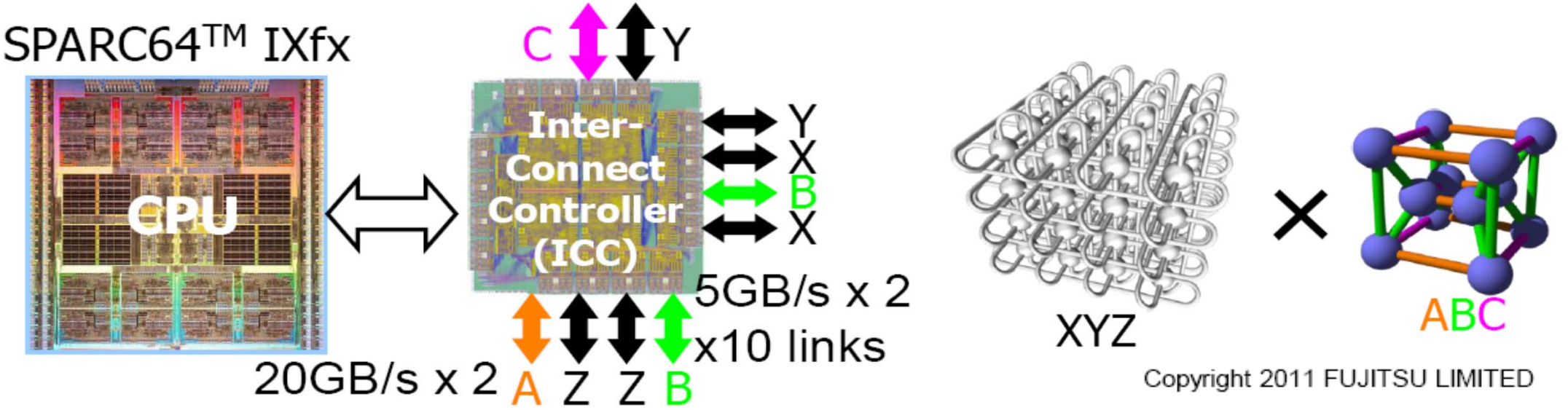
```
>$ cd <$O-S1>
>$ pjsub hello.sh

>$ cat hello.lst

  Hello World 0
  Hello World 3
  Hello World 2
  Hello World 1
```

Available QUEUE's

- Following 2 queues are available.
- 1 Tofu (12 nodes) can be used
  - **`lecture`**
    - 12 nodes (192 cores), 15 min., valid until the end of December, 2015
    - Shared by all "educational" users
  - **`lecture1`**
    - 12 nodes (192 cores), 15 min., active during class time
    - More jobs (compared to **`lecture`**) can be processed up on availability.

Tofu Interconnect

- Node Group
  - 12 nodes
  - A-/C- axis: 4 nodes in system board, B-axis: 3 boards
- 6D: (X,Y,Z,A,B,C)
  - ABC 3D Mesh: in each node group: 2 × 2 × 3
  - XYZ 3D Mesh: connection of node groups: 10 × 5 × 8
- Job submission according to network topology is possible:
  - Information about used “XYZ” is available after execution.



Submitting & Checking Jobs

• Submitting Jobs	`pjsub SCRIPT NAME`
• Checking status of jobs	`pjstat`
• Deleting/aborting	`pjdel JOB ID`
• Checking status of queues	`pjstat --rsc`
• Detailed info. of queues	`pjstat --rsc –x`
• Number of running jobs	`pjstat --rsc –b`
• Limitation of submission	`pjstat --limit`

```
[z30088@oakleaf-fx-6 S2-ref]$ pjstat

Oakleaf-FX scheduled stop time: 2012/09/28(Fri) 09:00:00 (Remain: 31days 20:01:46)

JOB_ID     JOB_NAME   STATUS  PROJECT  RSCGROUP  START_DATE        ELAPSE          TOKEN NODE:COORD
334730     go.sh      RUNNING gt61     lecture   08/27 12:58:08    00:00:05          0.0 1
```

Basic/Essential Functions

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

```
#include "mpi.h"
#include <stdio.h>
int main(int argc, char **argv)
{
    int n, myid, numprocs, i;

    MPI_Init(&argc,&argv);
    MPI_Comm_size(MPI_COMM_WORLD,&numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD,&myid);

    printf ("Hello World %d¥n", myid);
    MPI_Finalize();
}
```

‘mpif.h’, “mpi.h”

Essential Include file

“use mpi” is possible in F90

MPI_Init

Initialization

MPI_Comm_size

Number of MPI Processes

mpirun -np XX <prog>

MPI_Comm_rank

Process ID starting from 0

MPI_Finalize

Termination of MPI processes

Difference between FORTRAN/C

- (Basically) same interface
  - In C, UPPER/lower cases are considered as different
    - e.g.: **MPI_C**omm_size
      - MPI: UPPER case
      - First character of the function except “MPI_” is in UPPER case.
      - Other characters are in lower case.
- In Fortran, return value `ierr` has to be added at the end of the argument list.
- C needs special types for variables:
  - MPI_Comm, MPI_Datatype, MPI_Op etc.
- **`MPI_INIT`** is different:
  - `call MPI_INIT (ierr)`
  - `MPI_Init (int *argc, char ***argv)`

What's are going on ?

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

```
#!/bin/sh
#PJM -L "node=1"              Number of Nodes
#PJM -L "elapse=00:10:00"     Computation Time
#PJM -L "rscgrp=lecture"      Name of "QUEUE"
#PJM -g "gt64"                Group Name (Wallet)
#PJM -j
#PJM -o "hello.lst"           Standard Output
#PJM --mpi "proc=4"           MPI Process #

mpiexec ./a.out               Execs
```

- **`mpiexec`** starts up 4 MPI processes ("proc=4")
  - A single program runs on four processes.
  - each process writes a value of `myid`
- Four processes do same operations, but values of **`myid`** are different.
- Output of each process is different.
- That is SPMD !

mpi.h, mpif.h

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

```
#include "mpi.h"
#include <stdio.h>
int main(int argc, char **argv)
{
    int n, myid, numprocs, i;

    MPI_Init(&argc,&argv);
    MPI_Comm_size(MPI_COMM_WORLD,&numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD,&myid);

    printf ("Hello World %d¥n", myid);
    MPI_Finalize();
}
```

- Various types of parameters and variables for MPI & their initial values.
- Name of each var. starts from “MPI_”
- Values of these parameters and variables cannot be changed by users.
- Users do not specify variables starting from “MPI_” in users’ programs.

Fortran

MPI_INIT

- Initialize the MPI execution environment (required)
- It is recommended to put this BEFORE all statements in the program.

- **call MPI_INIT (ierr)**
  - **ierr** I O Completion Code

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

Fortran

MPI_FINALIZE

- Terminates MPI execution environment (required)
- It is recommended to put this AFTER all statements in the program.
- Please do not forget this.

- **call MPI_FINALIZE (ierr)**
  - **ierr** I O completion code

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

Fortran

MPI_COMM_SIZE

- Determines the size of the group associated with a communicator
- not required, but very convenient function

- **call MPI_COMM_SIZE (comm, size, ierr)**
  - **comm** I I communicator
  - **size** I O number of processes in the group of communicator
  - **ierr** I O completion code

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

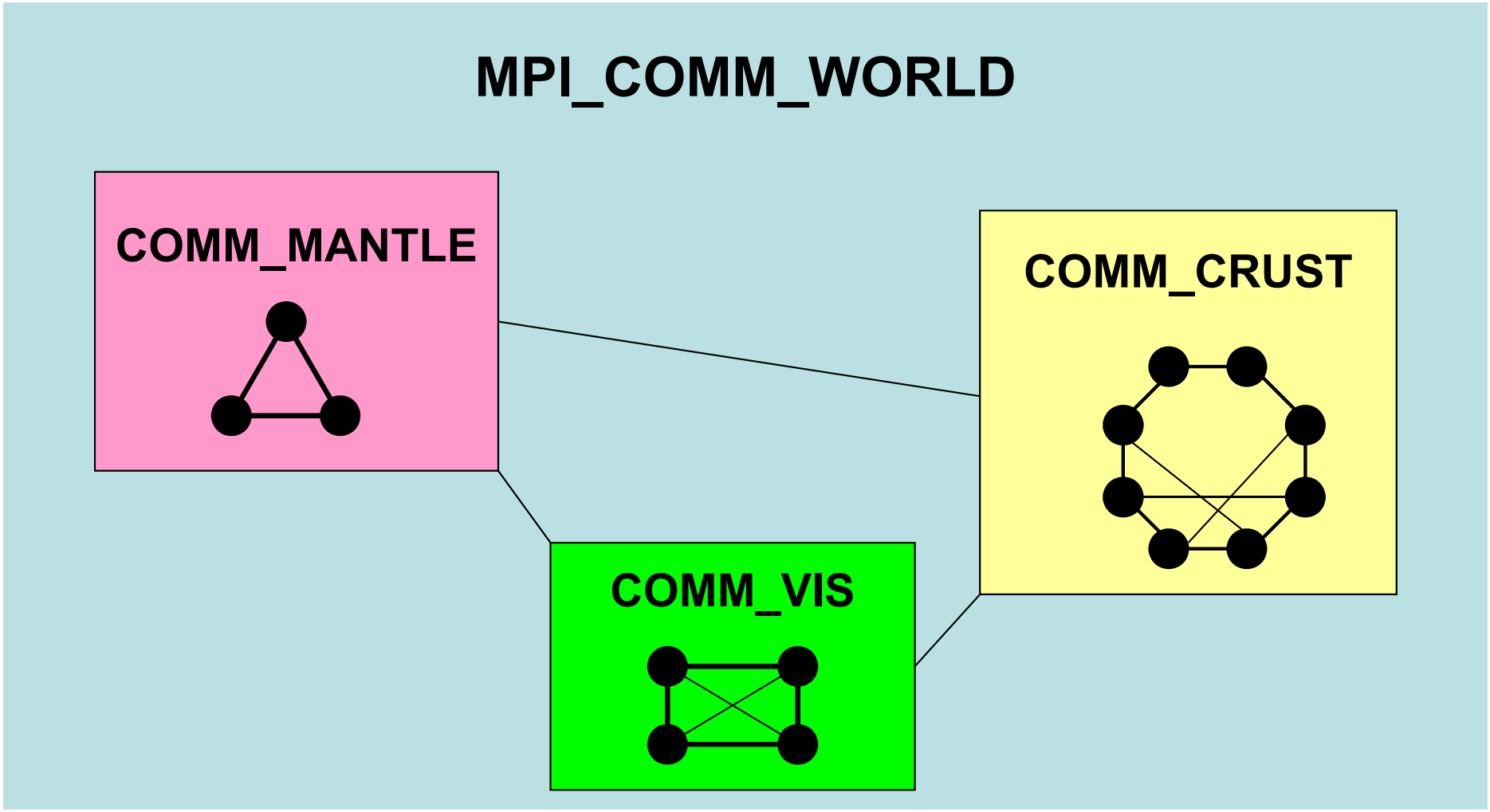
What is Communicator ?

```
MPI_Comm_Size (MPI_COMM_WORLD, PETOT)
```

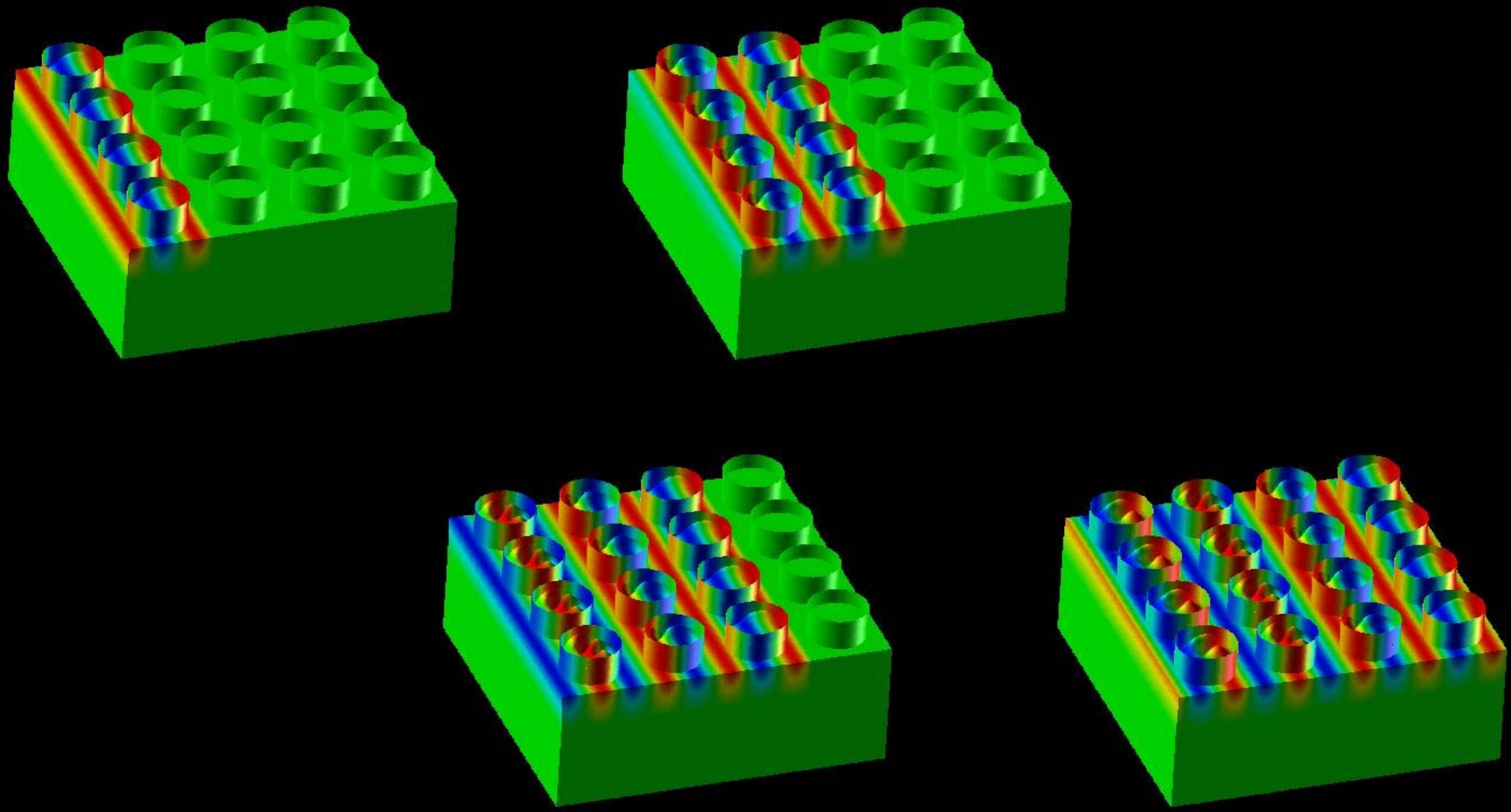
- Group of processes for communication
- Communicator must be specified in MPI program as a unit of communication
- All processes belong to a group, named "**MPI_COMM_WORLD**" (default)
- Multiple communicators can be created, and complicated operations are possible.
  - Computation, Visualization
- Only "MPI_COMM_WORLD" is needed in this class.

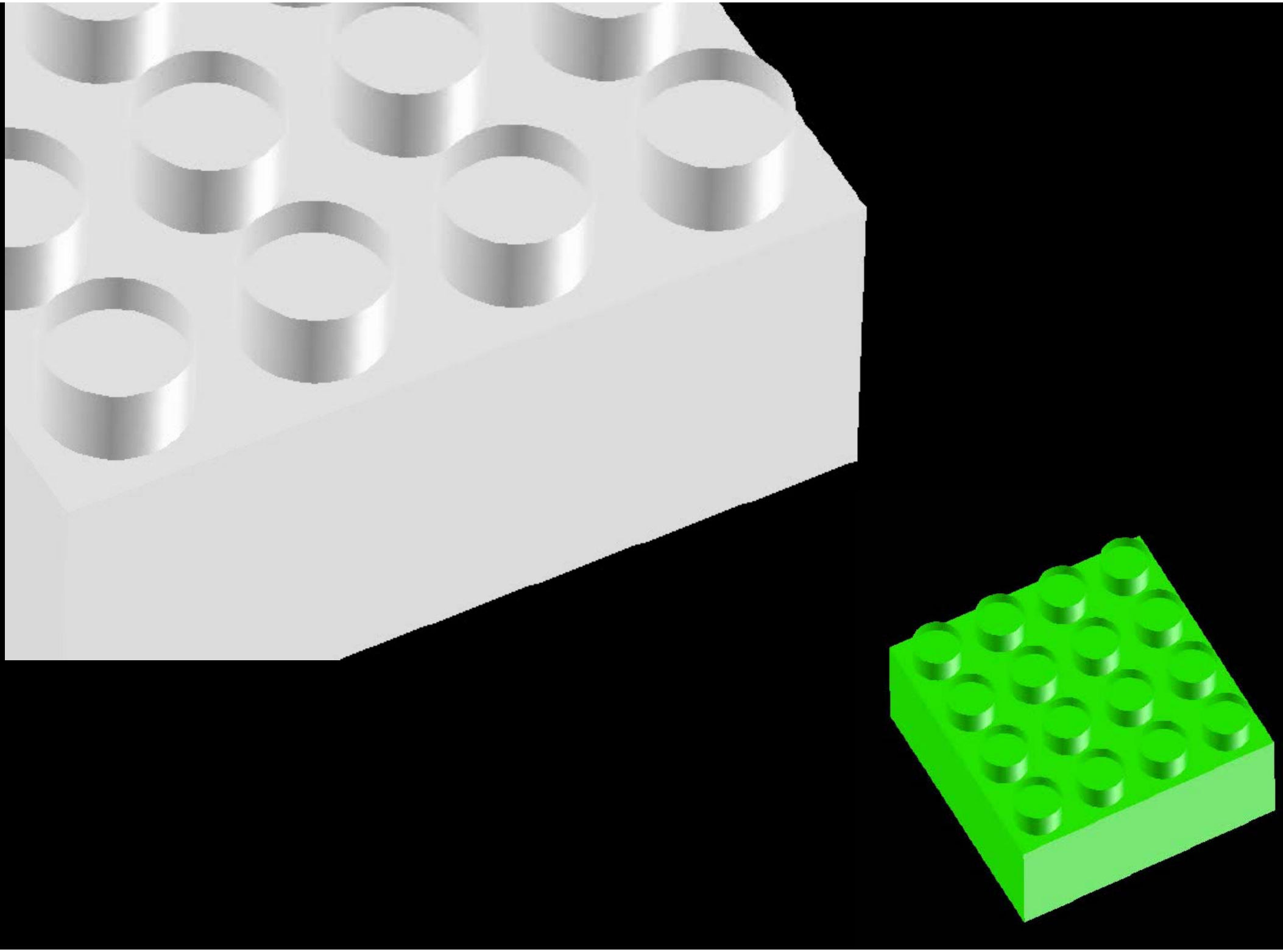
Communicator in MPI

One process can belong to multiple communicators



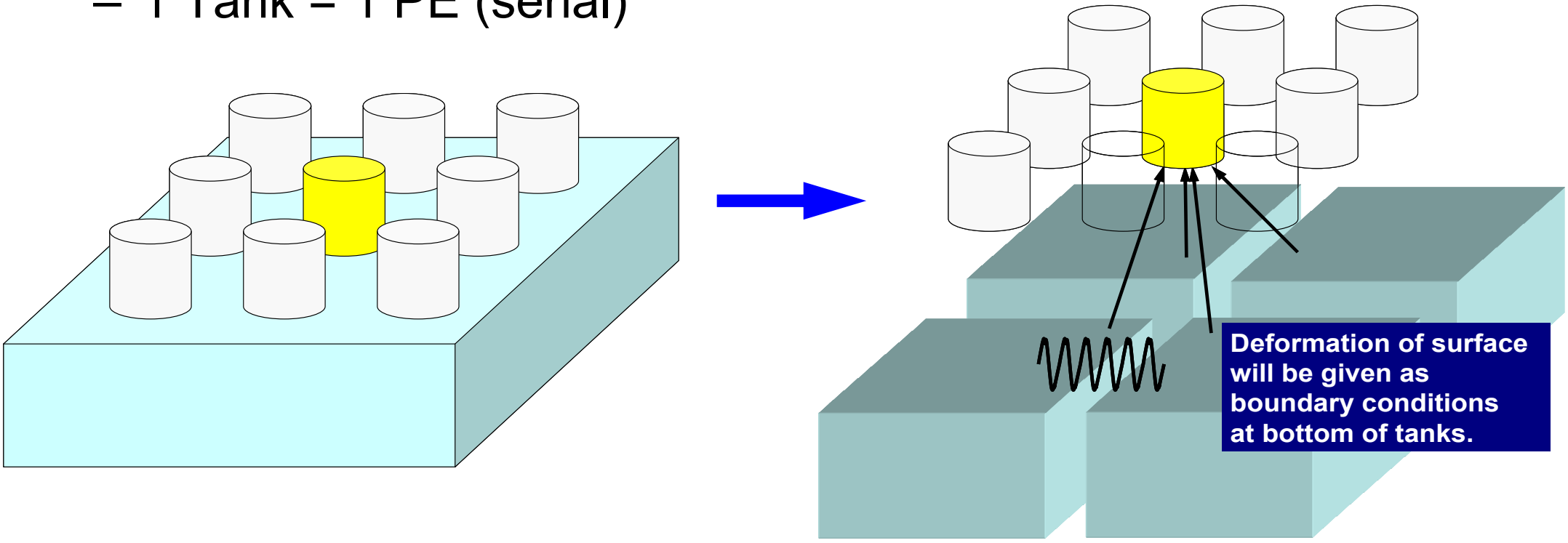
Coupling between “Ground Motion” and “Sloshing of Tanks for Oil-Storage”





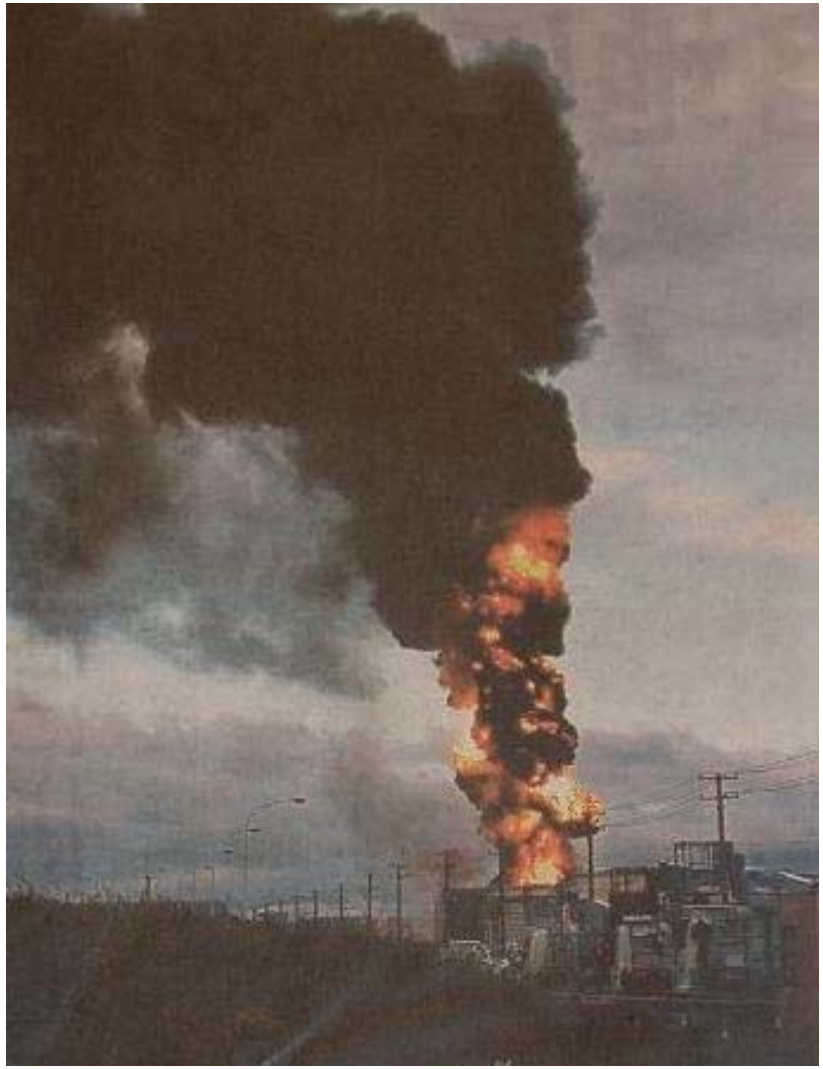
Target Application

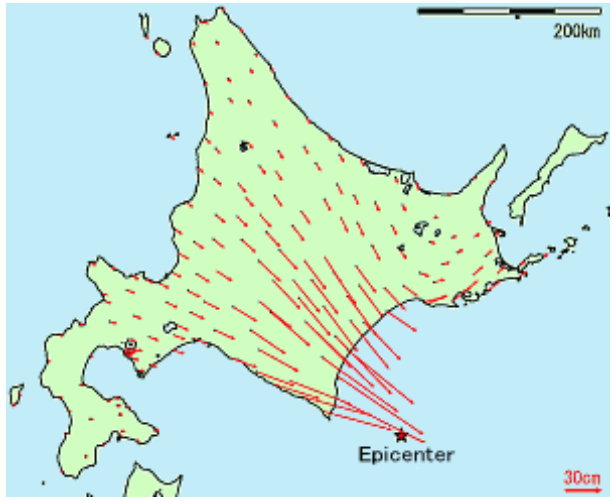
- Coupling between “Ground Motion” and “Sloshing of Tanks for Oil-Storage”
  - “One-way” coupling from “Ground Motion” to “Tanks”.
  - Displacement of ground surface is given as forced displacement of bottom surface of tanks.
  - 1 Tank = 1 PE (serial)



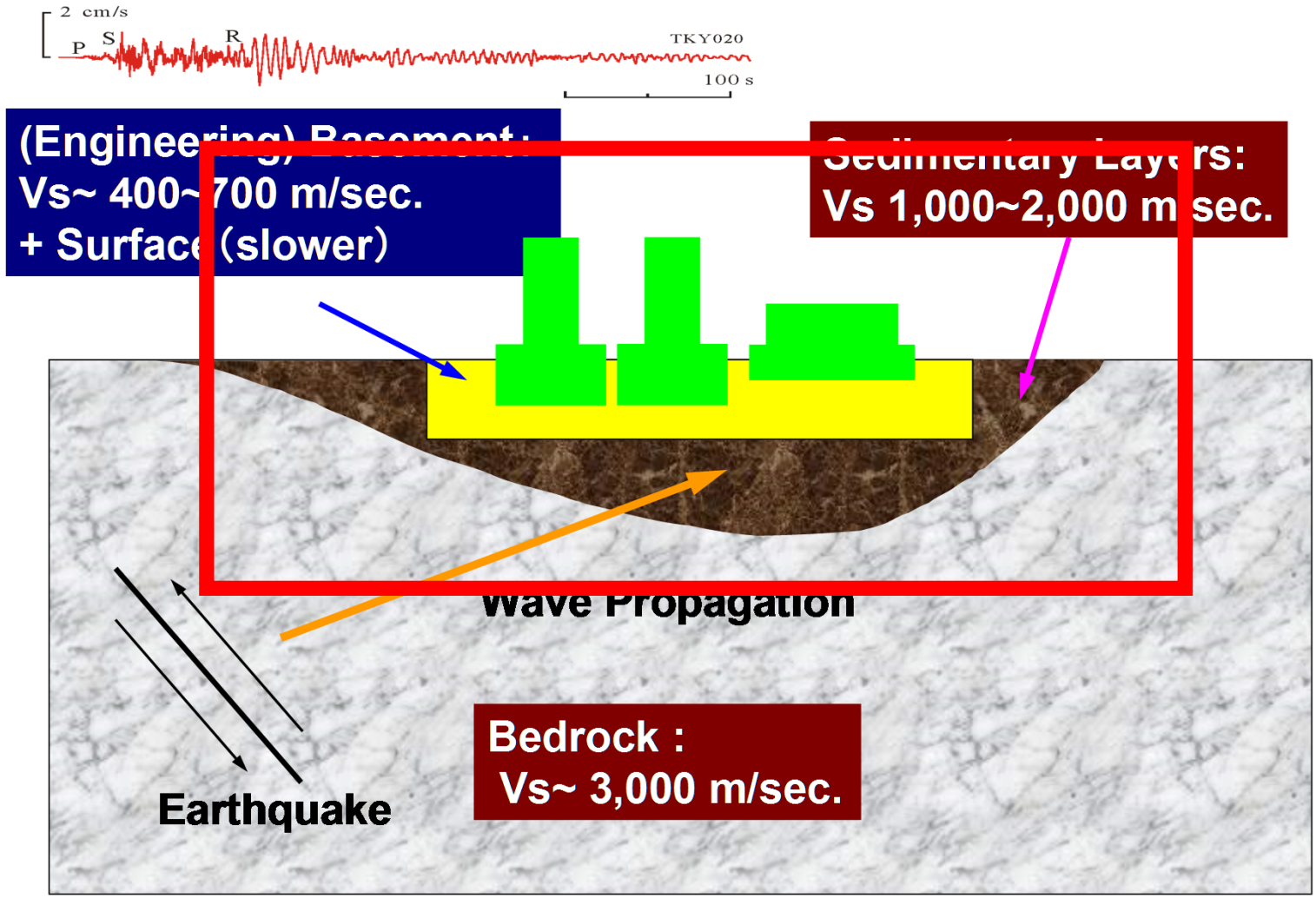
2003 Tokachi Earthquake (M8.0)

Fire accident of oil tanks due to long period
ground motion (surface waves) developed in the basin of Tomakomai



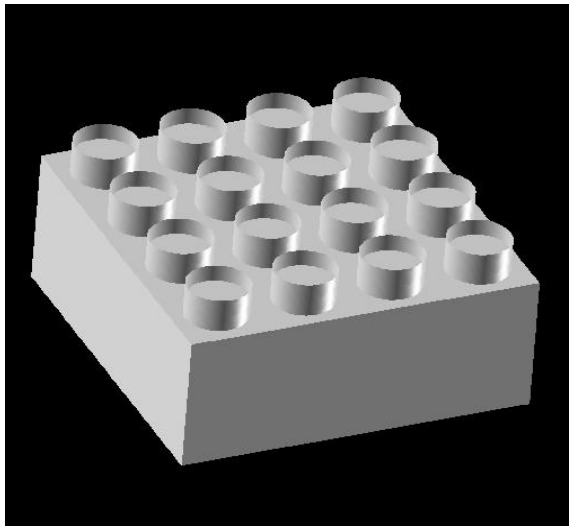


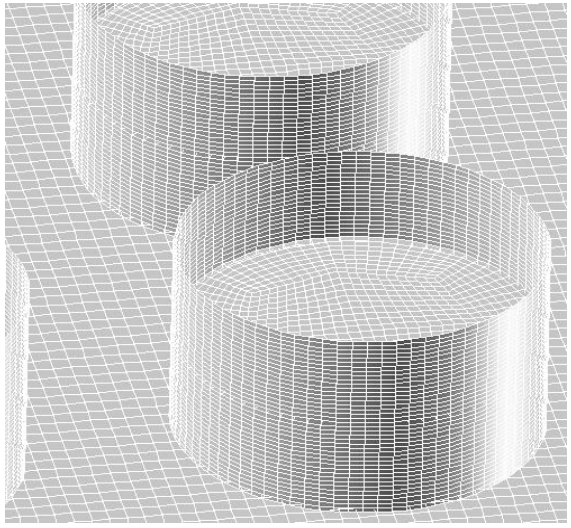
Seismic Wave Propagation, Underground Structure



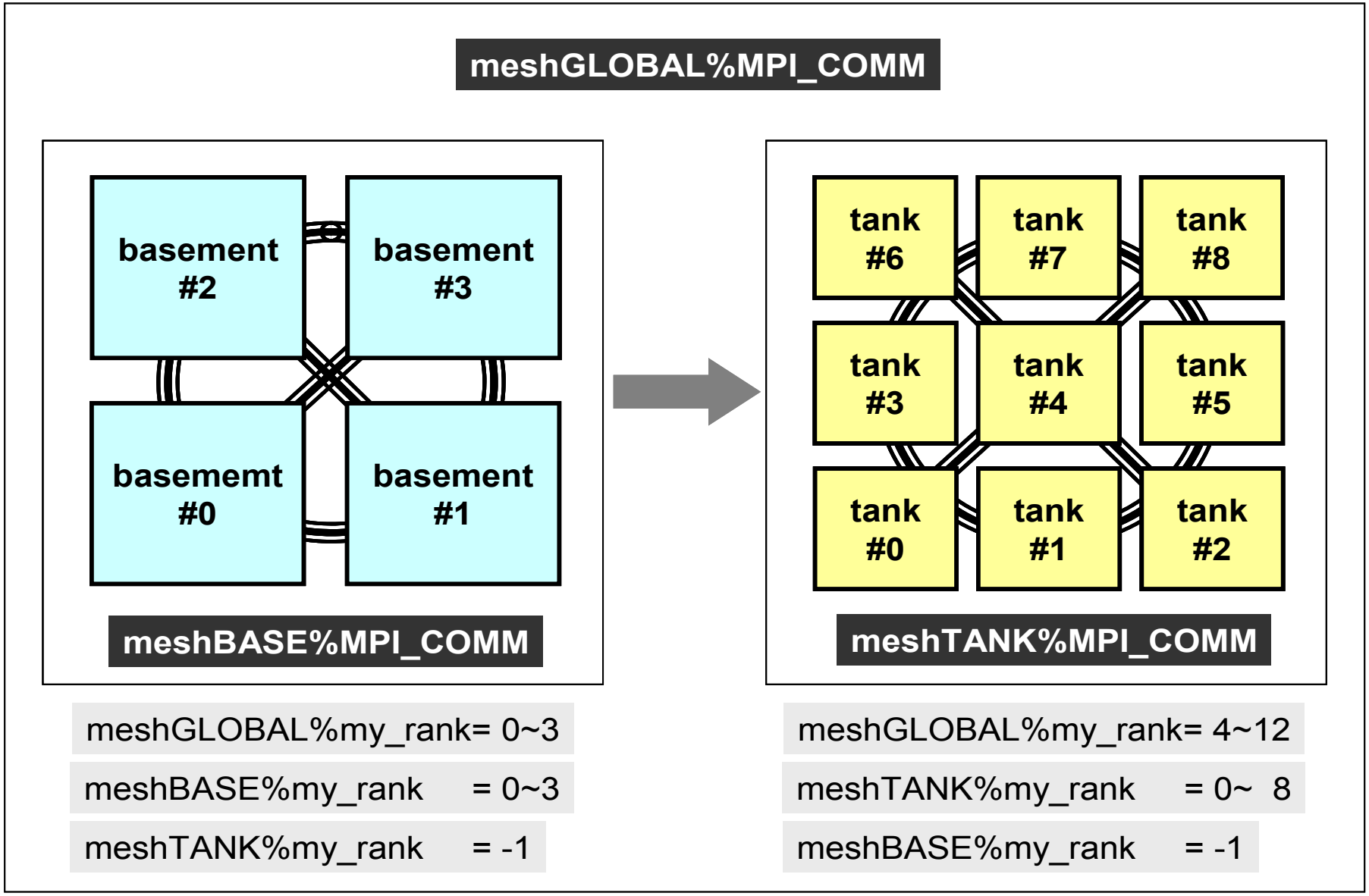
Simulation Codes

- Ground Motion (Ichimura): Fortran
  - Parallel FEM, 3D Elastic/Dynamic
    - Explicit forward Euler scheme
  - Each element: 2m × 2m × 2m cube
  - 240m × 240m × 100m region
- Sloshing of Tanks (Nagashima): C
  - Serial FEM (Embarrassingly Parallel)
    - Implicit backward Euler, Skyline method
    - Shell elements + Inviscid potential flow
  - D: 42.7m, H: 24.9m, T: 20mm,
  - Frequency: 7.6sec.
  - 80 elements in circ., 0.6m mesh in height
  - Tank-to-Tank: 60m, 4 × 4
- Total number of unknowns: 2,918,169





Three Communicators



Fortran

MPI_COMM_RANK

- Determines the rank of the calling process in the communicator
  - "ID of MPI process" is sometimes called "rank"

- **MPI_COMM_RANK (comm, rank, ierr)**
  - **comm** I I communicator
  - **rank** I O rank of the calling process in the group of comm
    Starting from "0"
  - **ierr** I O completion code

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

write (*,'(a,2i8)') 'Hello World FORTRAN', my_rank, PETOT

call MPI_FINALIZE (ierr)

stop
end
```

Fortran

MPI_ABORT

- Aborts MPI execution environment

- **`call MPI_ABORT (comm, errcode, ierr)`**
  - **`comm`** I I communication
  - **`errcode`** I O error code
  - **`ierr`** I O completion code

Fortran

MPI_WTIME

- Returns an elapsed time on the calling processor
- **time= MPI_WTIME ()**
  - **time** R8 O Time in seconds since an arbitrary time in the past.

```
…
real(kind=8):: Stime, Etime

Stime= MPI_WTIME ()
do i= 1, 100000000
  a= 1.d0
enddo
Etime= MPI_WTIME ()

write (*,'(i5,1pe16.6)') my_rank, Etime-Stime
```

Example of MPI_Wtime

```
$> cd <$O-S1>

$> mpifccpx –O1 time.c
$> mpifrtpx –O1 time.f

(modify go4.sh, 4 processes)
$> pjsub go4.sh

     0    1.113281E+00
     3    1.113281E+00
     2    1.117188E+00
     1    1.117188E+00

 Process      Time
   ID
```

MPI_Wtick

- Returns the resolution of MPI_Wtime
- depends on hardware, and compiler

- **time= MPI_Wtick ()**
  - **time** R8 O Time in seconds of resolution of MPI_Wtime

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'

…
TM= MPI_WTICK ()
write (*,*) TM
…
```

```
double Time;

…
Time = MPI_Wtick();
printf("%5d%16.6E¥n", MyRank, Time);
…
```

Example of MPI_Wtick

```
$> cd <$O-S1>

$> mpifccpx –O1 wtick.c
$> mpifrtpx –O1 wtick.f

(modify go1.sh, 1 process)
$> pjsub go1.sh
```

Fortran

MPI_BARRIER

- Blocks until all processes in the communicator have reached this routine.
- Mainly for debugging, huge overhead, not recommended for real code.

- **`call MPI_BARRIER (comm, ierr)`**
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

- What is MPI ?
- Your First MPI Program: Hello World
- **Global/Local Data**
- Collective Communication
- Peer-to-Peer Communication

Data Structures & Algorithms

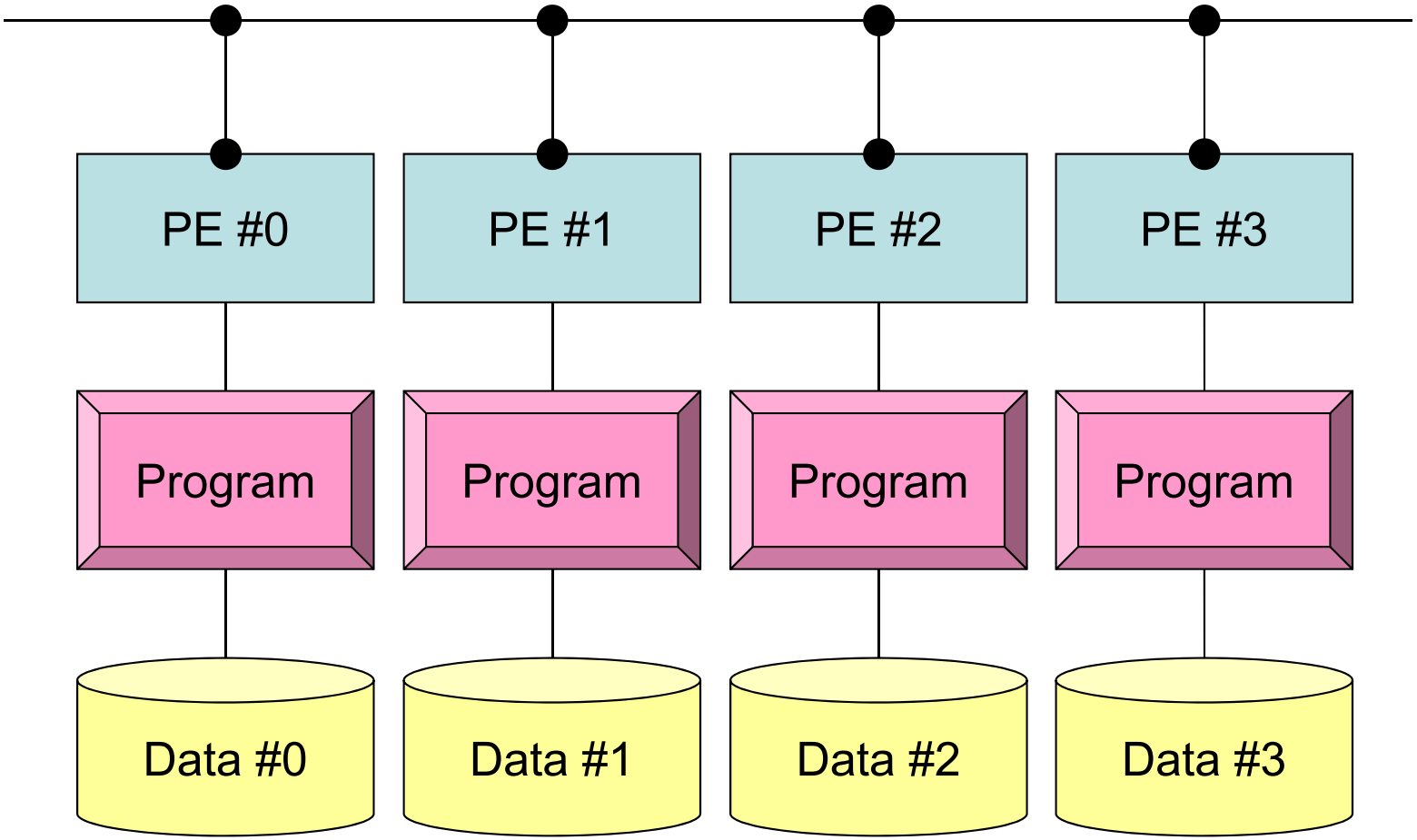
- Computer program consists of data structures and algorithms.
- They are closely related. In order to implement an algorithm, we need to specify an appropriate data structure for that.
  - We can even say that “Data Structures=Algorithms”
  - Some people may not agree with this, I (KN) think it is true for scientific computations from my experiences.

- Appropriate data structures for parallel computing must be specified before starting parallel computing.

SPMD：Single Program Multiple Data

- There are various types of "*parallel computing*", and there are many algorithms.
- Common issue is SPMD (Single Program Multiple Data).
- It is ideal that parallel computing is done in the same way for serial computing (except communications)
  - It is required to specify processes with communications and those without communications.

What is a data structure which is appropriate for SPMD ?



Data Structure for SMPD (1/2)

- SPMD: Large data is decomposed into small pieces, and each piece is processed by each processor/process
- Consider the following simple computation for vector **Vg** with lengh of **Ng** (=20):

```
integer, parameter :: NG= 20
real(kind=8), dimension(20) :: VG

do i= 1, NG
  VG(i)= 2.0 * VG(i)
enddo
```

- If you compute this using four processors, each processor stores and processes 5 (=20/4) components of **Vg**.

Data Structure for SMPD (2/2)

- i.e.

```
integer, parameter :: NL= 5
real(kind=8), dimension(5) :: VL

do i= 1, NL
  VL(i)= 2.0 * VL(i)
enddo
```

- Thus, a “single program” can execute parallel processing.
  - In each process, components of “VI” are different: Multiple Data
  - Computation using only “VI” (as long as possible) leads to efficient parallel computation.
  - Program is not different from that for serial CPU (in the previous page).

Global & Local Data

- Vg
  - Entire Domain
  - “Global Data” with “Global ID” from 1 to 20
- Vl
  - for Each Process (PE, Processor, Domain)
  - “Local Data” with “Local ID” from 1 to 5
  - Efficient utilization of local data leads to excellent parallel efficiency.

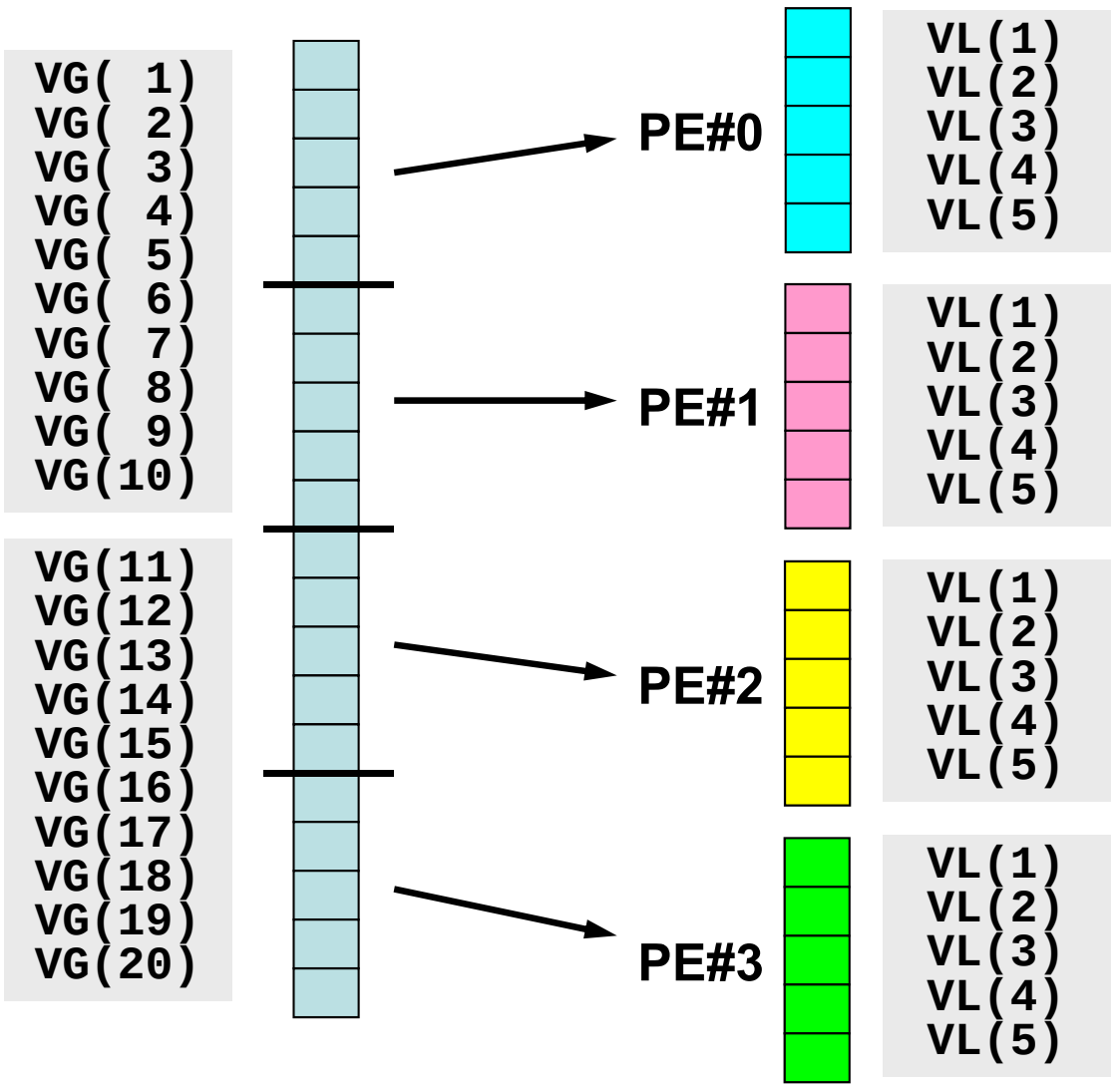
Fortran

Idea of Local Data

Vg: Global Data

- 1st-5th comp. on PE#0
- 6th-10th comp. on PE#1
- 11th-15th comp. on PE#2
- 16th-20th comp. on PE#3

Each of these four sets corresponds to 1st-5th components of **Vl** (local data) where there local ID's are 1-5.



Global & Local Data

- Vg
  - Entire Domain
  - “Global Data” with “Global ID” from 1 to 20
- Vl
  - for Each Process (PE, Processor, Domain)
  - “Local Data” with “Local ID” from 1 to 5
- Please keep your attention to the following:
  - How to generate Vl (local data) from Vg (global data)
  - How to map components, from Vg to Vl, and from Vl to Vg.
  - What to do if Vl cannot be calculated on each process in independent manner.
  - Processing as localized as possible leads to excellent parallel efficiency:
    - Data structures & algorithms for that purpose.

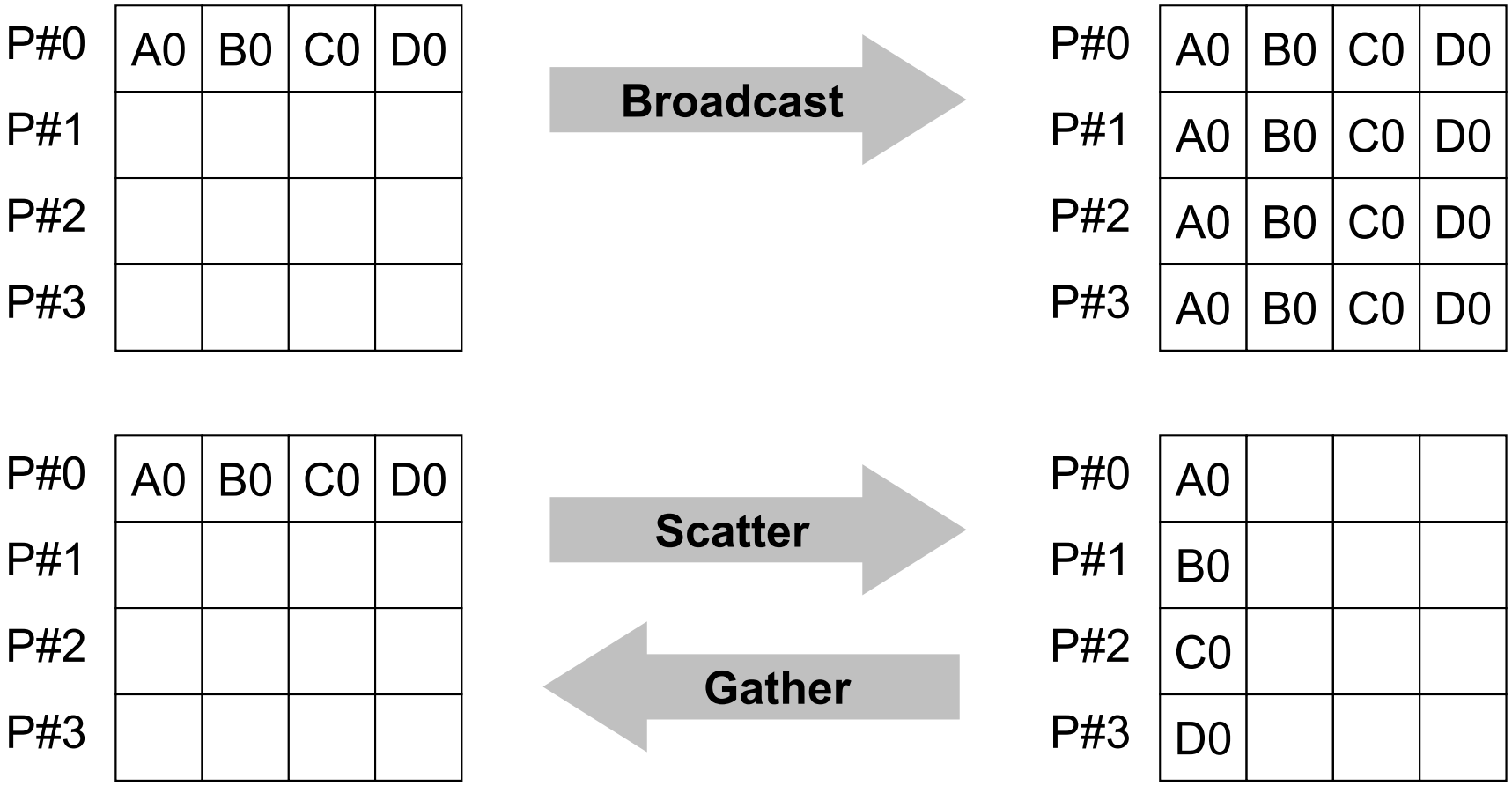
- What is MPI ?
- Your First MPI Program: Hello World
- Global/Local Data
- **Collective Communication**
- Peer-to-Peer Communication

What is Collective Communication ?
集団通信，グループ通信

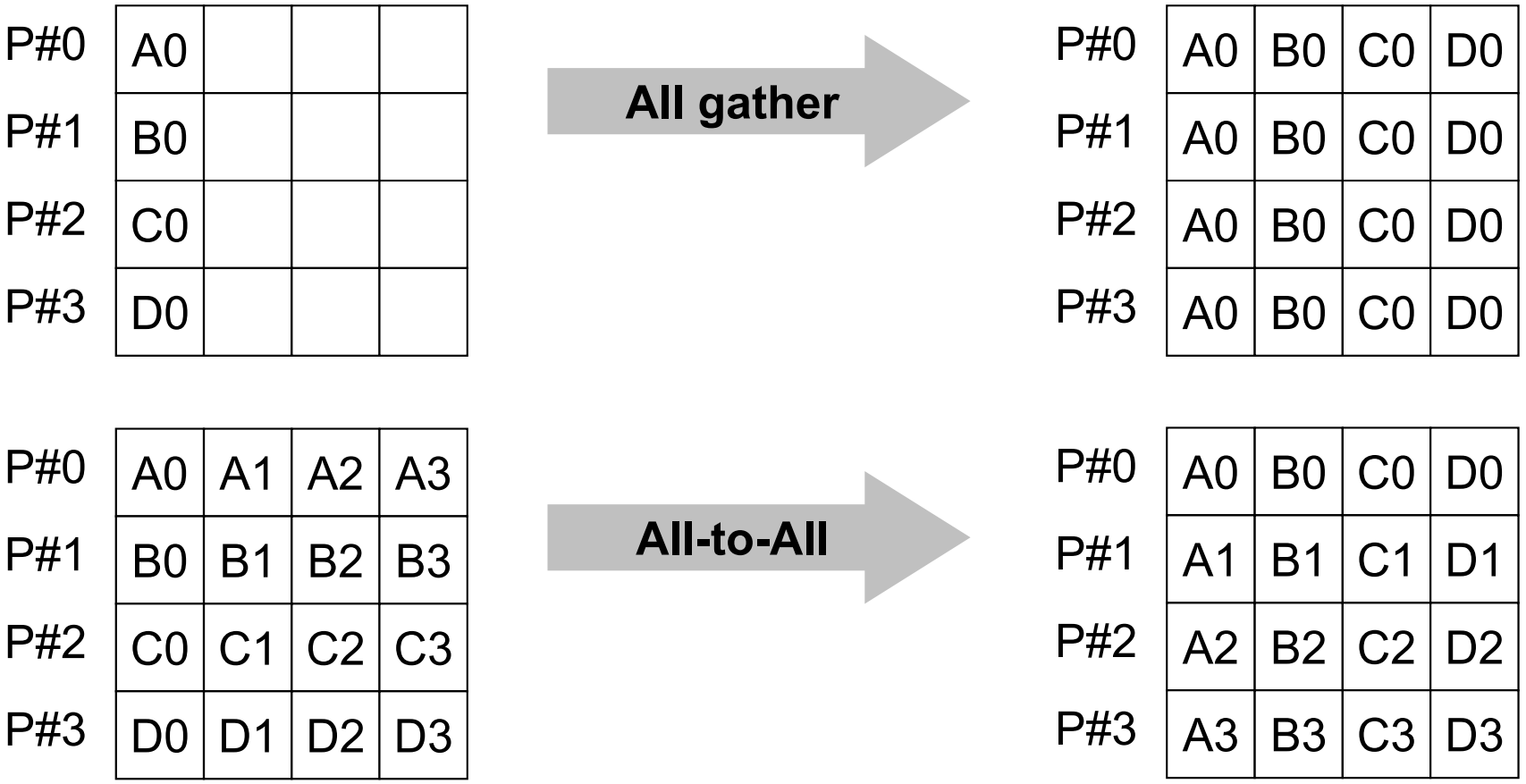
- Collective communication is the process of exchanging information between multiple MPI processes in the communicator: one-to-all or all-to-all communications.

- Examples
  - Broadcasting control data
  - Max, Min
  - Summation
  - Dot products of vectors
  - Transformation of dense matrices

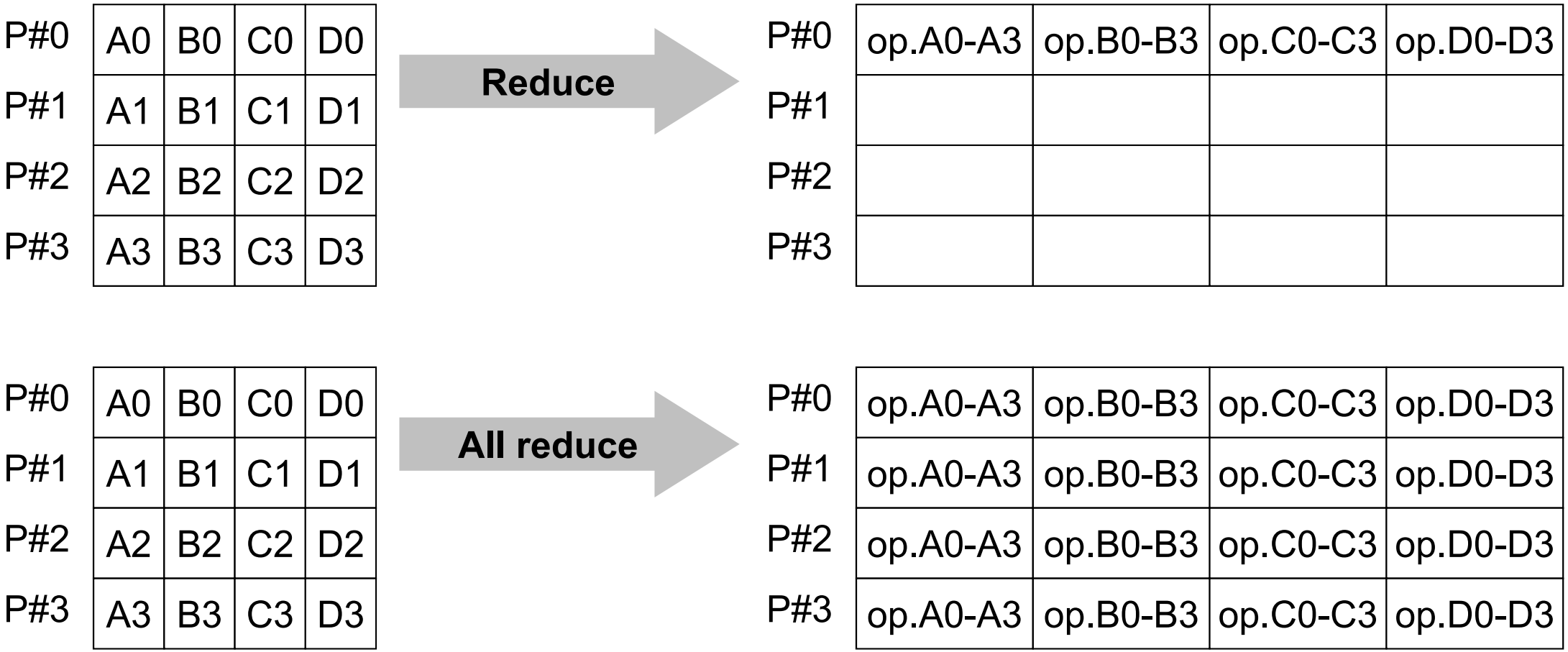
Example of Collective Communications (1/4)



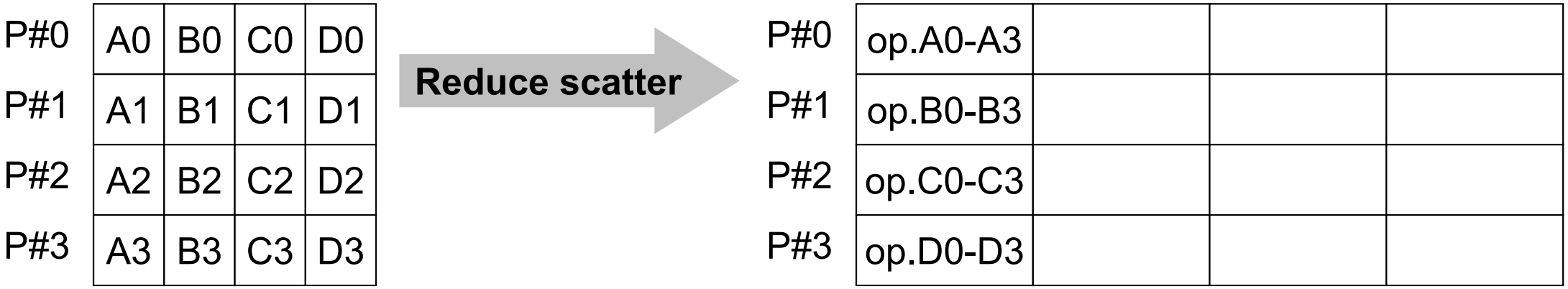
Example of Collective Communications (2/4)



Example of Collective Communications (3/4)



Example of Collective Communications (4/4)



Examples by Collective Comm.

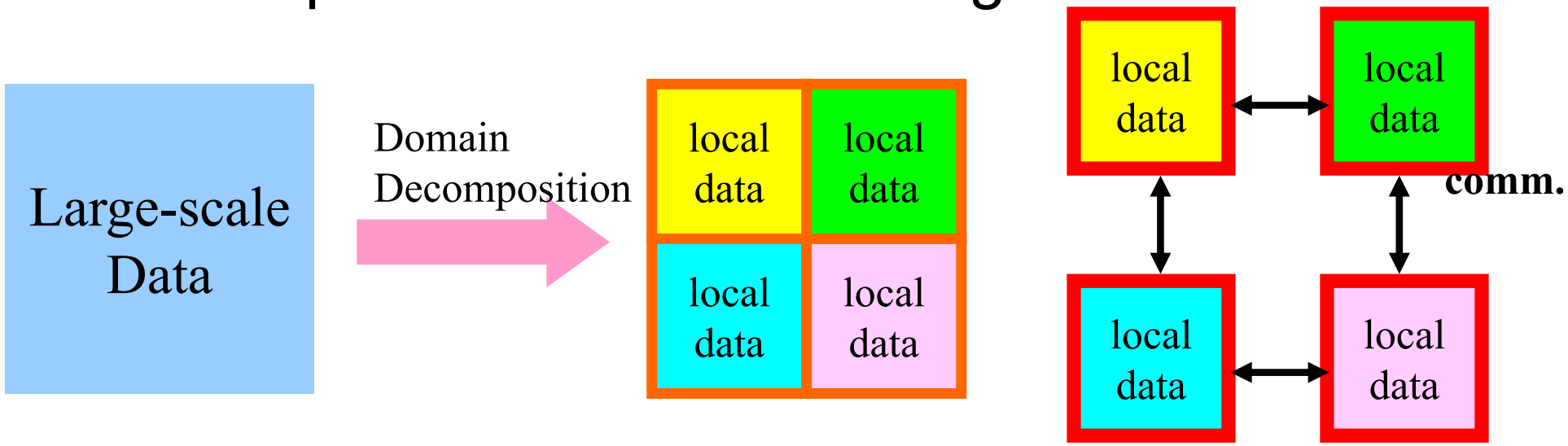
- Dot Products of Vectors
- Scatter/Gather
- Reading Distributed Files
- MPI_Allgatherv

Global/Local Data

- Data structure of parallel computing based on SPMD, where large scale “global data” is decomposed to small pieces of “local data”.

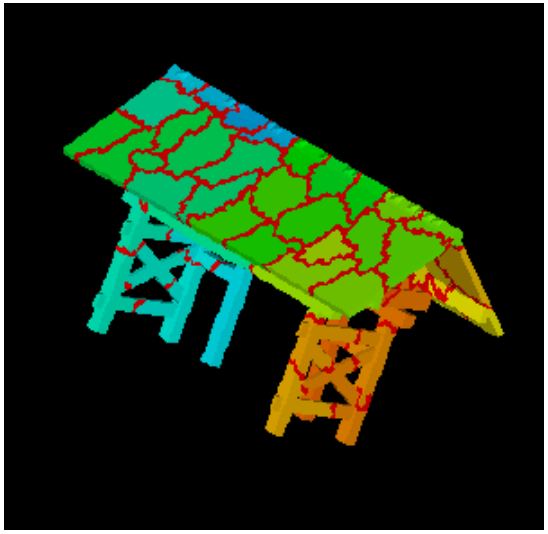
Domain Decomposition/Partitioning

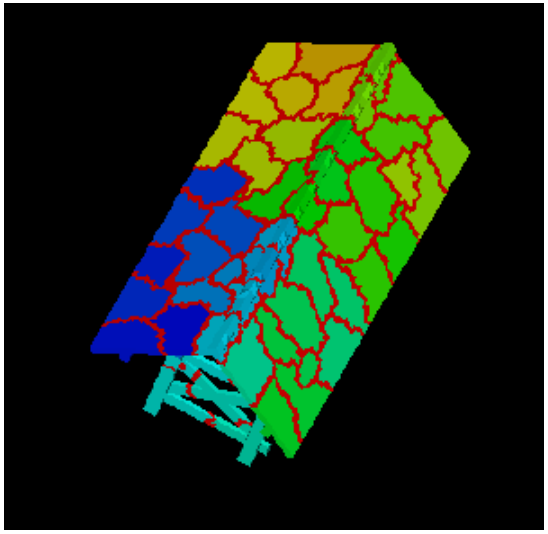
- PC with 1GB RAM: can execute FEM application with up to 10^6 meshes
  - 10^3km × 10^3 km × 10^2 km (SW Japan): 10^8 meshes by 1km cubes
- Large-scale Data: Domain decomposition, parallel & local operations
- Global Computation: Comm. among domains needed



Local Data Structure

- It is important to define proper local data structure for target computation (and its algorithm)
  - Algorithms= Data Structures
- Main objective of this class !





Global/Local Data

- Data structure of parallel computing based on SPMD, where large scale “global data” is decomposed to small pieces of “local data”.

- Consider the dot product of following VECp and VECs with length=20 by parallel computation using 4 processors

```
VECp( 1)=  2
    ( 2)=  2
    ( 3)=  2
…
    (18)=  2
    (19)=  2
    (20)=  2
```

```
VECs( 1)=  3
    ( 2)=  3
    ( 3)=  3
…
    (18)=  3
    (19)=  3
    (20)=  3
```

```
VECp[ 0]=  2
    [ 1]=  2
    [ 2]=  2
…
    [17]=  2
    [18]=  2
    [19]=  2
```

```
VECs[ 0]=  3
    [ 1]=  3
    [ 2]=  3
…
    [17]=  3
    [18]=  3
    [19]=  3
```

<$O-S1>/dot.f, dot.c

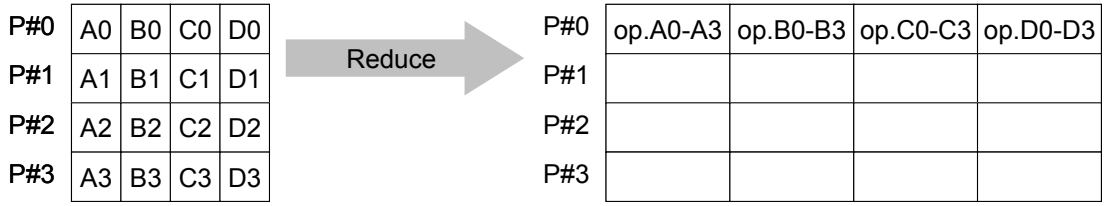
```
implicit REAL*8 (A-H,O-Z)
real(kind=8),dimension(20):: &
    VECp,  VECs

do i= 1, 20
  VECp(i)= 2.0d0
  VECs(i)= 3.0d0
enddo

sum= 0.d0
do ii= 1, 20
  sum= sum + VECp(ii)*VECs(ii)
enddo

stop
end
```

```
#include <stdio.h>
int main(){
   int i;
   double VECp[20], VECs[20]
   double sum;

   for(i=0;i<20;i++){
     VECp[i]= 2.0;
     VECs[i]= 3.0;
   }

   sum = 0.0;
   for(i=0;i<20;i++){
     sum += VECp[i] * VECs[i];
   }
   return 0;
}
```

<$O-S1>/dot.f, dot.c

```
>$ cd <$O-S1>

>$ cc -O3 dot.c
>$ g95 –O3 dot.f

>$ ./a.out

   1          2.          3.
   2          2.          3.
   3          2.          3.
…
  18          2.          3.
  19          2.          3.
  20          2.          3.

dot product       120.
```

MPI_REDUCE



- Reduces values on all processes to a single value
  - Summation, Product, Max, Min etc.

- **`call MPI_REDUCE (sendbuf,recvbuf,count,datatype,op,root,comm,ierr)`**
  - **`sendbuf`** choice I starting address of send buffer
  - **`recvbuf`** choice O starting address receive buffer
    type is defined by "**`datatype`**"
  - **`count`** I I number of elements in send/receive buffer
  - **`datatype`** I I data type of elements of send/recive buffer
    FORTRAN MPI_INTEGER, MPI_REAL, MPI_DOUBLE_PRECISION, MPI_CHARACTER etc.
    C MPI_INT, MPI_FLOAT, MPI_DOUBLE, MPI_CHAR etc
  - **`op`** I I reduce operation
    MPI_MAX, MPI_MIN, MPI_SUM, MPI_PROD, MPI_LAND, MPI_BAND etc
    Users can define operations by **`MPI_OP_CREATE`**
  - **`root`** I I rank of root process
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

Fortran

Send/Receive Buffer (Sending/Receiving)

- Arrays of “send (sending) buffer” and “receive (receiving) buffer” often appear in MPI.

- Addresses of “send (sending) buffer” and “receive (receiving) buffer” must be different.

Fortran

Example of MPI_Reduce (1/2)

```
call MPI_REDUCE
(sendbuf,recvbuf,count,datatype,op,root,comm,ierr)
```

```
real(kind=8):: X0, X1

call MPI_REDUCE
(X0, X1, 1, MPI_DOUBLE_PRECISION, MPI_MAX, 0, <comm>, ierr)
```

```
real(kind=8):: X0(4), XMAX(4)

call MPI_REDUCE
(X0, XMAX, 4, MPI_DOUBLE_PRECISION, MPI_MAX, 0, <comm>, ierr)
```

Global Max. values of X0(i) go to XMAX(i) on #0 process (i=1-4)

Fortran

Example of MPI_Reduce (2/2)

```
call MPI_REDUCE
(sendbuf,recvbuf,count,datatype,op,root,comm,ierr)
```

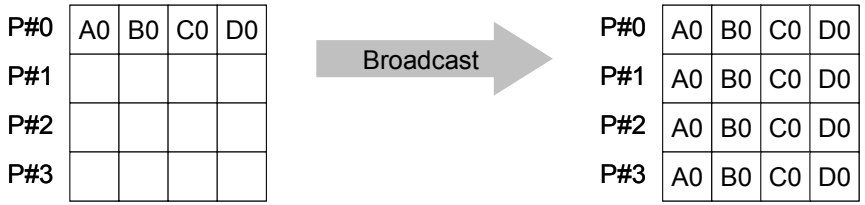
```
real(kind=8):: X0, XSUM

call MPI_REDUCE
(X0, XSUM, 1, MPI_DOUBLE_PRECISION, MPI_SUM, 0, <comm>, ierr)
```

Global summation of X0 goes to XSUM on #0 process.

```
real(kind=8):: X0(4)

call MPI_REDUCE
(X0(1), X0(3), 2, MPI_DOUBLE_PRECISION, MPI_SUM, 0, <comm>, ierr)
```

- Global summation of X0(1) goes to X0(3) on #0 process.
- Global summation of X0(2) goes to X0(4) on #0 process.

MPI_BCAST

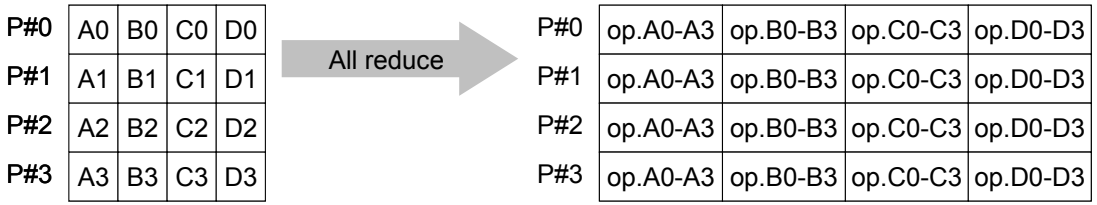


- Broadcasts a message from the process with rank "root" to all other processes of the communicator

- **`call MPI_BCAST (buffer,count,datatype,root,comm,ierr)`**
  - **`buffer`** choice I/O — starting address of buffer
    type is defined by "**`datatype`**"
  - **`count`** I I — number of elements in send/recv buffer
  - **`datatype`** I I — data type of elements of send/recv buffer
    FORTRAN `MPI_INTEGER, MPI_REAL, MPI_DOUBLE_PRECISION, MPI_CHARACTER etc.`
    C `MPI_INT, MPI_FLOAT, MPI_DOUBLE, MPI_CHAR etc.`
  - **`root`** I I — rank of root process
  - **`comm`** I I — communicator
  - **`ierr`** I O — completion code

Fortran

MPI_ALLREDUCE



- MPI_Reduce + MPI_Bcast
- Summation (of dot products) and MAX/MIN values are likely to utilized in each process

- **`call MPI_ALLREDUCE (sendbuf,recvbuf,count,datatype,op, comm,ierr)`**
  - **`sendbuf`** choice I — starting address of send buffer
  - **`recvbuf`** choice O — starting address receive buffer
    type is defined by "**`datatype`**"
  - **`count`** I I — number of elements in send/recv buffer
  - **`datatype`** I I — data type of elements in send/recv buffer
  - **`op`** I I — reduce operation
  - **`comm`** I I — commuinicator
  - **`ierr`** I O — completion code

Fortran

“op” of MPI_Reduce/Allreduce

Fortran

```
call MPI_REDUCE
(sendbuf,recvbuf,count,datatype,op,root,comm,ierr)
```

- **MPI_MAX**, **MPI_MIN** Max, Min
- **MPI_SUM**, **MPI_PROD** Summation, Product
- **MPI_LAND** Logical AND

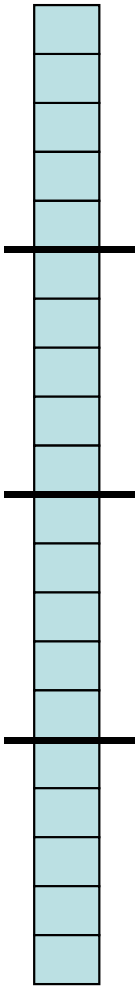
Local Data (1/2)

Fortran

- Decompose vector with length=20 into 4 domains (processes)
- Each process handles a vector with length= 5

```
VECp( 1)=  2
    ( 2)=  2
    ( 3)=  2
…
    (18)=  2
    (19)=  2
    (20)=  2
```

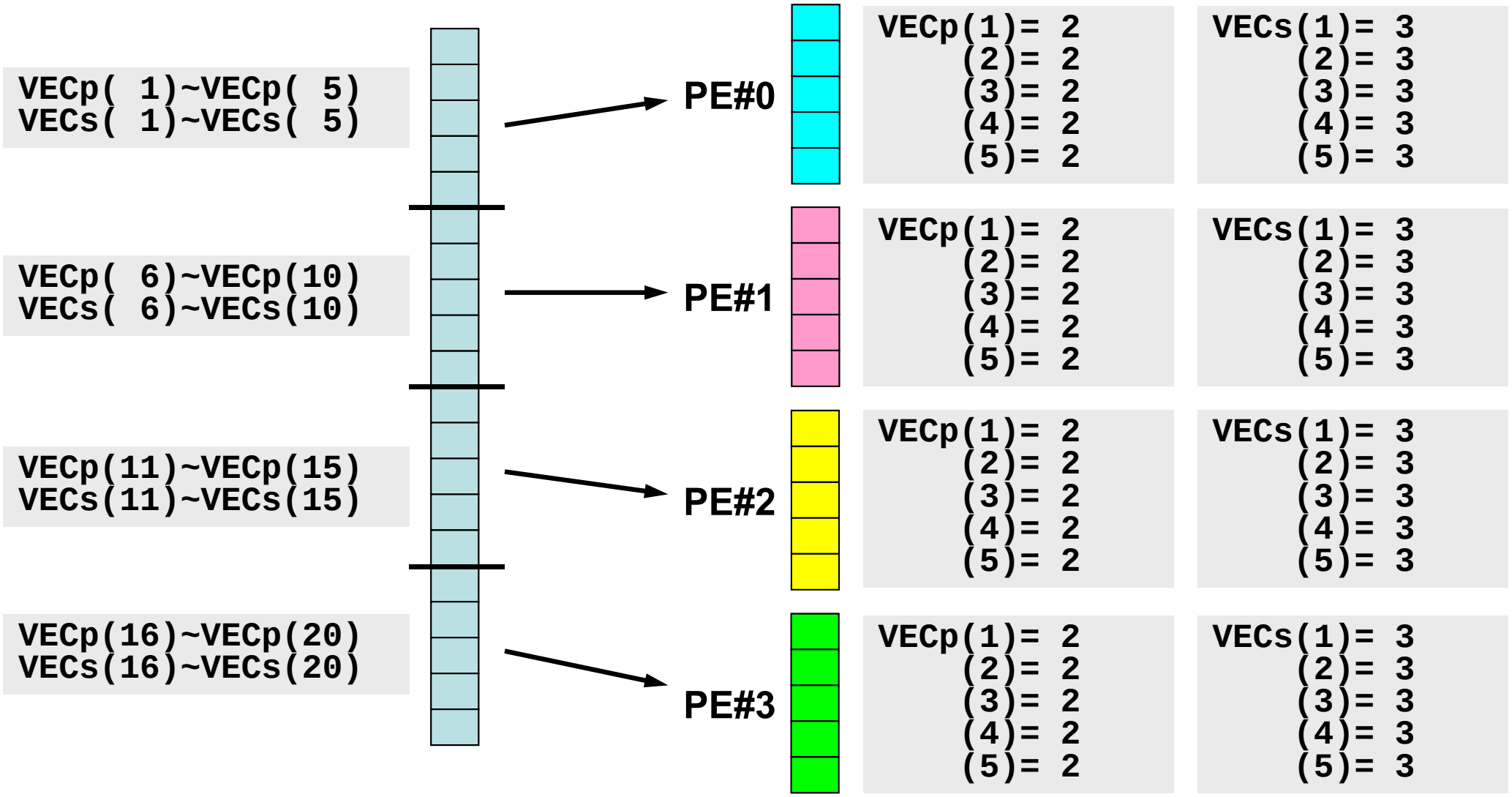
```
VECs( 1)=   3
    ( 2)=   3
    ( 3)=   3
…
    (18)=   3
    (19)=   3
    (20)=   3
```



Local Data (2/2)

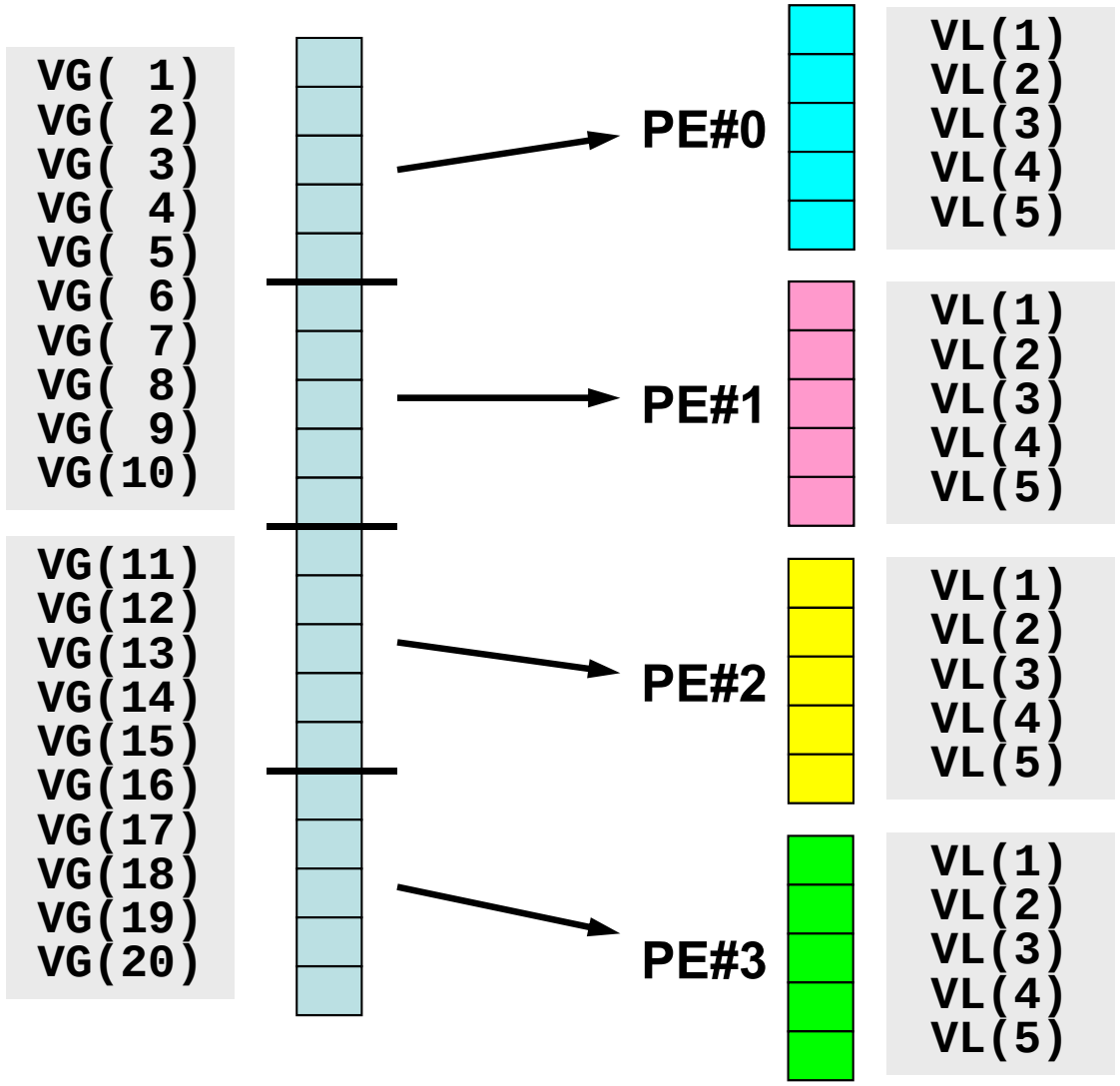
Fortran

- 1th-5th components of original global vector go to 1th-5th components of PE#0, 6th-10th -> PE#1, 11th-15th -> PE#2, 16th-20th -> PE#3.



But ...

- It is too easy !! Just decomposing and renumbering from 1 (or 0).
- Of course, this is not enough. Further examples will be shown in the latter part.



Example: Dot Product (1/3)

<$O-S1>/allreduce.f

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr
real(kind=8), dimension(5) :: VECp,  VECs

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

sumA= 0.d0
sumR= 0.d0
do i= 1, 5
  VECp(i)= 2.d0
  VECs(i)= 3.d0
enddo

sum0= 0.d0
do i= 1, 5
  sum0= sum0 + VECp(i) * VECs(i)
enddo

if (my_rank.eq.0) then
  write (*,'(a)') '(my_rank, sumALLREDUCE, sumREDUCE)‘
endif
```

Local vector is generated at each local process.

Example: Dot Product (2/3)

<$O-S1>/allreduce.f

```
!C
!C-- REDUCE
  call MPI_REDUCE (sum0, sumR, 1, MPI_DOUBLE_PRECISION, MPI_SUM, 0, &
                   MPI_COMM_WORLD, ierr)

!C
!C-- ALL-REDUCE
  call MPI_Allreduce (sum0, sumA, 1, MPI_DOUBLE_PRECISION, MPI_SUM, &
                      MPI_COMM_WORLD, ierr)

  write (*,'(a,i5, 2(1pe16.6))') 'before BCAST', my_rank, sumA, sumR
```

Dot Product

Summation of results of each process (sum0)

“sumR” has value only on PE#0.

“sumA” has value on all processes by MPI_Allreduce

Example: Dot Product (3/3)

<$O-S1>/allreduce.f

```
!C
!C-- BCAST
  call MPI_BCAST (sumR, 1, MPI_DOUBLE_PRECISION, 0, MPI_COMM_WORLD, &
                  ierr)
  write (*,'(a,i5, 2(1pe16.6))') 'after  BCAST', my_rank, sumA, sumR

  call MPI_FINALIZE (ierr)

  stop
  end
```

“sumR” has value on PE#1-#3 by MPI_Bcast

Execute <$O-S1>/allreduce.f/c

```
$> mpifccpx –Kfast allreduce.c
$> mpifrtpx –Kfast allreduce.f
(modify go4.sh, 4 process)
$> pjsub go4.sh

(my_rank, sumALLREDUCE,sumREDUCE)
before BCAST    0    1.200000E+02    1.200000E+02
after  BCAST    0    1.200000E+02    1.200000E+02

before BCAST    1    1.200000E+02    0.000000E+00
after  BCAST    1    1.200000E+02    1.200000E+02

before BCAST    3    1.200000E+02    0.000000E+00
after  BCAST    3    1.200000E+02    1.200000E+02

before BCAST    2    1.200000E+02    0.000000E+00
after  BCAST    2    1.200000E+02    1.200000E+02
```

Examples by Collective Comm.

- Dot Products of Vectors
- Scatter/Gather
- Reading Distributed Files
- MPI_Allgatherv

Global/Local Data (1/3)

- Parallelization of an easy process where a real number α is added to each component of real vector **VECg**:

```
      do i= 1, NG
        VECg(i)= VECg(i) + ALPHA
      enddo
```

```
for (i=0; i<NG; i++{
    VECg[i]= VECg[i] + ALPHA
}
```

Global/Local Data (2/3)

- Configurationa
  - **NG= 32 (length of the vector)**
  - **ALPHA=1000.**
  - Process # of MPI= 4

- Vector VECg has following 32 components (<$T-S1>/a1x.all):

```
(101.0,  103.0,  105.0,  106.0,  109.0,  111.0,  121.0,  151.0,
 201.0,  203.0,  205.0,  206.0,  209.0,  211.0,  221.0,  251.0,
 301.0,  303.0,  305.0,  306.0,  309.0,  311.0,  321.0,  351.0,
 401.0,  403.0,  405.0,  406.0,  409.0,  411.0,  421.0,  451.0)
```

Global/Local Data (3/3)

- Procedure
  - ① Reading vector **VECg** with length=32 from one process (*e.g.* 0th process)
    - Global Data
  - ② Distributing vector components to 4 MPI processes equally (*i.e.* length= 8 for each processes)
    - Local Data, Local ID/Numbering
  - ③ Adding **ALPHA** to each component of the local vector (with length= 8) on each process.
  - ④ Merging the results to global vector with length= 32.

- Actually, we do not need parallel computers for such a kind of small computation.

Operations of Scatter/Gather (1/8)

Reading **VECg** (length=32) from a process (*e.g.* #0)

- Reading global data from #0 process

```
include   'mpif.h'
integer,  parameter :: NG= 32
real(kind=8), dimension(NG):: VECg

call MPI_INIT (ierr)
call MPI_COMM_SIZE (<comm>, PETOT  , ierr)
call MPI_COMM_RANK (<comm>, my_rank, ierr)

if (my_rank.eq.0) then
  open (21, file= 'a1x.all', status= 'unknown')
  do i= 1, NG
    read (21,*) VECg(i)
  enddo
  close (21)
endif
```

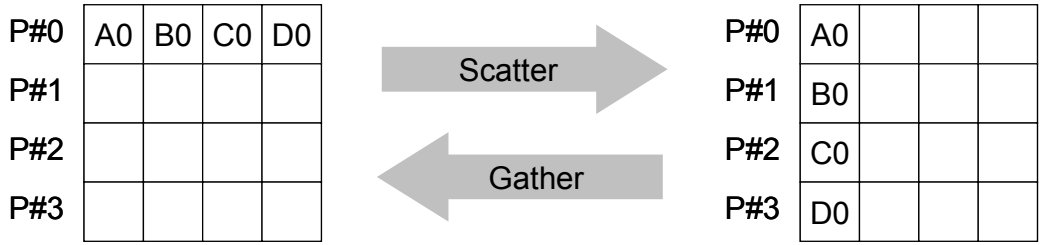
```
#include <mpi.h>
#include <stdio.h>
#include <math.h>
#include <assert.h>

int main(int argc, char **argv){
  int i, NG=32;
  int PeTot, MyRank, MPI_Comm;
  double VECg[32];
  char filename[80];
  FILE *fp;

  MPI_Init(&argc, &argv);
  MPI_Comm_size(<comm>, &PeTot);
  MPI_Comm_rank(<comm>, &MyRank);

        fp = fopen("a1x.all", "r");
        if(!MyRank) for(i=0;i<NG;i++){
                fscanf(fp, "%lf", &VECg[i]);
        }
```

Operations of Scatter/Gather (2/8)

Distributing global data to 4 process equally (*i.e.* length=8 for each process)

- MPI_Scatter

MPI_SCATTER



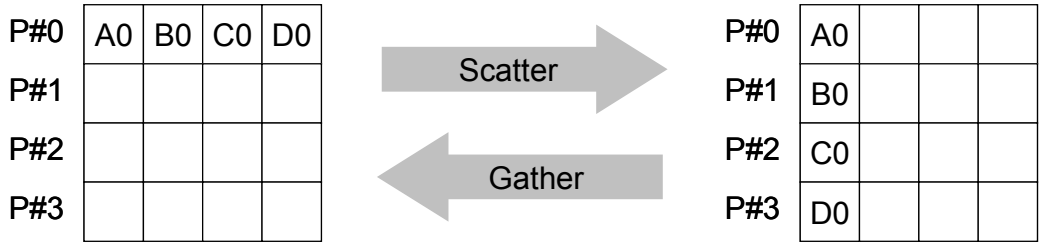
- Sends data from one process to all other processes in a communicator
  - scount-size messages are sent to each process

- **call MPI_SCATTER (sendbuf, scount, sendtype, recvbuf, rcount, recvtype, root, comm, ierr)**
  - **sendbuf** choice I starting address of sending buffer
    type is defined by "**datatype**"
  - **scount** I I number of elements sent to each process
  - **sendtype** I I data type of elements of sending buffer

    FORTRAN MPI_INTEGER, MPI_REAL, MPI_DOUBLE_PRECISION, MPI_CHARACTER etc.
    C MPI_INT, MPI_FLOAT, MPI_DOUBLE, MPI_CHAR etc.
  - **recvbuf** choice O starting address of receiving buffer
  - **rcount** I I number of elements received from the root process
  - **recvtype** I I data type of elements of receiving buffer
  - **root** I I rank of root process
  - **comm** I I communicator
  - **ierr** I O completion code

Fortran

MPI_SCATTER (cont.)



- **`call MPI_SCATTER (sendbuf, scount, sendtype, recvbuf, rcount, recvtype, root, comm, ierr)`**
  - **`sendbuf`** choice I — starting address of sending buffer; type is defined by "**`datatype`**"
  - **`scount`** I I — number of elements sent to each process
  - **`sendtype`** I I — data type of elements of sending buffer
  - **`recvbuf`** choice O — starting address of receiving buffer
  - **`rcount`** I I — number of elements received from the root process
  - **`recvtype`** I I — data type of elements of receiving buffer
  - **`root`** I I — rank of root process
  - **`comm`** I I — communicator
  - **`ierr`** I O — completion code
- Usually
  - **`scount = rcount`**
  - **`sendtype= recvtype`**
- This function sends **`scount`** components starting from **`sendbuf`** (sending buffer) at process **`#root`** to each process in **`comm`**. Each process receives **`rcount`** components starting from **`recvbuf`** (receiving buffer).

Fortran

Operations of Scatter/Gather (3/8)

Distributing global data to 4 processes equally

- Allocating receiving buffer **VEC** (length=8) at each process.
- 8 components sent from sending buffer **VECg** of process #0 are received at each process #0-#3 as 1st-8th components of receiving buffer **VEC**.

```
integer, parameter :: N =  8
real(kind=8), dimension(N ) :: VEC
...
call MPI_Scatter                              &
     (VECg, N, MPI_DOUBLE_PRECISION, &
      VEC , N, MPI_DOUBLE_PRECISION, &
      0, <comm>, ierr)
```

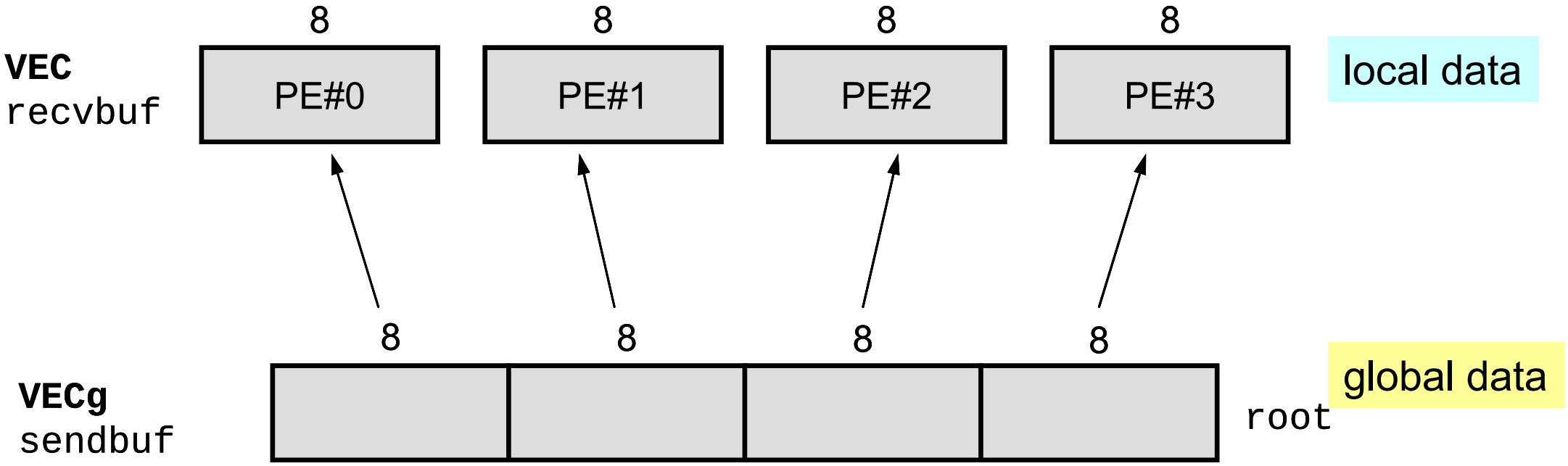
```
int  N=8;
double VEC [8];
...
MPI_Scatter  (VECg,  N,  MPI_DOUBLE,  VEC,  N,
MPI_DOUBLE, 0, <comm>);
```

```
call MPI_SCATTER
(sendbuf, scount, sendtype, recvbuf, rcount,
 recvtype, root, comm, ierr)
```

Operations of Scatter/Gather (4/8)

Distributing global data to 4 processes equally

- 8 components are *scattered* to each process from root (#0)
- 1st-8th components of **VECg** are stored as 1st-8th ones of **VEC** at **#0**, 9th-16th components of **VECg** are stored as 1st-8th ones of **VEC** at **#1**, etc.
  - **VECg**: Global Data, **VEC**: Local Data



Operations of Scatter/Gather (5/8)

Distributing global data to 4 processes equally

- Global Data: 1st-32nd components of **VECg** at **#0**
- Local Data: 1st-8th components of **VEC** at each process
- Each component of **VEC** can be written from each process in the following way:

```
do i= 1, N
  write (*,'(a, 2i8,f10.0)') 'before',  my_rank, i, VEC(i)
enddo
```

```
for(i=0;i<N;i++){
printf("before %5d %5d %10.0F¥n", MyRank, i+1, VEC[i]);}
```

Operations of Scatter/Gather (5/8)

Distributing global data to 4 processes equally

- Global Data: 1st-32nd components of **VECg** at **#0**
- Local Data: 1st-8th components of **VEC** at each process
- Each component of **VEC** can be written from each process in the following way:

```
PE#0
before 0 1   101.
before 0 2   103.
before 0 3   105.
before 0 4   106.
before 0 5   109.
before 0 6   111.
before 0 7   121.
before 0 8   151.
```

```
PE#1
before 1 1   201.
before 1 2   203.
before 1 3   205.
before 1 4   206.
before 1 5   209.
before 1 6   211.
before 1 7   221.
before 1 8   251.
```

```
PE#2
before 2 1   301.
before 2 2   303.
before 2 3   305.
before 2 4   306.
before 2 5   309.
before 2 6   311.
before 2 7   321.
before 2 8   351.
```

```
PE#3
before 3 1   401.
before 3 2   403.
before 3 3   405.
before 3 4   406.
before 3 5   409.
before 3 6   411.
before 3 7   421.
before 3 8   451.
```

Operations of Scatter/Gather (6/8)

On each process, **ALPHA** is added to each of 8 components of **VEC**

- On each process, computation is in the following way

```
real(kind=8), parameter :: ALPHA= 1000.
do i= 1, N
  VEC(i)= VEC(i) + ALPHA
enddo
```

```
double ALPHA=1000.;
...
for(i=0;i<N;i++){
  VEC[i]= VEC[i] + ALPHA;}
```

- Results:

```
PE#0
after 0 1  1101.
after 0 2  1103.
after 0 3  1105.
after 0 4  1106.
after 0 5  1109.
after 0 6  1111.
after 0 7  1121.
after 0 8  1151.
```

```
PE#1
after 1 1  1201.
after 1 2  1203.
after 1 3  1205.
after 1 4  1206.
after 1 5  1209.
after 1 6  1211.
after 1 7  1221.
after 1 8  1251.
```

```
PE#2
after 2 1  1301.
after 2 2  1303.
after 2 3  1305.
after 2 4  1306.
after 2 5  1309.
after 2 6  1311.
after 2 7  1321.
after 2 8  1351.
```

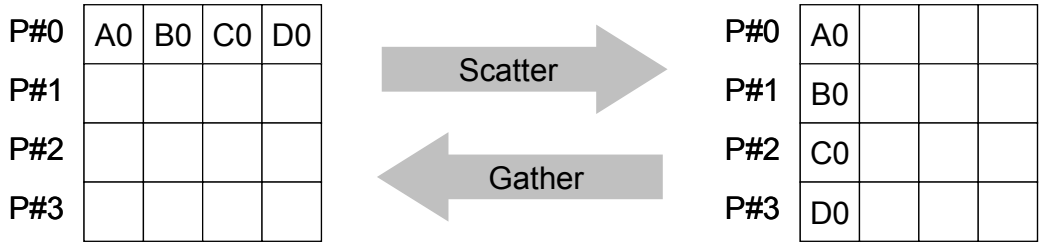
```
PE#3
after 3 1  1401.
after 3 2  1403.
after 3 3  1405.
after 3 4  1406.
after 3 5  1409.
after 3 6  1411.
after 3 7  1421.
after 3 8  1451.
```

Operations of Scatter/Gather (7/8)

Merging the results to global vector with length= 32

- Using MPI_Gather (inverse operation to MPI_Scatter)

MPI_GATHER



- Gathers together values from a group of processes, inverse operation to MPI_Scatter

- **`call MPI_GATHER (sendbuf, scount, sendtype, recvbuf, rcount, recvtype, root, comm, ierr)`**
  - **`sendbuf`** choice I starting address of sending buffer
  - **`scount`** I I number of elements sent to each process
  - **`sendtype`** I I data type of elements of sending buffer
  - **`recvbuf`** choice O starting address of receiving buffer
  - **`rcount`** I I number of elements received from the root process
  - **`recvtype`** I I data type of elements of receiving buffer
  - **`root`** I I rank of root process
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

- **`recvbuf`** is on **`root`** process.

Fortran

Operations of Scatter/Gather (8/8)

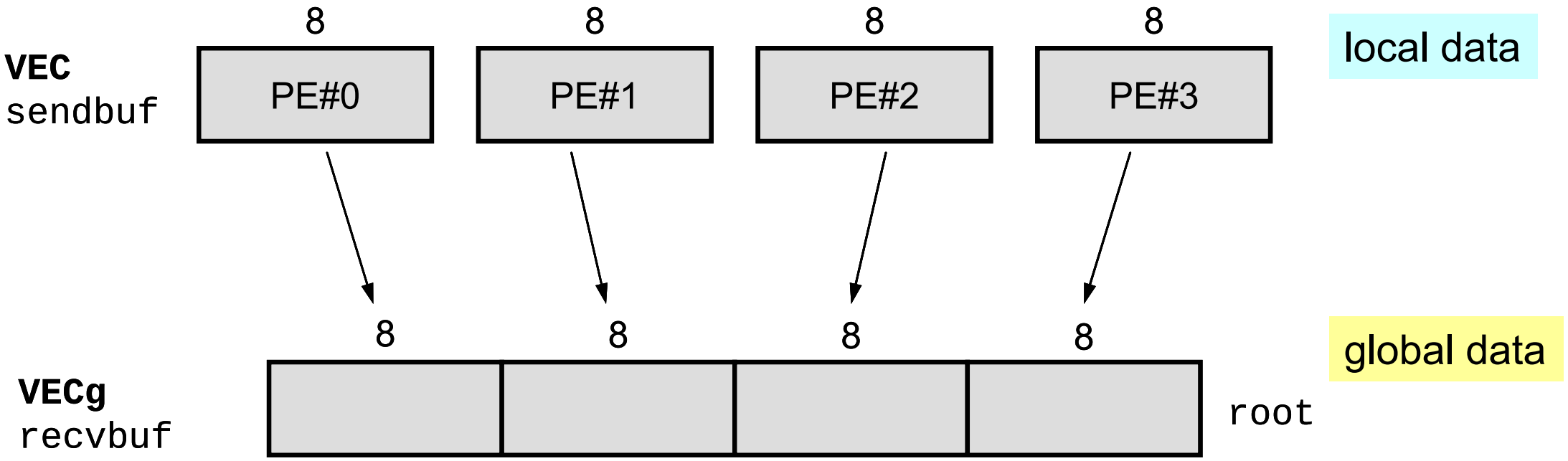
Merging the results to global vector with length= 32

- Each process components of **VEC** to **VECg** on root (#0 in this case).

```
call MPI_Gather                                    &
     (VEC , N, MPI_DOUBLE_PRECISION, &
      VECg, N, MPI_DOUBLE_PRECISION, &
      0, <comm>, ierr)
```

```
MPI_Gather (VEC, N, MPI_DOUBLE, VECg, N,
MPI_DOUBLE, 0, <comm>);
```

- 8 components are gathered from each process to the root process.



<$O-S1>/scatter-gather.f/c example

```
$> mpifccpx –Kfast scatter-gather.c
$> mpifrtpx –Kfast scatter-gather.f
$> (exec.4 proc’s) go4.sh
```

PE#0
```
before 0 1  101.
before 0 2  103.
before 0 3  105.
before 0 4  106.
before 0 5  109.
before 0 6  111.
before 0 7  121.
before 0 8  151.
```

PE#1
```
before 1 1  201.
before 1 2  203.
before 1 3  205.
before 1 4  206.
before 1 5  209.
before 1 6  211.
before 1 7  221.
before 1 8  251.
```

PE#2
```
before 2 1  301.
before 2 2  303.
before 2 3  305.
before 2 4  306.
before 2 5  309.
before 2 6  311.
before 2 7  321.
before 2 8  351.
```

PE#3
```
before 3 1  401.
before 3 2  403.
before 3 3  405.
before 3 4  406.
before 3 5  409.
before 3 6  411.
before 3 7  421.
before 3 8  451.
```

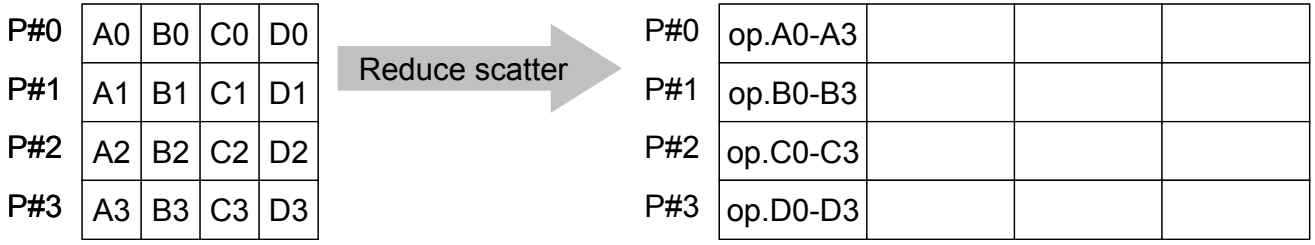
PE#0
```
after 0 1  1101.
after 0 2  1103.
after 0 3  1105.
after 0 4  1106.
after 0 5  1109.
after 0 6  1111.
after 0 7  1121.
after 0 8  1151.
```

PE#1
```
after 1 1  1201.
after 1 2  1203.
after 1 3  1205.
after 1 4  1206.
after 1 5  1209.
after 1 6  1211.
after 1 7  1221.
after 1 8  1251.
```

PE#2
```
after 2 1  1301.
after 2 2  1303.
after 2 3  1305.
after 2 4  1306.
after 2 5  1309.
after 2 6  1311.
after 2 7  1321.
after 2 8  1351.
```

PE#3
```
after 3 1  1401.
after 3 2  1403.
after 3 3  1405.
after 3 4  1406.
after 3 5  1409.
after 3 6  1411.
after 3 7  1421.
after 3 8  1451.
```

MPI_REDUCE_SCATTER

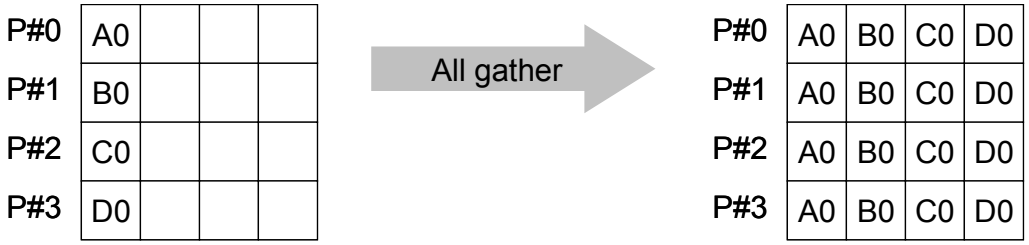


- MPI_REDUCE + MPI_SCATTER

- **`call MPI_REDUCE_SCATTER (sendbuf, recvbuf, rcount, datatype, op, comm, ierr)`**
  - **`sendbuf`** choice I starting address of sending buffer
  - **`recvbuf`** choice O starting address of receiving buffer
  - **`rcount`** I I integer array specifying the number of elements in result distributed to each process. Array must be identical on all calling processes.
  - **`datatype`** I I data type of elements of sending/receiving buffer
  - **`op`** I I reduce operation
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

Fortran

MPI_ALLGATHER

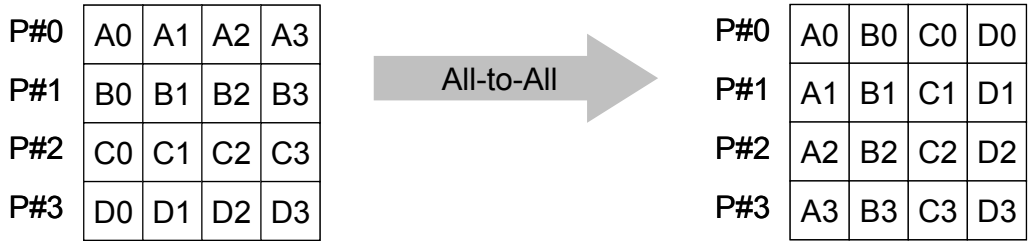


- MPI_GATHER＋MPI_BCAST
  - Gathers data from all tasks and distribute the combined data to all tasks

- **`call MPI_ALLGATHER (sendbuf, scount, sendtype, recvbuf, rcount, recvtype, comm, ierr)`**
  - **`sendbuf`** choice I starting address of sending buffer
  - **`scount`** I I number of elements sent to each process
  - **`sendtype`** I I data type of elements of sending buffer
  - **`recvbuf`** choice O starting address of receiving buffer
  - **`rcount`** I I number of elements received from each process
  - **`recvtype`** I I data type of elements of receiving buffer
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

Fortran

MPI_ALLTOALL



- Sends data from all to all processes: transformation of dense matrix

- **`call MPI_ALLTOALL (sendbuf, scount, sendtype, recvbuf, rcount, recvrype, comm, ierr)`**
  - **`sendbuf`** choice I starting address of sending buffer
  - **`scount`** I I number of elements sent to each process
  - **`sendtype`** I I data type of elements of sending buffer
  - **`recvbuf`** choice O starting address of receiving buffer
  - **`rcount`** I I number of elements received from each process
  - **`recvtype`** I I data type of elements of receiving buffer
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

Fortran

Examples by Collective Comm.

- Dot Products of Vectors
- Scatter/Gather
- Reading Distributed Files
- MPI_Allgatherv

Operations of Distributed Local Files

- In Scatter/Gather example, PE#0 reads global data, that is *scattered* to each processer, then parallel operations are done.

- If the problem size is very large, a single processor may not read entire global data.
  - If the entire global data is decomposed to distributed local data sets, each process can read the local data.
  - If global operations are needed to a certain sets of vectors, MPI functions, such as MPI_Gather etc. are available.

Reading Distributed Local Files: Uniform Vec. Length (1/2)

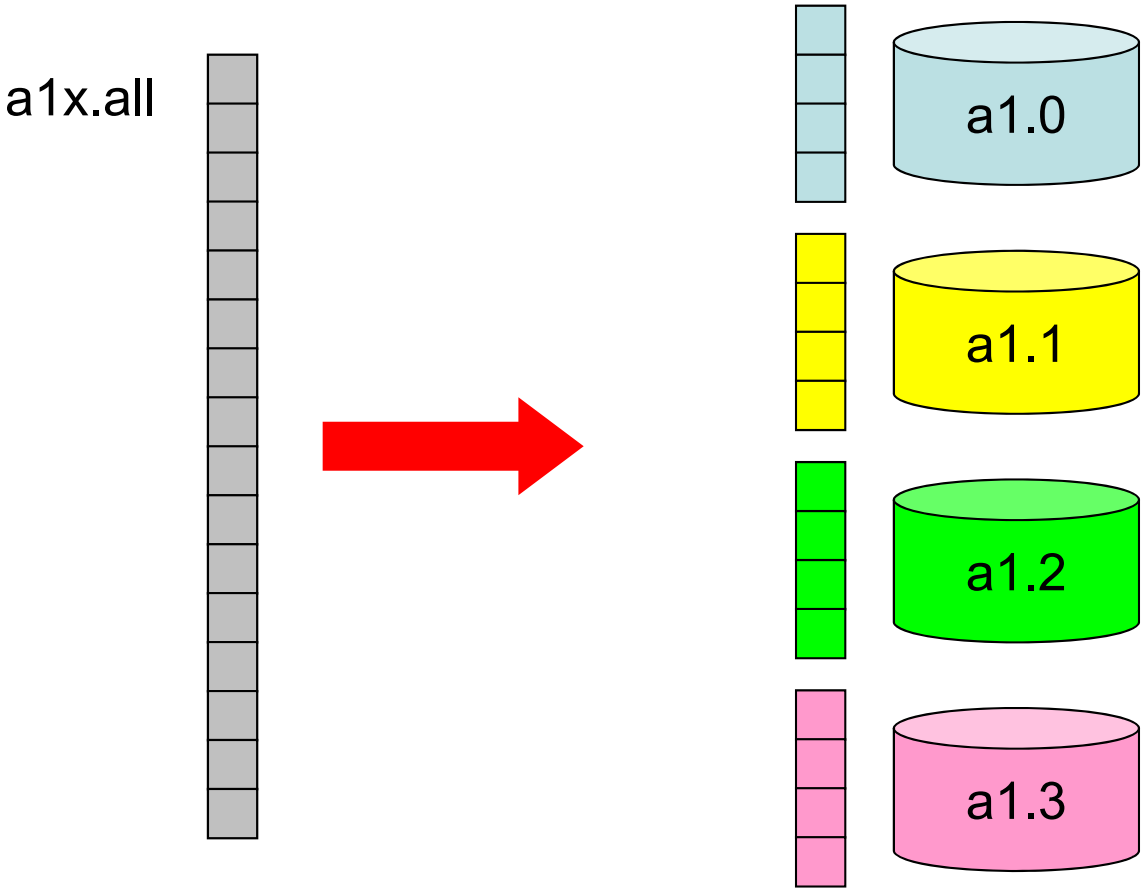
```
>$ cd <$O-S1>
>$ ls a1.*
   a1.0 a1.1 a1.2 a1.3
```

a1x.all is decomposed to 4 files.

```
>$ mpifccpx –Kfast file.c
>$ mpifrtpx –Kfast file.f

(modify go4.sh for 4 processes)
>$ pjsub go4.sh
```

Operations of Distributed Local Files

- Local files `a1.0~a1.3` are originally from global file `a1x.all`.



Reading Distributed Local Files: Uniform Vec. Length (2/2)

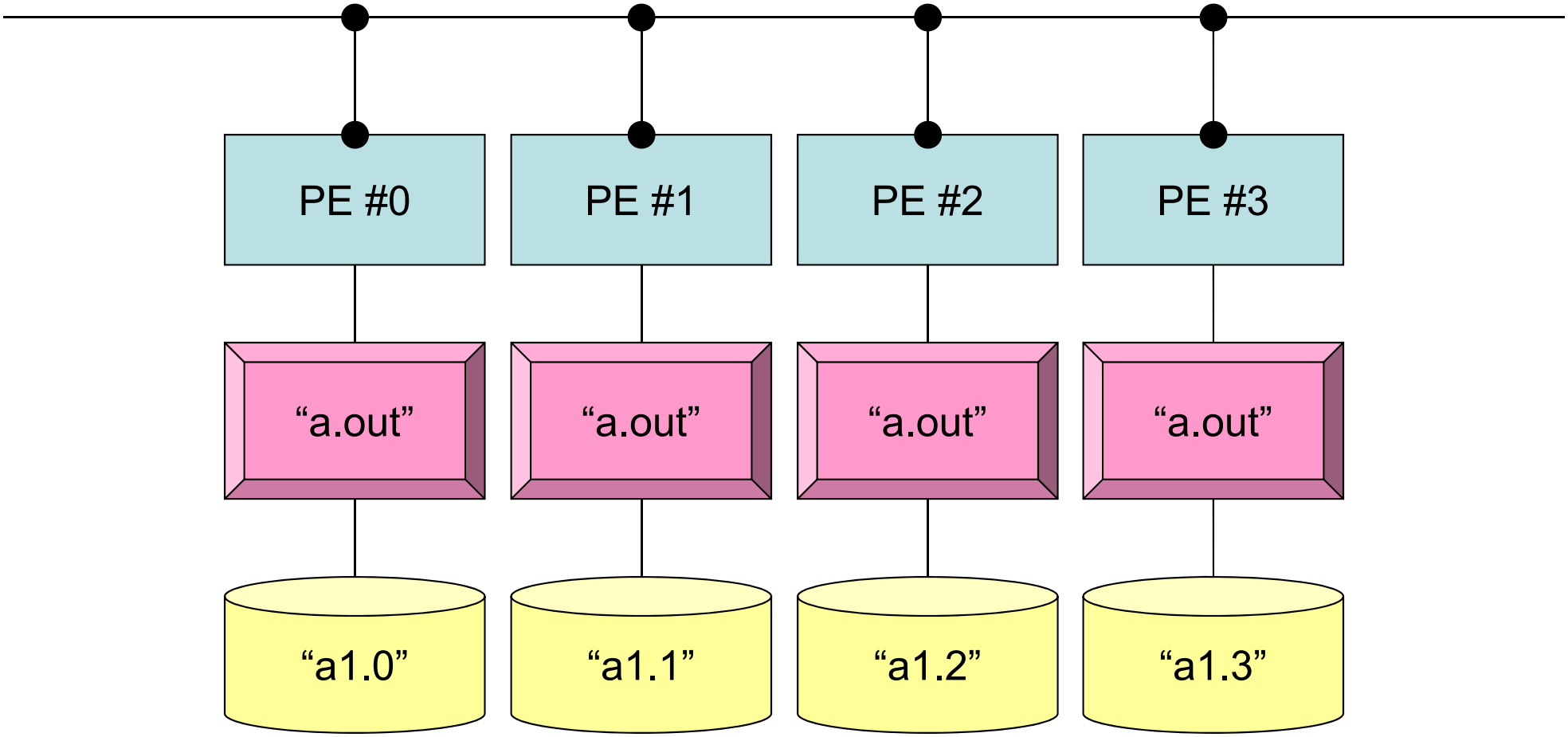
<$O-S1>/file.f

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr
real(kind=8), dimension(8) :: VEC
character(len=80)          :: filename

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

if (my_rank.eq.0) filename= 'a1.0'
if (my_rank.eq.1) filename= 'a1.1'
if (my_rank.eq.2) filename= 'a1.2'
if (my_rank.eq.3) filename= 'a1.3'

open (21, file= filename, status= 'unknown')
  do i= 1, 8
    read (21,*) VEC(i)
  enddo
close (21)

call MPI_FINALIZE (ierr)

stop
end
```

Similar to “Hello”

Local ID is 1-8

Typical SPMD Operation




```
mpirun -np 4 a.out
```

Non-Uniform Vector Length (1/2)

```
>$ cd <$O-S1>
>$ ls a2.*
   a2.0 a2.1 a2.2 a2.3
>$ cat a2.0
  5          Number of Components at each Process
  201.0      Components
  203.0
  205.0
  206.0
  209.0

>$ mpifccpx –Kfast file2.c
>$ mpifrtpx –Kfast file2.f

(modify go4.sh for 4 processes)
>$ pjsub go4.sh
```

Non-Uniform Vector Length (2/2)

<$O-S1>/file2.f

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'
integer :: PETOT, my_rank, ierr
real(kind=8), dimension(:), allocatable :: VEC
character(len=80)                       :: filename

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

 if (my_rank.eq.0) filename= 'a2.0'
 if (my_rank.eq.1) filename= 'a2.1'
 if (my_rank.eq.2) filename= 'a2.2'
 if (my_rank.eq.3) filename= 'a2.3'

 open (21, file= filename, status= 'unknown')
   read (21,*) N
   allocate (VEC(N))
   do i= 1, N
     read (21,*) VEC(i)
   enddo
 close(21)

call MPI_FINALIZE (ierr)
stop
end
```

"N" is different at each process

How to generate local data

- Reading global data (N=NG)
  - Scattering to each process
  - Parallel processing on each process
  - (If needed) reconstruction of global data by gathering local data
- Generating local data (N=NL), or reading distributed local data
  - Generating or reading local data on each process
  - Parallel processing on each process
  - (If needed) reconstruction of global data by gathering local data
- In future, latter case is more important, but former case is also introduced in this class for understanding of operations of global/local data.

Examples by Collective Comm.

- Dot Products of Vectors
- Scatter/Gather
- Reading Distributed Files
- MPI_Allgatherv

MPI_GATHERV, MPI_SCATTERV

- MPI_Gather, MPI_Scatter
  - Length of message from/to each process is uniform

- MPI_XXXv extends functionality of MPI_XXX by allowing a varying count of data from each process:
  - MPI_Gatherv
  - MPI_Scatterv
  - MPI_Allgatherv
  - MPI_Alltoallv

Fortran

MPI_ALLGATHERV

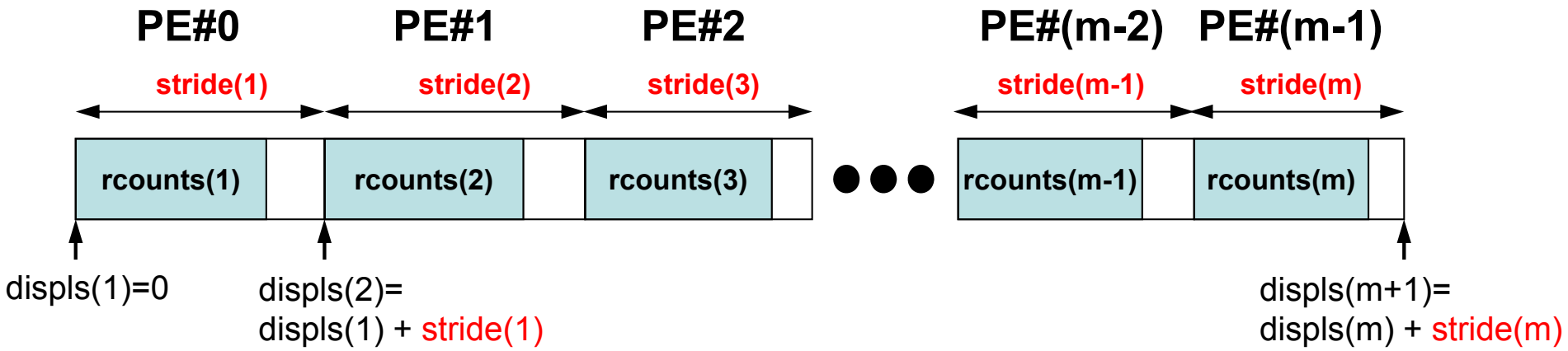
- Variable count version of MPI_Allgather
  - creates “global data” from “local data”

- **`call MPI_ALLGATHERV (sendbuf, scount, sendtype, recvbuf, rcounts, displs, recvtype, comm, ierr)`**
  - **`sendbuf`** choice I starting address of sending buffer
  - **`scount`** I I number of elements sent to each process
  - **`sendtype`** I I data type of elements of sending buffer
  - **`recvbuf`** choice O starting address of receiving buffer
  - **`rcounts`** I I integer array (of length group size) containing the number of elements that are to be received from each process (array: size= PETOT)
  - **`displs`** I I integer array (of length group size). Entry *i* specifies the displacement (relative to recvbuf) at which to place the incoming data from process *i* (array: size= PETOT+1)
  - **`recvtype`** I I data type of elements of receiving buffer
  - **`comm`** I I communicator
  - **`ierr`** I O completion code

MPI_ALLGATHERV (cont.)

Fortran

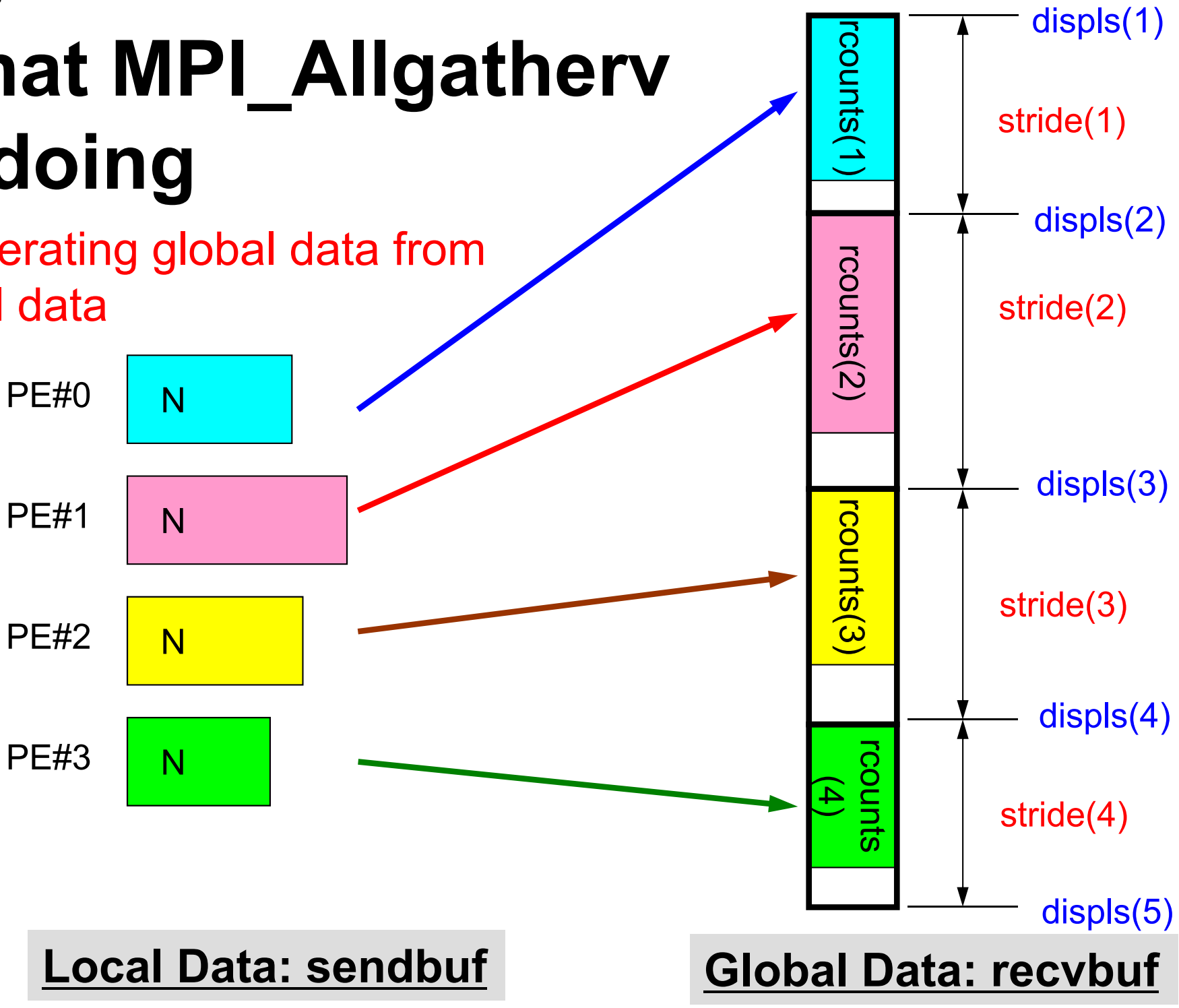
- **`call MPI_ALLGATHERV (sendbuf, scount, sendtype, recvbuf, rcounts, displs, recvtype, comm, ierr)`**
  - **`rcounts`** I I integer array (of length group size) containing the number of elements that are to be received from each process (array: size= PETOT)
  - **`displs`** I I integer array (of length group size). Entry *i* specifies the displacement (relative to recvbuf) at which to place the incoming data from process *i* (array: size= PETOT+1)
  - These two arrays are related to size of final "global data", therefore each process requires information of these arrays (`rcounts, displs`)
    - Each process must have same values for all components of both vectors
  - Usually, **`stride(i)=rcounts(i)`**



size(recvbuf)= displs(PETOT+1)= sum(stride)

What MPI_Allgatherv is doing

Generating global data from local data

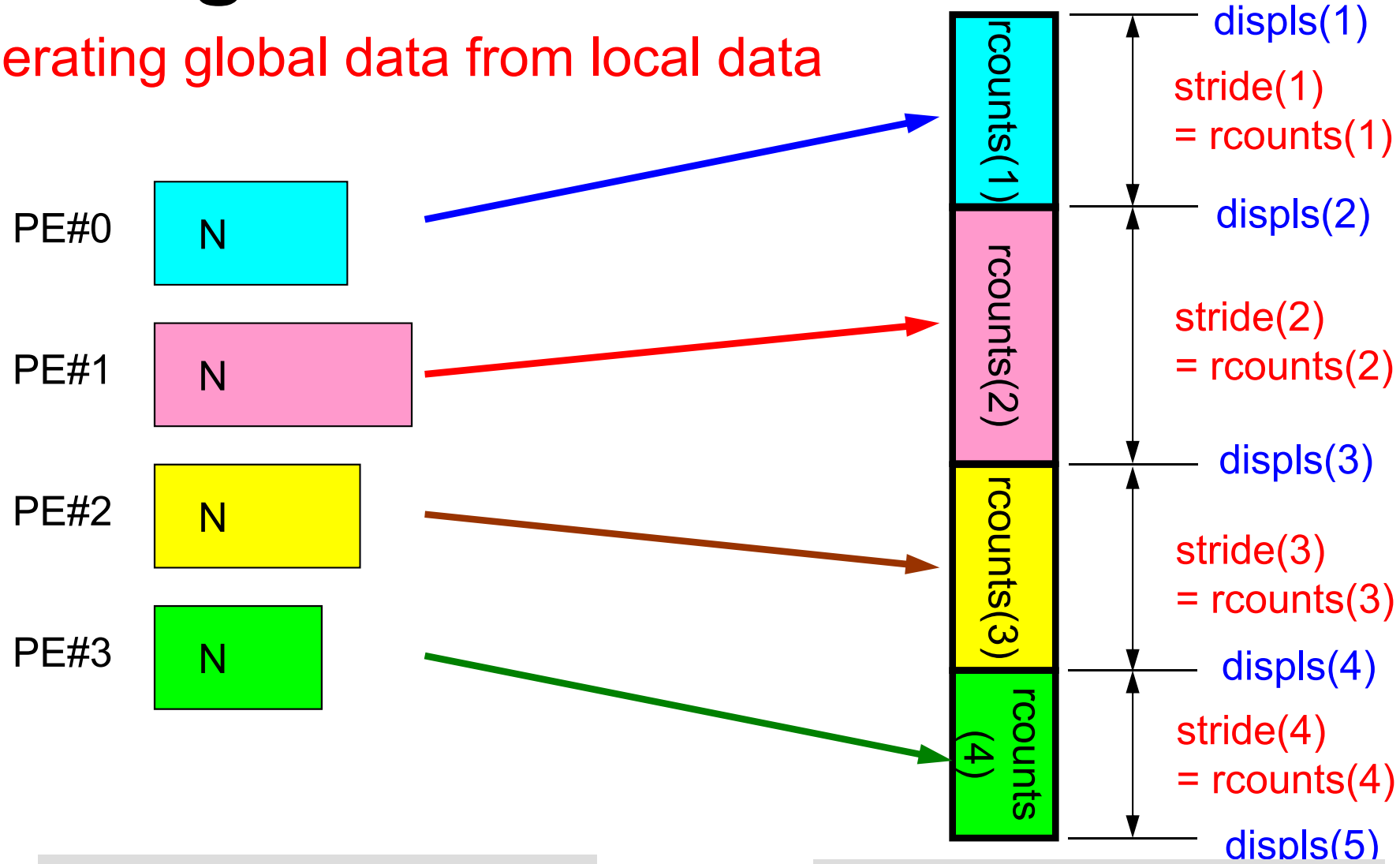


Local Data: sendbuf

Global Data: recvbuf

What MPI_Allgatherv is doing

Generating global data from local data



Local Data: sendbuf

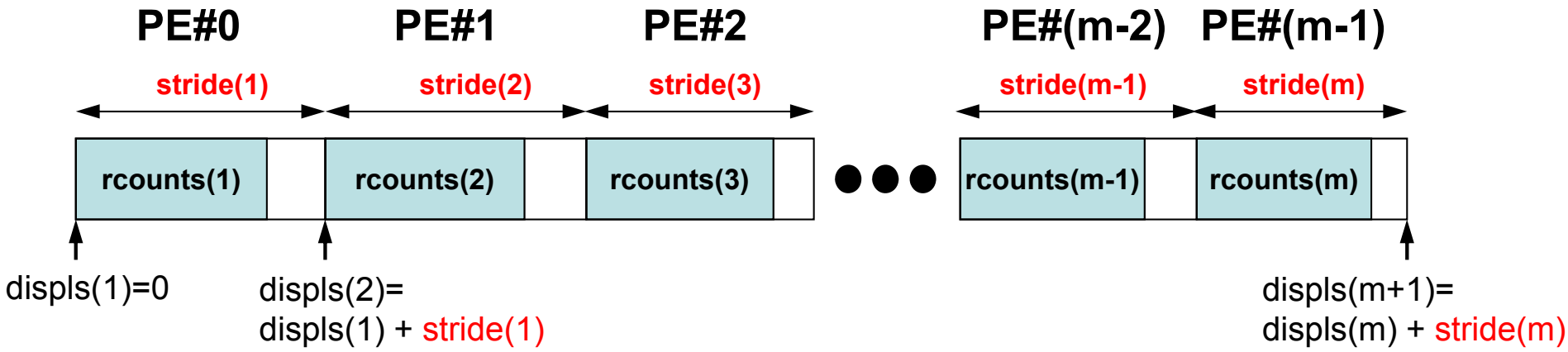
Global Data: recvbuf

MPI_Allgatherv in detail (1/2)

Fortran

- `call MPI_ALLGATHERV (sendbuf, scount, sendtype, recvbuf, rcounts, displs, recvtype, comm, ierr)`

- **`rcounts`**
  - Size of message from each PE: Size of Local Data (Length of Local Vector)
- **`displs`**
  - Address/index of each local data in the vector of global data
  - **`displs(PETOT+1)`**= Size of Entire Global Data (Global Vector)

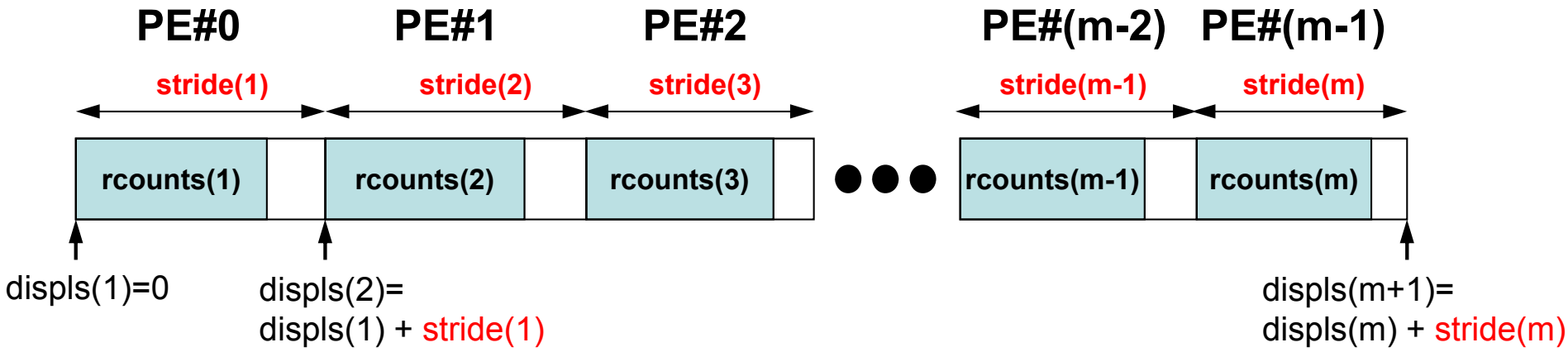


size(recvbuf)= displs(PETOT+1)= sum(stride)

MPI_Allgatherv in detail (2/2)

Fortran

- Each process needs information of **rcounts** & **displs**
  - **"rcounts"** can be created by gathering local vector length **"N"** from each process.
  - On each process, **"displs"** can be generated from **"rcounts"** on each process.
    - **stride[i]= rcounts[i]**
  - Size of **"recvbuf"** is calculated by summation of **"rcounts"**.



size(recvbuf)= displs(PETOT+1)= sum(stride)

Preparation for MPI_Allgatherv <$O-S1>/agv.f

- Generating global vector from “a2.0”~”a2.3”.
- Length of the each vector is 8, 5, 7, and 3, respectively. Therefore, size of final global vector is 23 (= 8+5+7+3).

a2.0~a2.3

PE#0

```
   8
101.0
103.0
105.0
106.0
109.0
111.0
121.0
151.0
```

PE#1

```
   5
201.0
203.0
205.0
206.0
209.0
```

PE#2

```
   7
301.0
303.0
305.0
306.0
311.0
321.0
351.0
```

PE#3

```
   3
401.0
403.0
405.0
```

Preparation: MPI_Allgatherv (1/4)

Fortran

<$O-S1>/agv.f

```
implicit REAL*8 (A-H,O-Z)
include 'mpif.h'

integer :: PETOT, my_rank, SOLVER_COMM, ierr
real(kind=8), dimension(:), allocatable :: VEC
real(kind=8), dimension(:), allocatable :: VEC2
real(kind=8), dimension(:), allocatable :: VECg
integer(kind=4), dimension(:), allocatable :: rcounts
integer(kind=4), dimension(:), allocatable :: displs
character(len=80)                          :: filename

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

if (my_rank.eq.0) filename= 'a2.0'
if (my_rank.eq.1) filename= 'a2.1'
if (my_rank.eq.2) filename= 'a2.2'
if (my_rank.eq.3) filename= 'a2.3'

open (21, file= filename, status= 'unknown')
  read (21,*) N
  allocate (VEC(N))
  do i= 1, N
    read (21,*) VEC(i)
  enddo
```

N(NL) is different at each process

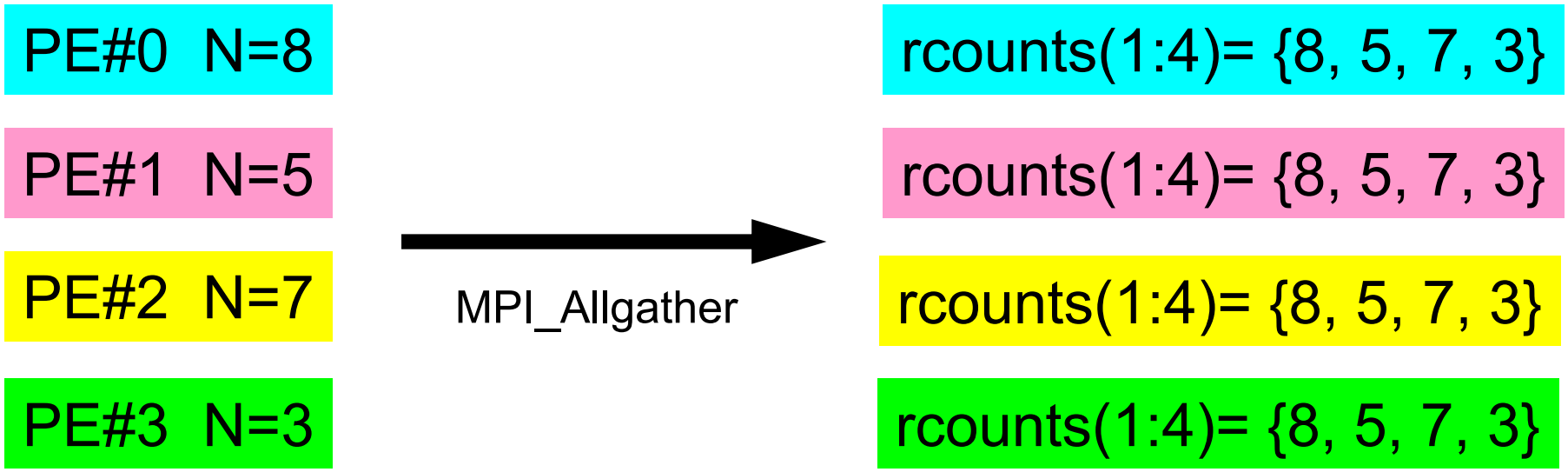
Preparation: MPI_Allgatherv (2/4)

Fortran

<$O-S1>/agv.f

```
 allocate (rcounts(PETOT), displs(PETOT+1))
 rcounts= 0
 write (*,'(a,10i8)') "before", my_rank, N, rcounts

 call MPI_allGATHER ( N     , 1, MPI_INTEGER,                &
&                     rcounts, 1, MPI_INTEGER,                &
&                     MPI_COMM_WORLD, ierr)

 write (*,'(a,10i8)') "after ", my_rank, N, rcounts
 displs(1)= 0
```

Rcounts on each PE



Preparation: MPI_Allgatherv (2/4)

Fortran

<$O-S1>/agv.f

```
 allocate (rcounts(PETOT), displs(PETOT+1))
 rcounts= 0
 write (*,'(a,10i8)') "before", my_rank, N, rcounts

 call MPI_allGATHER ( N     , 1, MPI_INTEGER,          &
&                     rcounts, 1, MPI_INTEGER,          &
&                     MPI_COMM_WORLD, ierr)

 write (*,'(a,10i8)') "after ", my_rank, N, rcounts
 displs(1)= 0

 do ip= 1, PETOT
   displs(ip+1)= displs(ip) + rcounts(ip)
 enddo

 write (*,'(a,10i8)') "displs", my_rank, displs

 call MPI_FINALIZE (ierr)

 stop
 end
```

Rcounts on each PE

Displs on each PE

Preparation: MPI_Allgatherv (3/4)

```
> cd <$O-S1>
> mpifrtpx –Kfast agv.f, mpifccpx –Kfast agv.c

(modify go4.sh for 4 processes)
> pjsub go4.sh

before       0       8       0       0       0       0
after        0       8       8       5       7       3
displs       0       0       8      13      20      23
FORTRAN STOP

before       1       5       0       0       0       0
after        1       5       8       5       7       3
displs       1       0       8      13      20      23
FORTRAN STOP

before       3       3       0       0       0       0
after        3       3       8       5       7       3
displs       3       0       8      13      20      23
FORTRAN STOP

before       2       7       0       0       0       0
after        2       7       8       5       7       3
displs       2       0       8      13      20      23
FORTRAN STOP
```

```
write (*,‘(a,10i8)’) “before”, my_rank, N, rcounts
write (*,'(a,10i8)') "after ", my_rank, N, rcounts
write (*,'(a,10i8)') "displs", my_rank, displs
```

Preparation: MPI_Allgatherv (4/4)

- Only "recvbuf" is not defined yet.
- Size of "recvbuf" = "displs(PETOT+1)"

```
call MPI_allGATHERv
     ( VEC , N, MPI_DOUBLE_PRECISION,
       recvbuf, rcounts, displs, MPI_DOUBLE_PRECISION,
       MPI_COMM_WORLD, ierr)
```

Report S1 (1/2)

- Deadline: 17:00 October 24th (Sat), 2015.
  - Send files via e-mail at **nakajima(at)cc.u-tokyo.ac.jp**

- Problem S1-1
  - Read local files <$O-S1>/a1.0~a1.3, <$O-S1>/a2.0~a2.3.
  - Develop codes which calculate norm ||x|| of global vector for each case.
    - <$O-S1>file.f, <$O-S1>file2.f
- Problem S1-2
  - Read local files <$O-S1>/a2.0~a2.3.
  - Develop a code which constructs “global vector” using MPI_Allgatherv.

Report S1 (2/2)

- Problem S1-3
  - Develop parallel program which calculates the following numerical integration using “trapezoidal rule” by MPI_Reduce, MPI_Bcast etc.
  - Measure computation time, and parallel performance

$$\int_0^1 \frac{4}{1+x^2}\,dx$$

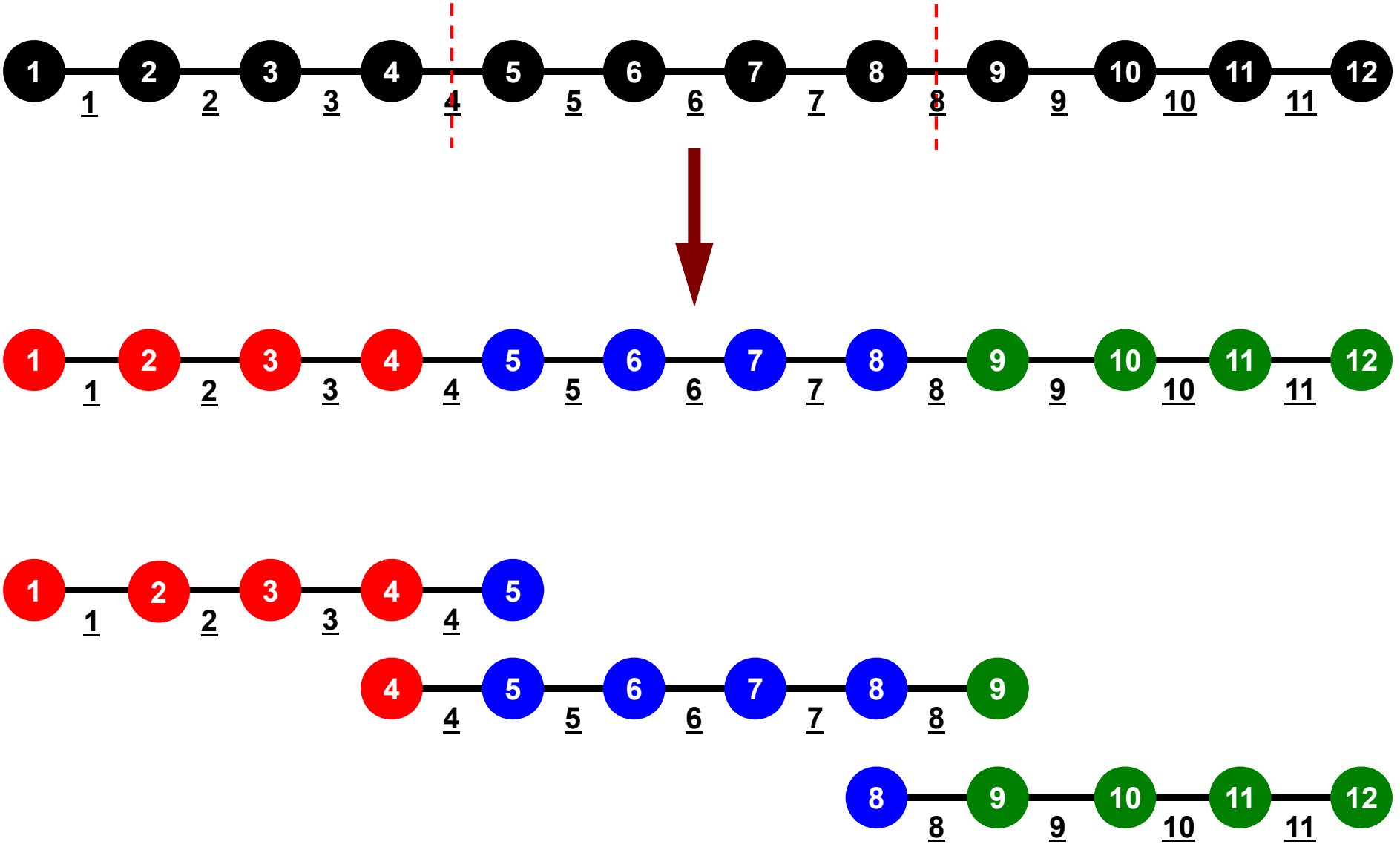
- Report
  - Cover Page: Name, ID, and Problem ID (S1) must be written.
  - Less than two pages including figures and tables (A4) for each of three sub-problems
    - Strategy, Structure of the Program, Remarks
  - Source list of the program (if you have bugs)
  - Output list (as small as possible)

- What is MPI ?
- Your First MPI Program: Hello World
- Global/Local Data
- Collective Communication
- **Peer-to-Peer Communication**

Peer-to-Peer Communication
Point-to-Point Communicatio
1対1通信

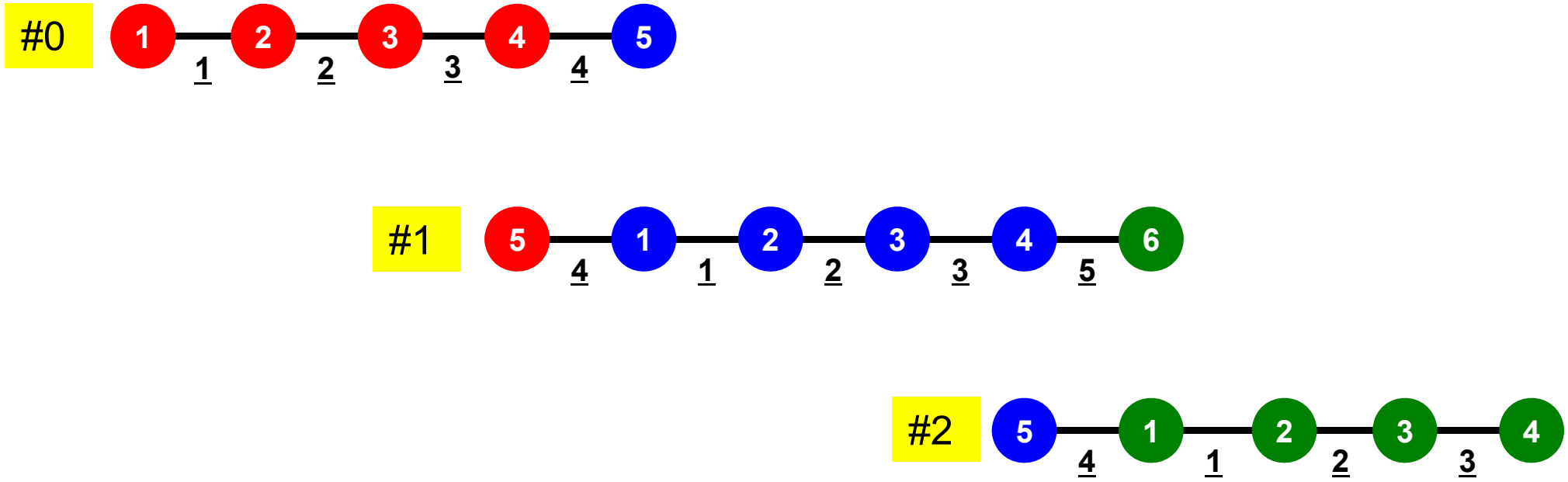
- What is P2P Communication ?
- 2D Problem, Generalized Communication Table
- Report S2

1D FEM: 12 nodes/11 elem's/3 domains



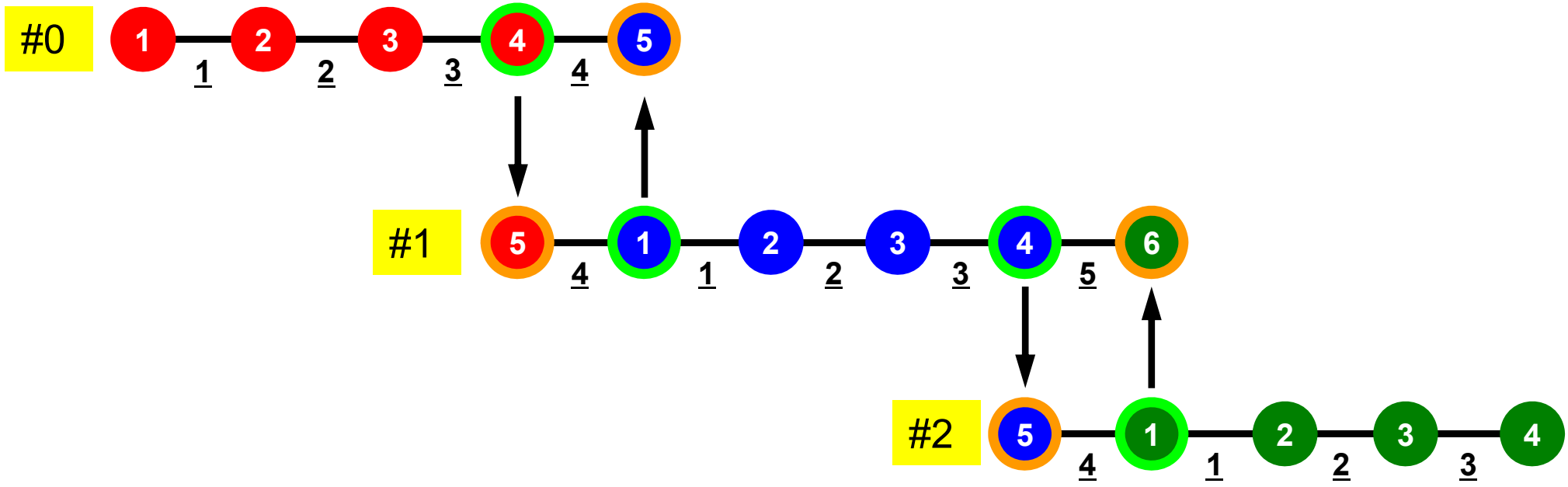
1D FEM: 12 nodes/11 elem's/3 domains

Local ID: Starting from 1 for node and elem at each domain



1D FEM: 12 nodes/11 elem's/3 domains

Internal/External Nodes



Preconditioned Conjugate Gradient Method（CG）

Compute $\mathbf{r^{(0)}= b-[A]x^{(0)}}$
for i= 1, 2, …
  solve $\mathbf{[M]z^{(i-1)}= r^{(i-1)}}$
  $\rho_{i-1}= \mathbf{r^{(i-1)}\ z^{(i-1)}}$
  if i=1
    $p^{(1)}= z^{(0)}$
  else
    $\beta_{i-1}= \rho_{i-1}/\rho_{i-2}$
    $p^{(i)}= z^{(i-1)} + \beta_{i-1}\ p^{(i-1)}$
  endif
  $\mathbf{q^{(i)}= [A]p^{(i)}}$
  $\alpha_i = \rho_{i-1}/\mathbf{p^{(i)}q^{(i)}}$
  $x^{(i)}= x^{(i-1)} + \alpha_i p^{(i)}$
  $r^{(i)}= r^{(i-1)} - \alpha_i q^{(i)}$
  check convergence $\mathbf{|r|}$
end

Preconditioner:

Diagonal Scaling
Point-Jacobi Preconditioning

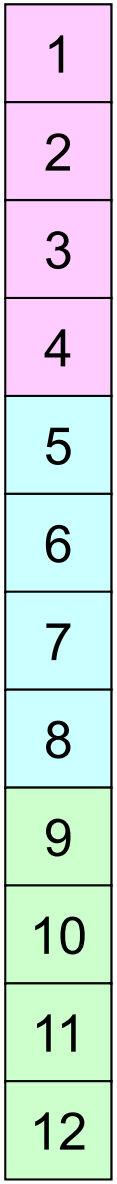
$$[M]=\begin{bmatrix} D_1 & 0 & \dots & 0 & 0 \\ 0 & D_2 & & 0 & 0 \\ \dots & & \dots & & \dots \\ 0 & 0 & & D_{N-1} & 0 \\ 0 & 0 & \dots & 0 & D_N \end{bmatrix}$$

Preconditioning, DAXPY

Local Operations by Only Internal Points: Parallel Processing is possible

```
!C
!C-- {z}= [Minv]{r}

      do i= 1, N
        W(i,Z)= W(i,DD) * W(i,R)
      enddo
```

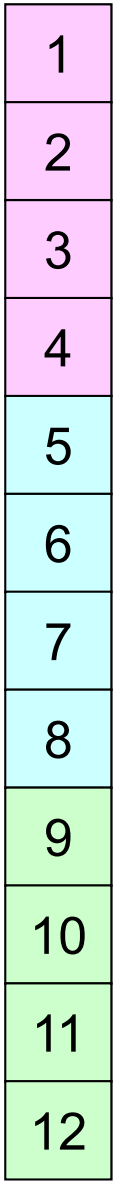
```
!C
!C-- {x}= {x} + ALPHA*{p}        DAXPY: double a{x} plus {y}
!C   {r}= {r} - ALPHA*{q}

      do i= 1, N
        PHI(i)= PHI(i) + ALPHA * W(i,P)
        W(i,R)= W(i,R) - ALPHA * W(i,Q)
      enddo
```



Dot Products

Global Summation needed: Communication ?

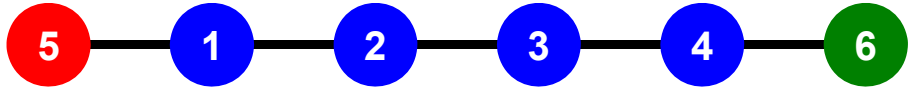
```
!C
!C-- ALPHA= RHO / {p}{q}

      C1= 0.d0
      do i= 1, N
        C1= C1 + W(i,P)*W(i,Q)
      enddo
      ALPHA= RHO / C1
```



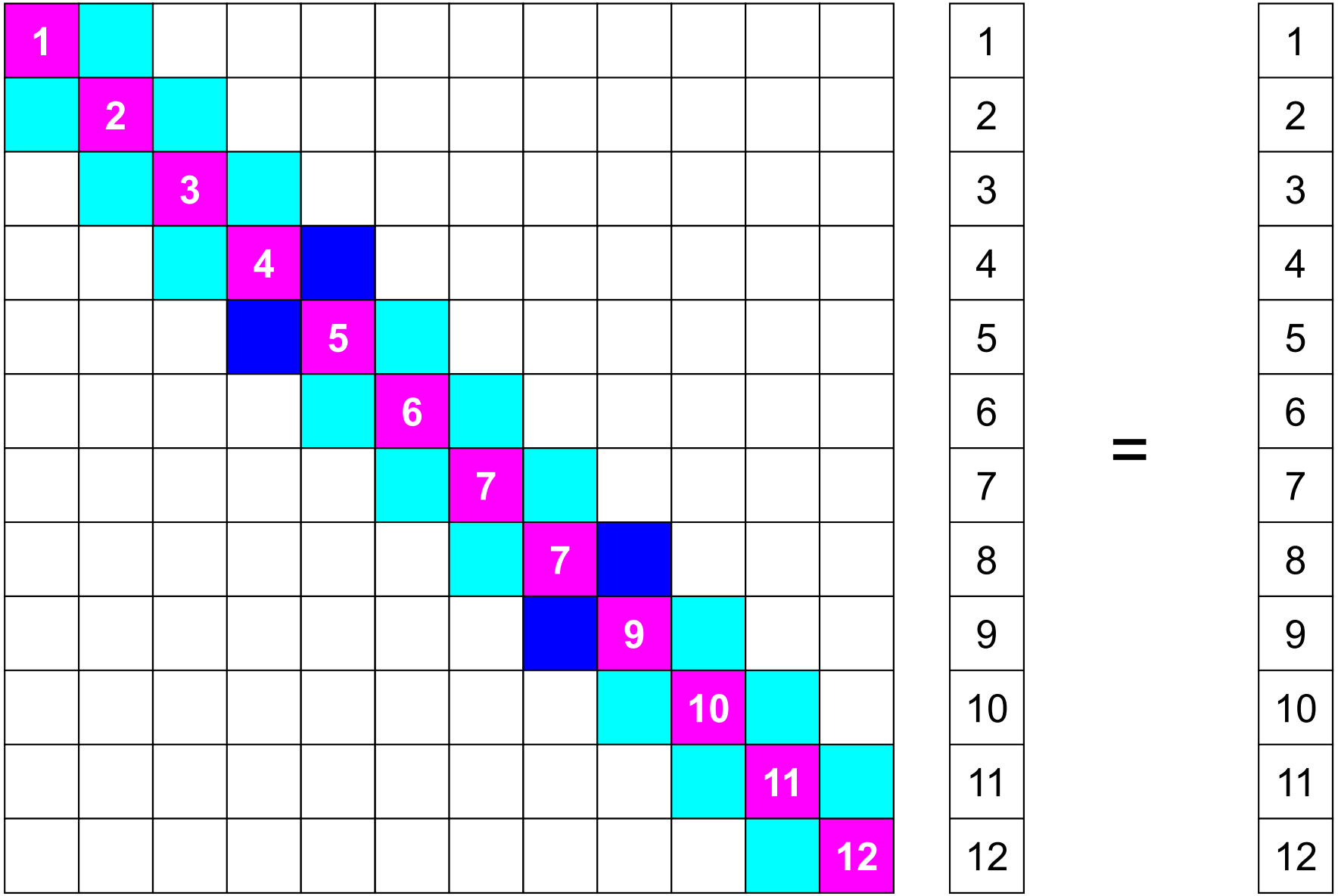
Matrix-Vector Products

Values at External Points: P-to-P Communication

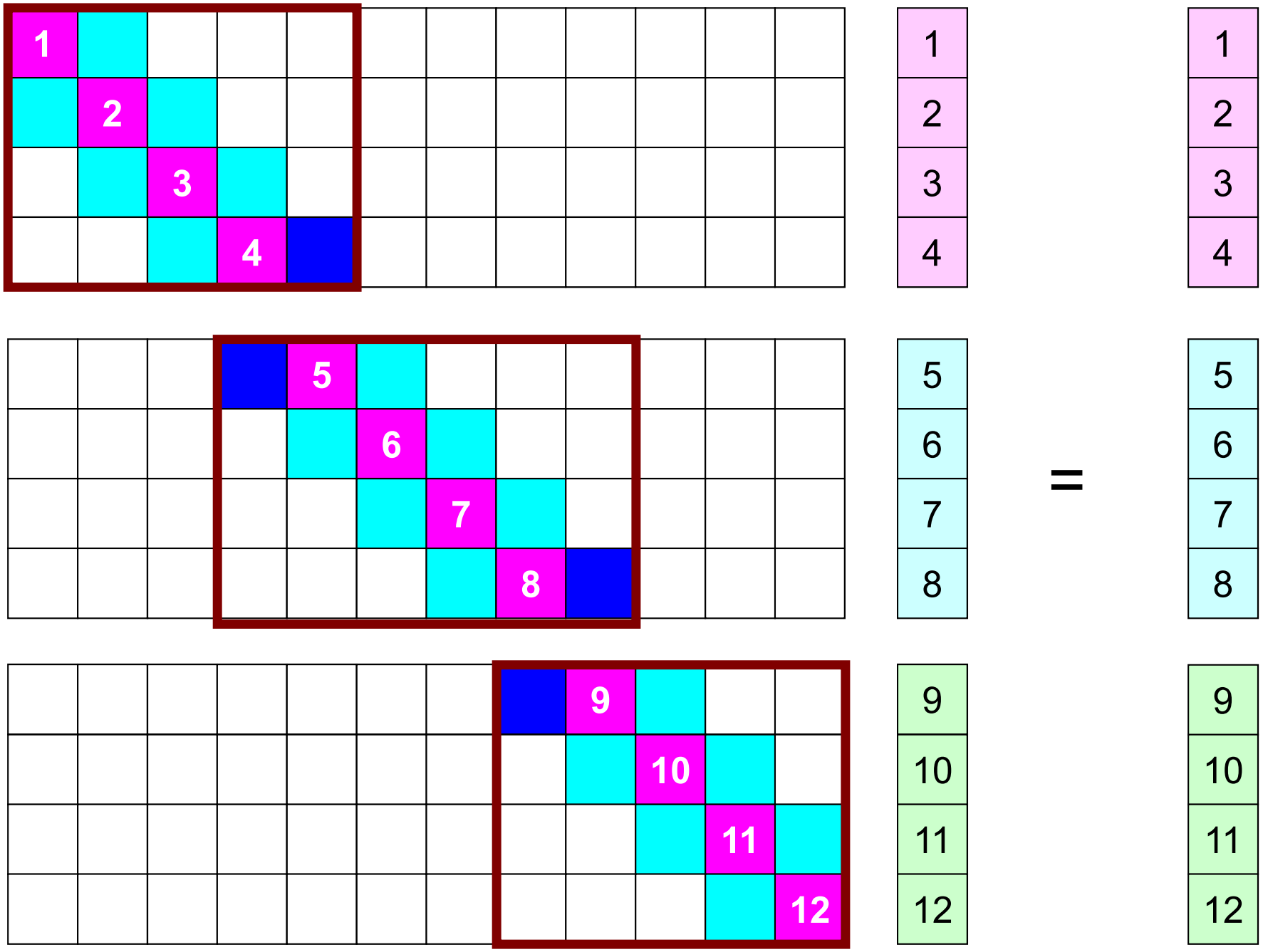
```
!C
!C-- {q}= [A]{p}

      do i= 1, N
        W(i,Q) = DIAG(i)*W(i,P)
        do j= INDEX(i-1)+1, INDEX(i)
          W(i,Q) = W(i,Q) + AMAT(j)*W(ITEM(j),P)
        enddo
      enddo
```



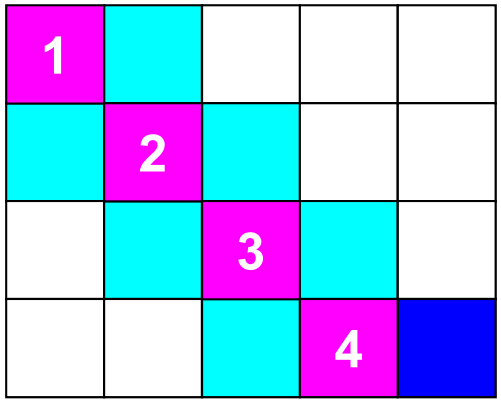
Mat-Vec Products: Local Op. Possible

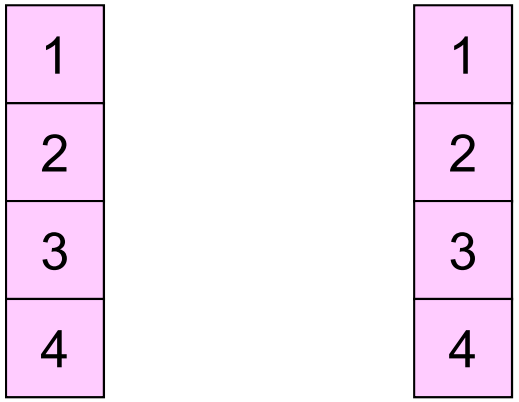


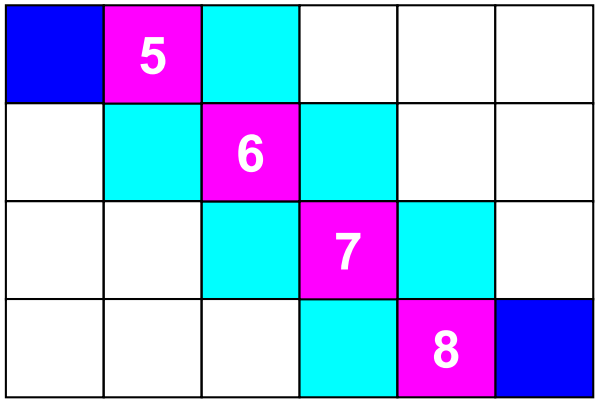
Mat-Vec Products: Local Op. Possible

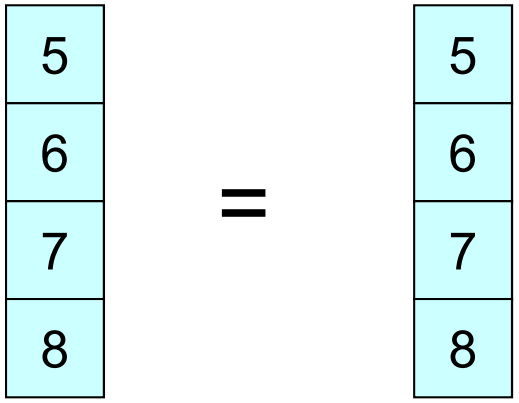


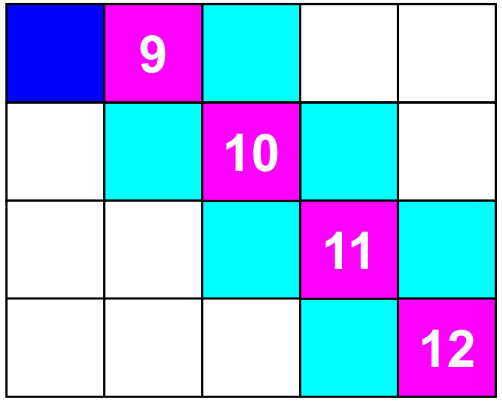
Mat-Vec Products: Local Op. Possible

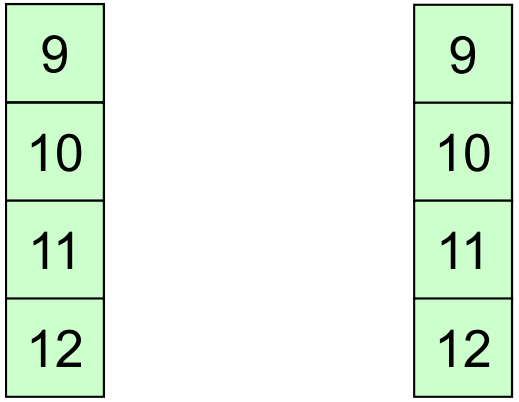




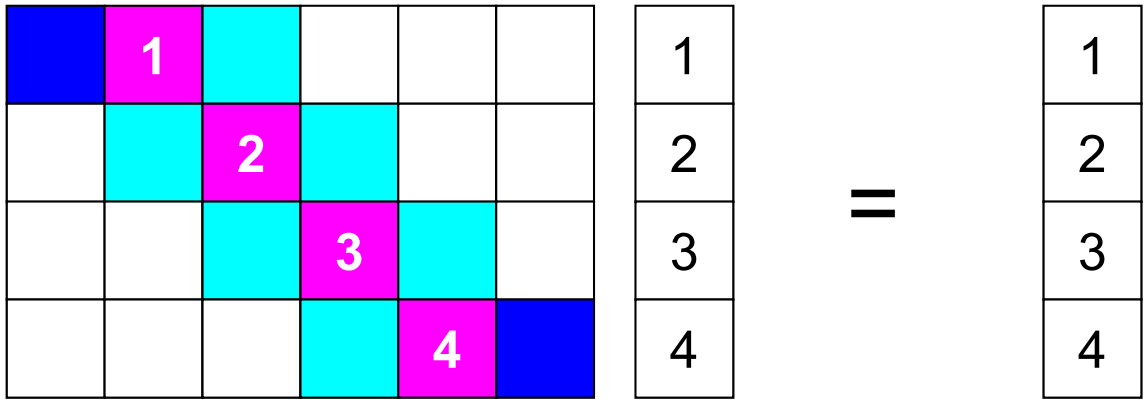


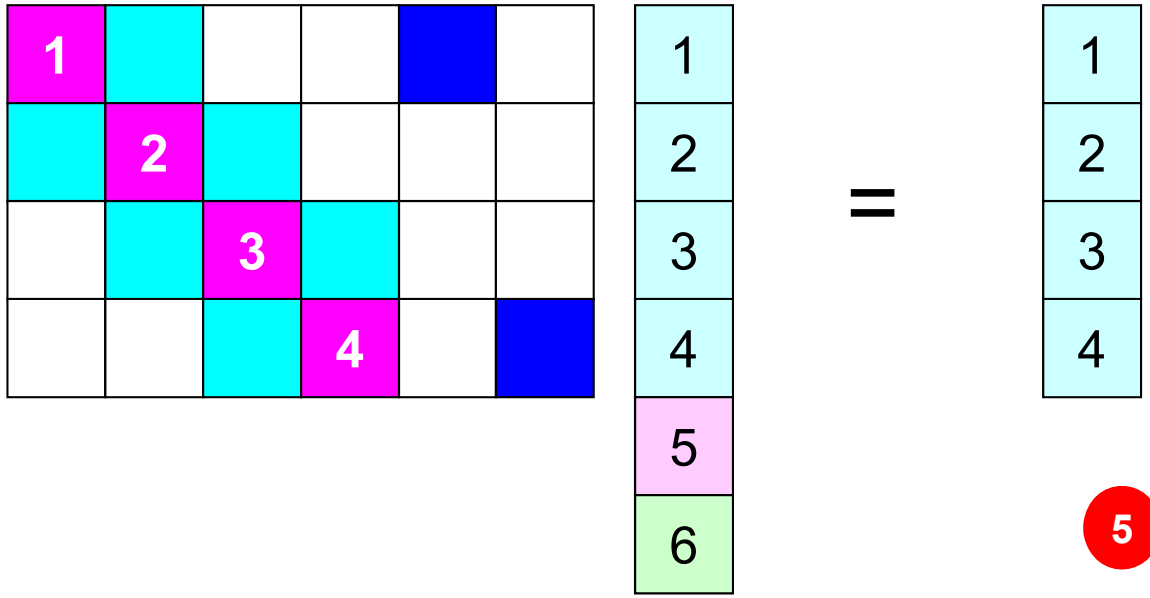


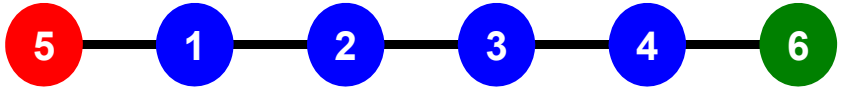




Mat-Vec Products: Local Op. #1



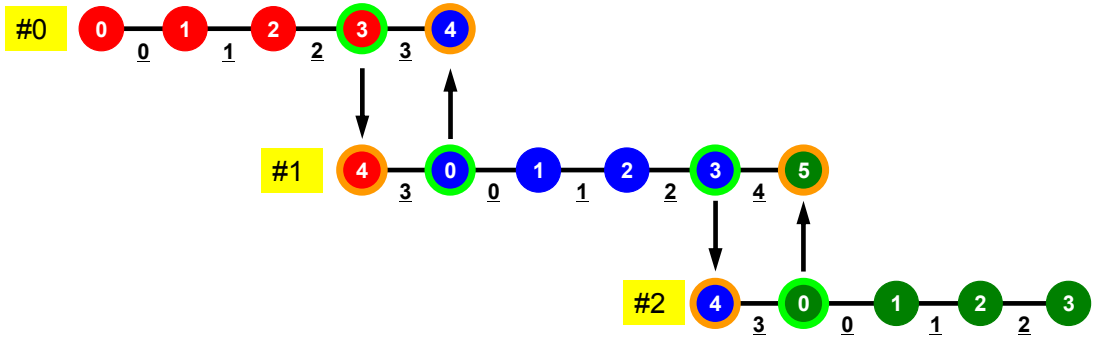




What is Peer-to-Peer Communication ?

- Collective Communication
  - MPI_Reduce, MPI_Scatter/Gather etc.
  - Communications with all processes in the communicator
  - Application Area
    - BEM, Spectral Method, MD: global interactions are considered
    - Dot products, MAX/MIN: Global Summation & Comparison

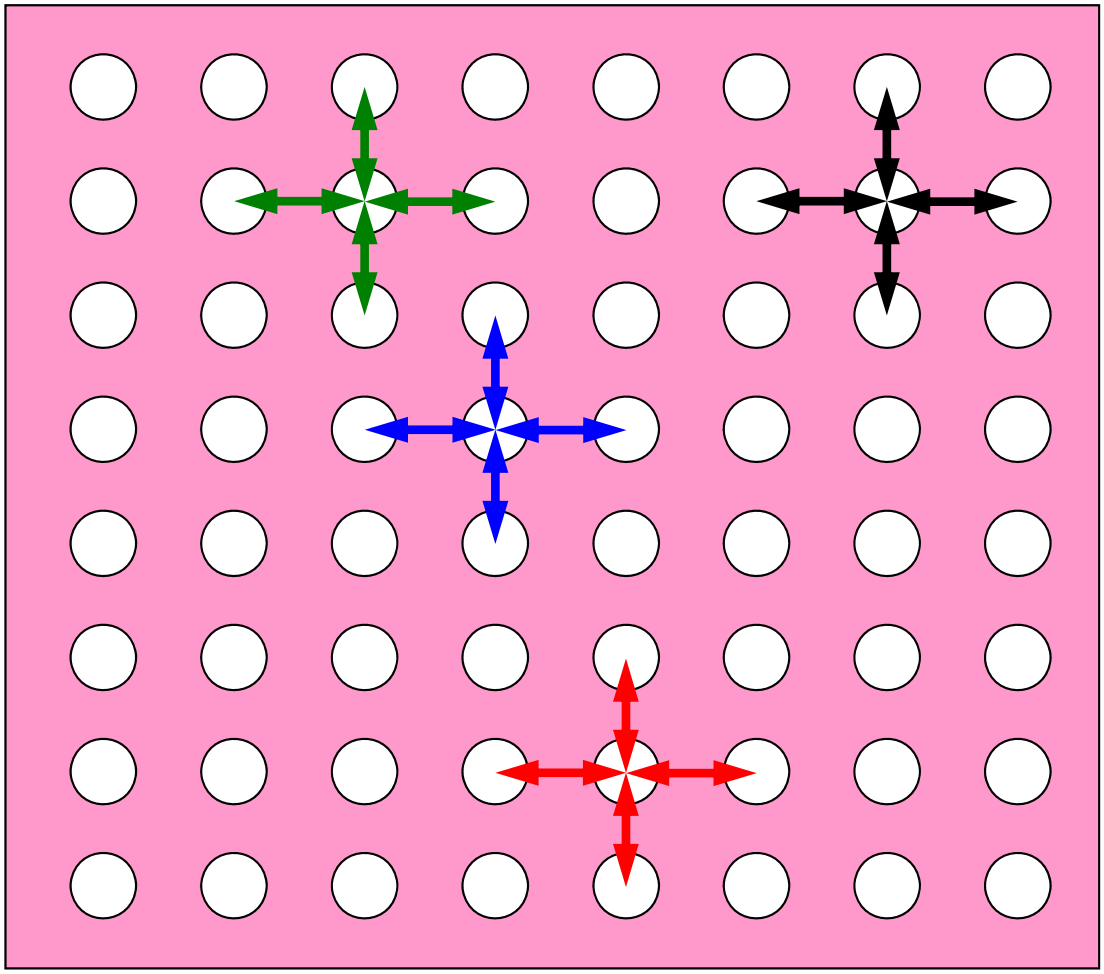
- Peer-toPeer/Point-to-Point
  - MPI_Send, MPI_Receive
  - Communication with limited processes
    - Neighbors
  - Application Area
    - FEM, FDM: Localized Method



Collective/P2P Communications

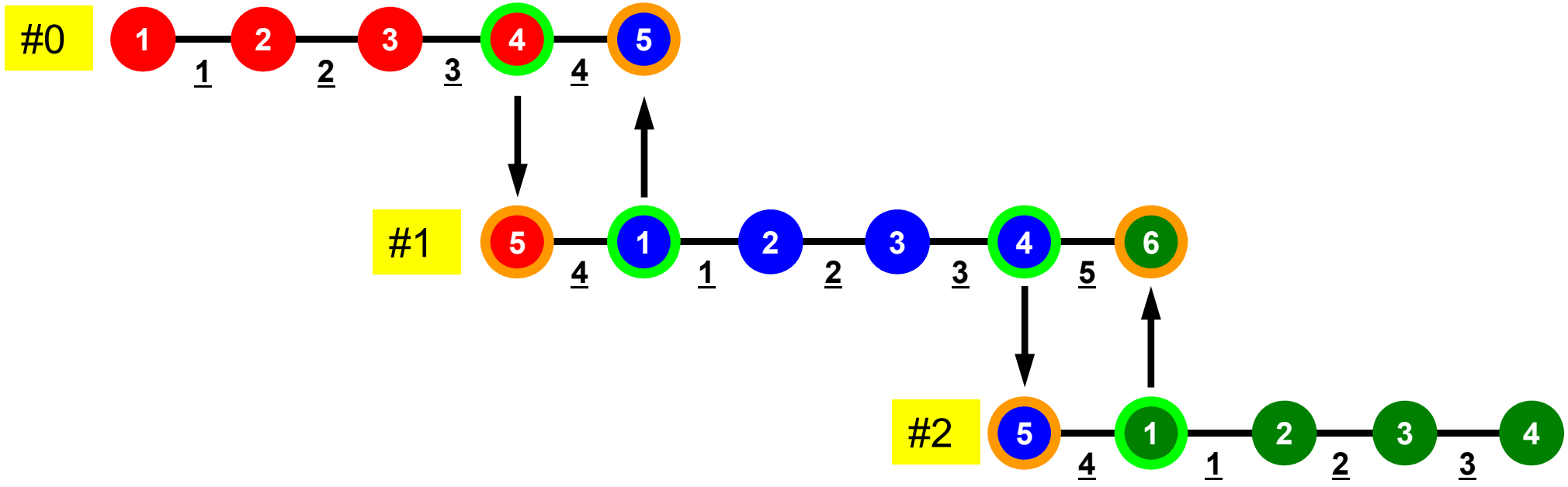
Interactions with only Neighboring Processes/Element

Finite Difference Method (FDM), Finite Element Method (FEM)



When do we need P2P comm.: 1D-FEM

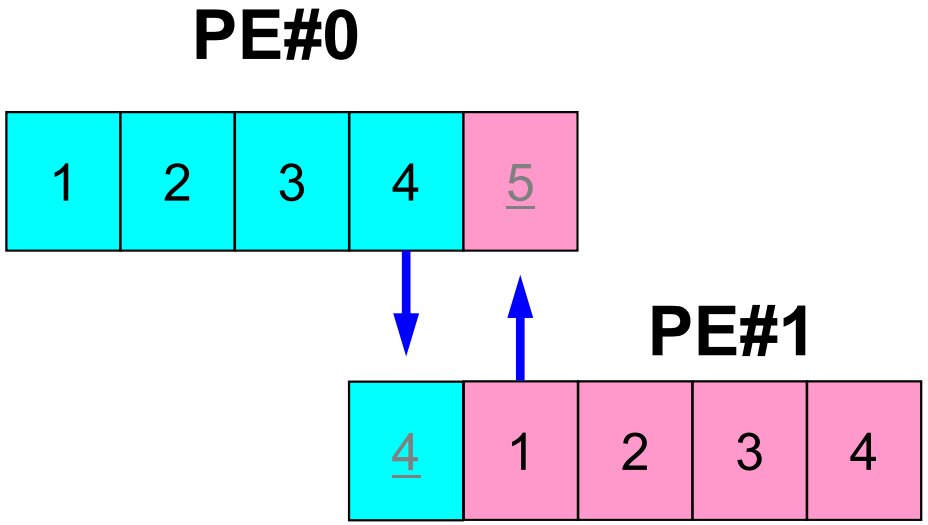
Info in neighboring domains is required for FEM operations
Matrix assembling, Iterative Method



Method for P2P Comm.

- **`MPI_Send`, `MPI_Recv`**
- These are “blocking” functions. “Dead lock” occurs for these “blocking” functions.
- A “blocking” MPI call means that the program execution will be suspended until the message buffer is safe to use.
- The MPI standards specify that a blocking SEND or RECV does not return until the send buffer is safe to reuse (for MPI_Send), or the receive buffer is ready to use (for MPI_Recv).
  - Blocking comm. confirms “secure” communication, but it is very inconvenient.
- Please just remember that “there are such functions”.

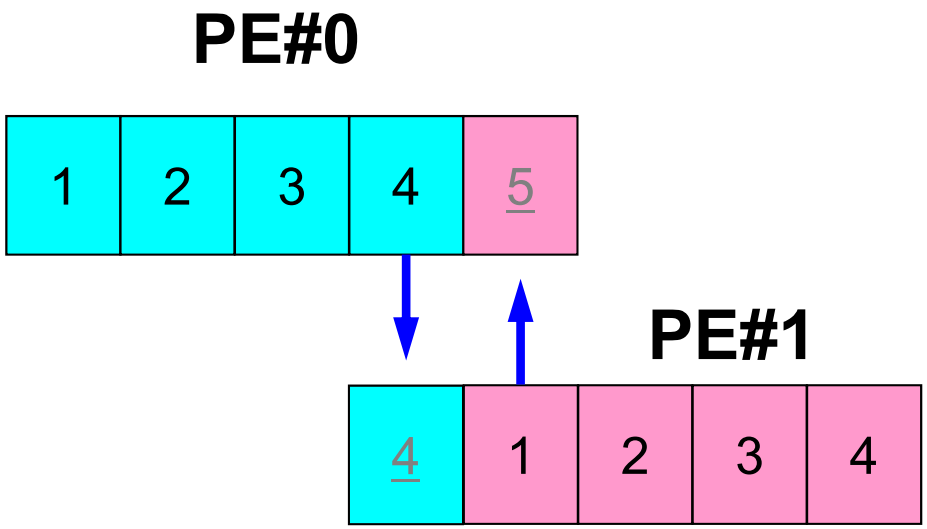
MPI_Send/MPI_Recv




```
if (my_rank.eq.0) NEIB_ID=1
if (my_rank.eq.1) NEIB_ID=0

…
call MPI_SEND (NEIB_ID, arg's)
call MPI_RECV (NEIB_ID, arg's)
…
```

- This seems reasonable, but it stops at MPI_Send/MPI_Recv.
  - Sometimes it works (according to implementation).

MPI_Send/MPI_Recv (cont.)

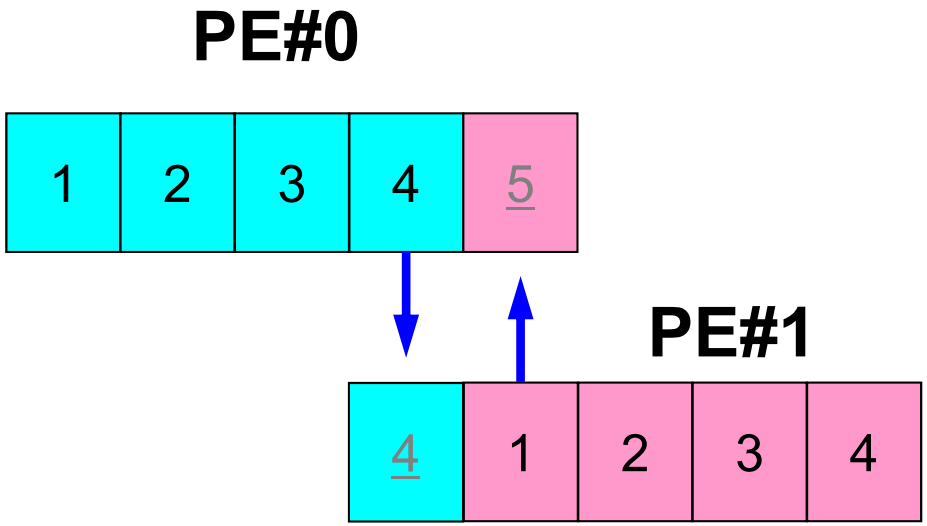



```
if (my_rank.eq.0) NEIB_ID=1
if (my_rank.eq.1) NEIB_ID=0

…
if (my_rank.eq.0) then
  call MPI_SEND (NEIB_ID, arg's)
  call MPI_RECV (NEIB_ID, arg's)
endif

if (my_rank.eq.1) then
  call MPI_RECV (NEIB_ID, arg's)
  call MPI_SEND (NEIB_ID, arg's)
endif

…
```

- It works ... but

How to do P2P Comm. ?

- Using “non-blocking” functions **MPI_Isend** & **MPI_Irecv** together with **MPI_Waitall** for synchronization
- **MPI_Sendrecv** is also available.




```
if (my_rank.eq.0) NEIB_ID=1
if (my_rank.eq.1) NEIB_ID=0

…
call MPI_Isend (NEIB_ID, arg’s)
call MPI_Irecv (NEIB_ID, arg’s)
…
call MPI_Waitall (for Irecv)
…
call MPI_Waitall (for Isend)
```

MPI_Waitall for both of **MPI_Isend/MPI_Irecv** is possible

Fortran

MPI_ISEND

- Begins a non-blocking send
  - Send the contents of sending buffer (starting from **sendbuf**, number of messages: **count**) to **dest** with **tag** .
  - Contents of sending buffer cannot be modified before calling corresponding **MPI_Waitall**.

- **call MPI_ISEND (sendbuf,count,datatype,dest,tag,comm,request, ierr)**
  - **sendbuf** choice I starting address of sending buffer
  - **count** I I number of elements sent to each process
  - **datatype** I I data type of elements of sending buffer
  - **dest** I I rank of destination
  - **tag** I I message tag
    This integer can be used by the application to distinguish messages. Communication occurs if `tag's` of `MPI_Isend` and `MPI_Irecv` are matched. Usually tag is set to be "0" (in this class),
  - **comm** I I communicator
  - **request** I O communication request array used in `MPI_Waitall`
  - **ierr** I O completion code

Communication Request: request 通信識別子

- **`call MPI_ISEND (sendbuf,count,datatype,dest,tag,comm,request, ierr)`**
  - **`sendbuf`** choice I — starting address of sending buffer
  - **`count`** I I — number of elements sent to each process
  - **`datatype`** I I — data type of elements of sending buffer
  - **`dest`** I I — rank of destination
  - **`tag`** I I — message tag
    This integer can be used by the application to distinguish messages. Communication occurs if `tag's` of `MPI_Isend` and `MPI_Irecv` are matched.
    Usually tag is set to be "0" (in this class),
  - **`comm`** I I — communicator
  - **`request`** I O — communication request used in `MPI_Waitall`
    Size of the array is total number of neighboring processes
  - **`ierr`** I O — completion code

- Just define the array

```
allocate (request(NEIBPETOT))
```

Fortran

Fortran

MPI_IRECV

- Begins a non-blocking receive
  - Receiving the contents of receiving buffer (starting from **`recvbuf`**, number of messages: **`count`**) from **`source`** with **`tag`** .
  - Contents of receiving buffer cannot be used before calling corresponding **`MPI_Waitall`**.

- **`call MPI_IRECV (recvbuf,count,datatype,dest,tag,comm,request, ierr)`**

`recvbuf`	choice	I	starting address of receiving buffer
`count`	I	I	number of elements in receiving buffer
`datatype`	I	I	data type of elements of receiving buffer
`source`	I	I	rank of source
`tag`	I	I	message tag This integer can be used by the application to distinguish messages. Communication occurs if `tag's` of `MPI_Isend` and `MPI_Irecv` are matched. Usually tag is set to be "0" (in this class),
`comm`	I	I	communicator
`request`	I	O	communication request used in `MPI_Waitall`
`ierr`	I	O	completion code

MPI_WAITALL

Fortran

- **MPI_Waitall** blocks until all comm's, associated with **request** in the array, complete. It is used for synchronizing **MPI_Isend** and **MPI_Irecv** in this class.
- At sending phase, contents of sending buffer cannot be modified before calling corresponding **MPI_Waitall**. At receiving phase, contents of receiving buffer cannot be used before calling corresponding **MPI_Waitall**.
- **MPI_Isend** and **MPI_Irecv** can be synchronized simultaneously with a single **MPI_Waitall** if it is consitent.
  - Same **request** should be used in **MPI_Isend** and **MPI_Irecv**.
- Its operation is similar to that of **MPI_Barrier** but, **MPI_Waitall** can not be replaced by **MPI_Barrier**.
  - Possible troubles using **MPI_Barrier** instead of **MPI_Waitall**: Contents of **request** and **status** are not updated properly, very slow operations etc.

- **call MPI_WAITALL (count,request,status,ierr)**
  - **count** I I number of processes to be synchronized
  - **request** I I/O comm. request used in MPI_Waitall (array size: count)
  - **status** I O array of status objects
    MPI_STATUS_SIZE: defined in 'mpif.h', 'mpi.h'
  - **ierr** I O completion code

Array of status object：status
状況オブジェクト配列

- **`call MPI_WAITALL (count,request,status,ierr)`**
  - **`count`** I I number of processes to be synchronized
  - **`request`** I I/O comm. request used in `MPI_Waitall` (array size: `count`)
  - **`status`** I O array of status objects
    `MPI_STATUS_SIZE: defined in 'mpif.h', 'mpi.h'`
  - **`ierr`** I O completion code

- Just define the array

```
allocate (stat(MPI_STATUS_SIZE,NEIBPETOT))
```

Fortran

Fortran

MPI_SENDRECV

- MPI_Send+MPI_Recv: not recommended, many restrictions

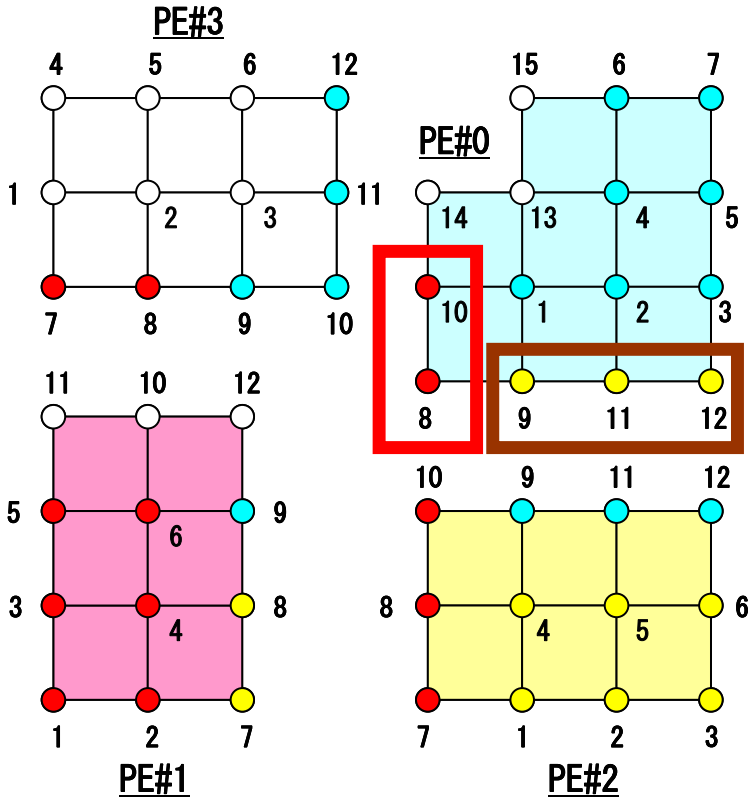
- **`call MPI_SENDRECV`**
  `(sendbuf,sendcount,sendtype,dest,sendtag,recvbuf,`
  `recvcount,recvtype,source,recvtag,comm,status,ierr)`

–	**`sendbuf`**	choice	I	starting address of sending buffer
–	**`sendcount`**	I	I	number of elements in sending buffer
–	**`sendtype`**	I	I	datatype of each sending buffer element
–	**`dest`**	I	I	rank of destination
–	**`sendtag`**	I	I	message tag for sending
–	**`comm`**	I	I	communicator
–	**`recvbuf`**	choice	I	starting address of receiving buffer
–	**`recvcount`**	I	I	number of elements in receiving buffer
–	**`recvtype`**	I	I	datatype of each receiving buffer element
–	**`source`**	I	I	rank of source
–	**`recvtag`**	I	I	message tag for receiving
–	**`comm`**	I	I	communicator
–	**`status`**	I	O	array of status objects `MPI_STATUS_SIZE: defined in 'mpif.h', 'mpi.h'`
–	**`ierr`**	I	O	completion code

RECV: receiving to external nodes

Recv. continuous data to recv. buffer from neighbors

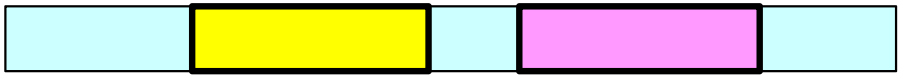
- **`MPI_Irecv`**
  `(recvbuf,count,datatype,dest,tag,comm,request)`
  - **`recvbuf`** choice I starting address of receiving buffer
  - **`count`** I I number of elements in receiving buffer
  - **`datatype`** I I data type of elements of receiving buffer
  - **`source`** I I rank of source

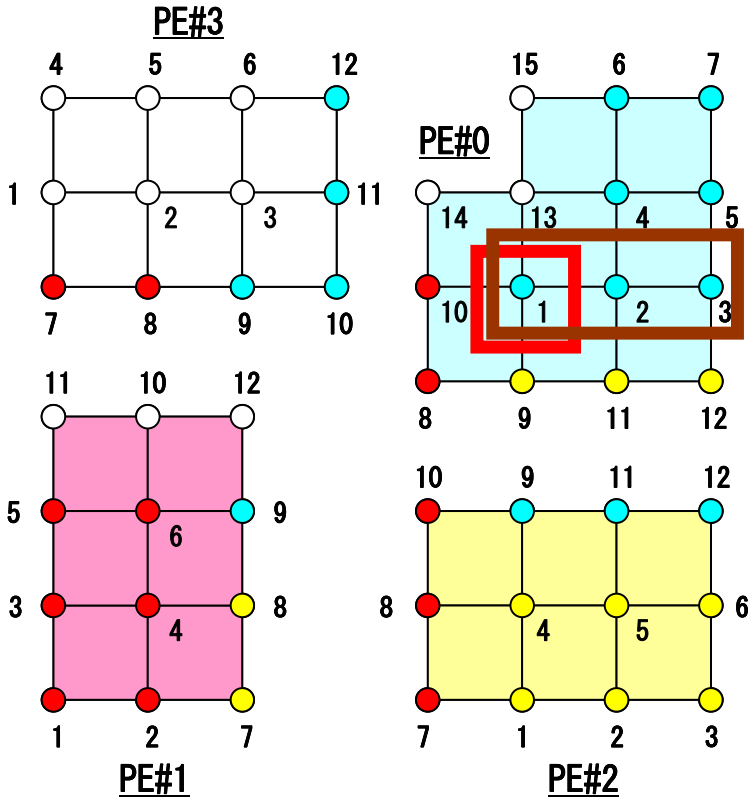


SEND: sending from boundary nodes

Send continuous data to send buffer of neighbors

- **`MPI_Isend (sendbuf,count,datatype,dest,tag,comm,request)`**
  - **`sendbuf`** choice I starting address of sending buffer
  - **`count`** I I number of elements sent to each process
  - **`datatype`** I I data type of elements of sending buffer
  - **`dest`** I I rank of destination





Request, Status in Fortran

- **MPI_Isend: request**
- **MPI_Irecv: request**
- **MPI_Waitall: request, status**

```
integer request(NEIBPETOT)
integer status (MPI_STAUTS_SIZE,NEIBPETOT)
```

- **MPI_Sendrecv: status**

```
integer status (MPI_STATUS_SIZE)
```

Files on Oakleaf-FX

Fotran

```
>$ cd <$O-TOP>
>$ cp /home/z30088/class_eps/F/s2-f.tar .
>$ tar xvf s2-f.tar
```

C

```
>$ cd <$O-TOP>
>$ cp /home/z30088/class_eps/C/s2-c.tar .
>$ tar xvf s2-c.tar
```

Confirm Directory

```
>$ ls
   mpi

>$ cd mpi/S2
```

This directory is called as <$O-S2> in this course.

<$O-S2> = <$O-TOP>/mpi/S2

Ex.1: Send-Recv a Scalar

- Exchange VAL (real, 8-byte) between PE#0 & PE#1

```
if (my_rank.eq.0) NEIB= 1
if (my_rank.eq.1) NEIB= 0

call MPI_Isend (VAL    ,1,MPI_DOUBLE_PRECISION,NEIB,…,req_send,…)
call MPI_Irecv (VALtemp,1,MPI_DOUBLE_PRECISION,NEIB,…,req_recv,…)
call MPI_Waitall (…,req_recv,stat_recv,…) Recv.buf VALtemp can be used
call MPI_Waitall (…,req_send,stat_send,…) Send buf VAL can be modified
VAL= VALtemp
```

```
if (my_rank.eq.0) NEIB= 1
if (my_rank.eq.1) NEIB= 0

call MPI_Sendrecv (VAL    ,1,MPI_DOUBLE_PRECISION,NEIB,…              &
                   VALtemp,1,MPI_DOUBLE_PRECISION,NEIB,…, status,…)
VAL= VALtemp
```

Name of recv. buffer could be "VAL", but not recommended.

Ex.1: Send-Recv a Scalar

Isend/Irecv/Waitall

```
$> cd <$O-S2>
$> mpifrtpx -Kfast ex1-1.f
$> pjsub go2.sh
```

```
implicit REAL*8 (A-H,O-Z)
include  'mpif.h'
integer(kind=4) :: my_rank, PETOT, NEIB
real   (kind=8) :: VAL, VALtemp
integer(kind=4), dimension(MPI_STATUS_SIZE,1) :: stat_send, stat_recv
integer(kind=4), dimension(1)                 :: request_send, request_recv

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

if (my_rank.eq.0) then
  NEIB= 1
  VAL = 10.d0
 else
  NEIB= 0
  VAL = 11.d0
endif

call MPI_ISEND (VAL, 1,MPI_DOUBLE_PRECISION,NEIB,0,MPI_COMM_WORLD,request_send(1),ierr)
call MPI_IRECV (VALx,1,MPI_DOUBLE_PRECISION,NEIB,0,MPI_COMM_WORLD,request_recv(1),ierr)
call MPI_WAITALL (1, request_recv, stat_recv, ierr)
call MPI_WAITALL (1, request_send, stat_send, ierr)
VAL= VALx

call MPI_FINALIZE (ierr)
end
```

Ex.1: Send-Recv a Scalar

SendRecv

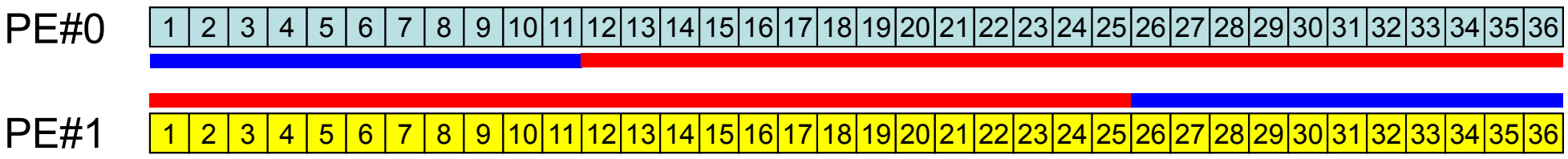
```
$> cd <$O-S2>
$> mpifrtpx –Kfast ex1-2.f
$> pjsub go2.sh
```

```
implicit REAL*8 (A-H,O-Z)
include  'mpif.h'
integer(kind=4) :: my_rank, PETOT, NEIB
real   (kind=8) :: VAL, VALtemp
integer(kind=4) :: status(MPI_STATUS_SIZE)

call MPI_INIT      (ierr)
call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )

if (my_rank.eq.0) then
  NEIB= 1
  VAL = 10.d0
endif
if (my_rank.eq.1) then
  NEIB= 0
  VAL = 11.d0
endif

call MPI_SENDRECV                                                    &
    & (VAL    , 1, MPI_DOUBLE_PRECISION, NEIB, 0,                    &
    &  VALtemp, 1, MPI_DOUBLE_PRECISION, NEIB, 0, MPI_COMM_WORLD, status, ierr)

VAL= VALtemp
call MPI_FINALIZE (ierr)
end
```

Ex.2: Send-Recv an Array (1/4)

- Exchange VEC (real, 8-byte) between PE#0 & PE#1
- PE#0 to PE#1
  - PE#0: send VEC(1)-VEC(11) (length=11)
  - PE#1: recv. as VEC(26)-VEC(36) (length=11)
- PE#1 to PE#0
  - PE#1: send VEC(1)-VEC(25) (length=25)
  - PE#0: recv. as VEC(12)-VEC(36) (length=25)

- Practice: Develop a program for this operation.



t1

Practice: t1

- Initial status of VEC(:):
  - PE#0 VEC(1-36)= 101,102,103,~,135,136
  - PE#1 VEC(1-36)= 201,202,203,~,235,236
- Confirm the results in the next page
- Using following two functions:
  - MPI_Isend/Irecv/Waitall
  - MPI_Sendrecv

Estimated Results

t1

```
0 #BEFORE#  1      101.
0 #BEFORE#  2      102.
0 #BEFORE#  3      103.
0 #BEFORE#  4      104.
0 #BEFORE#  5      105.
0 #BEFORE#  6      106.
0 #BEFORE#  7      107.
0 #BEFORE#  8      108.
0 #BEFORE#  9      109.
0 #BEFORE# 10      110.
0 #BEFORE# 11      111.
0 #BEFORE# 12      112.
0 #BEFORE# 13      113.
0 #BEFORE# 14      114.
0 #BEFORE# 15      115.
0 #BEFORE# 16      116.
0 #BEFORE# 17      117.
0 #BEFORE# 18      118.
0 #BEFORE# 19      119.
0 #BEFORE# 20      120.
0 #BEFORE# 21      121.
0 #BEFORE# 22      122.
0 #BEFORE# 23      123.
0 #BEFORE# 24      124.
0 #BEFORE# 25      125.
0 #BEFORE# 26      126.
0 #BEFORE# 27      127.
0 #BEFORE# 28      128.
0 #BEFORE# 29      129.
0 #BEFORE# 30      130.
0 #BEFORE# 31      131.
0 #BEFORE# 32      132.
0 #BEFORE# 33      133.
0 #BEFORE# 34      134.
0 #BEFORE# 35      135.
0 #BEFORE# 36      136.
```

```
0 #AFTER #  1      101.
0 #AFTER #  2      102.
0 #AFTER #  3      103.
0 #AFTER #  4      104.
0 #AFTER #  5      105.
0 #AFTER #  6      106.
0 #AFTER #  7      107.
0 #AFTER #  8      108.
0 #AFTER #  9      109.
0 #AFTER # 10      110.
0 #AFTER # 11      111.
0 #AFTER # 12      201.
0 #AFTER # 13      202.
0 #AFTER # 14      203.
0 #AFTER # 15      204.
0 #AFTER # 16      205.
0 #AFTER # 17      206.
0 #AFTER # 18      207.
0 #AFTER # 19      208.
0 #AFTER # 20      209.
0 #AFTER # 21      210.
0 #AFTER # 22      211.
0 #AFTER # 23      212.
0 #AFTER # 24      213.
0 #AFTER # 25      214.
0 #AFTER # 26      215.
0 #AFTER # 27      216.
0 #AFTER # 28      217.
0 #AFTER # 29      218.
0 #AFTER # 30      219.
0 #AFTER # 31      220.
0 #AFTER # 32      221.
0 #AFTER # 33      222.
0 #AFTER # 34      223.
0 #AFTER # 35      224.
0 #AFTER # 36      225.
```

```
1 #BEFORE#  1      201.
1 #BEFORE#  2      202.
1 #BEFORE#  3      203.
1 #BEFORE#  4      204.
1 #BEFORE#  5      205.
1 #BEFORE#  6      206.
1 #BEFORE#  7      207.
1 #BEFORE#  8      208.
1 #BEFORE#  9      209.
1 #BEFORE# 10      210.
1 #BEFORE# 11      211.
1 #BEFORE# 12      212.
1 #BEFORE# 13      213.
1 #BEFORE# 14      214.
1 #BEFORE# 15      215.
1 #BEFORE# 16      216.
1 #BEFORE# 17      217.
1 #BEFORE# 18      218.
1 #BEFORE# 19      219.
1 #BEFORE# 20      220.
1 #BEFORE# 21      221.
1 #BEFORE# 22      222.
1 #BEFORE# 23      223.
1 #BEFORE# 24      224.
1 #BEFORE# 25      225.
1 #BEFORE# 26      226.
1 #BEFORE# 27      227.
1 #BEFORE# 28      228.
1 #BEFORE# 29      229.
1 #BEFORE# 30      230.
1 #BEFORE# 31      231.
1 #BEFORE# 32      232.
1 #BEFORE# 33      233.
1 #BEFORE# 34      234.
1 #BEFORE# 35      235.
1 #BEFORE# 36      236.
```

```
1 #AFTER #  1      201.
1 #AFTER #  2      202.
1 #AFTER #  3      203.
1 #AFTER #  4      204.
1 #AFTER #  5      205.
1 #AFTER #  6      206.
1 #AFTER #  7      207.
1 #AFTER #  8      208.
1 #AFTER #  9      209.
1 #AFTER # 10      210.
1 #AFTER # 11      211.
1 #AFTER # 12      212.
1 #AFTER # 13      213.
1 #AFTER # 14      214.
1 #AFTER # 15      215.
1 #AFTER # 16      216.
1 #AFTER # 17      217.
1 #AFTER # 18      218.
1 #AFTER # 19      219.
1 #AFTER # 20      220.
1 #AFTER # 21      221.
1 #AFTER # 22      222.
1 #AFTER # 23      223.
1 #AFTER # 24      224.
1 #AFTER # 25      225.
1 #AFTER # 26      101.
1 #AFTER # 27      102.
1 #AFTER # 28      103.
1 #AFTER # 29      104.
1 #AFTER # 30      105.
1 #AFTER # 31      106.
1 #AFTER # 32      107.
1 #AFTER # 33      108.
1 #AFTER # 34      109.
1 #AFTER # 35      110.
1 #AFTER # 36      111.
```

t1

Ex.2: Send-Recv an Array (2/4)

```
if (my_rank.eq.0) then
  call MPI_Isend (VEC( 1),11,MPI_DOUBLE_PRECISION,1,…,req_send,…)
  call MPI_Irecv (VEC(12),25,MPI_DOUBLE_PRECISION,1,…,req_recv,…)
endif

if (my_rank.eq.1) then
  call MPI_Isend (VEC( 1),25,MPI_DOUBLE_PRECISION,0,…,req_send,…)
  call MPI_Irecv (VEC(26),11,MPI_DOUBLE_PRECISION,0,…,req_recv,…)
endif

call MPI_Waitall (…,req_recv,stat_recv,…)
call MPI_Waitall (…,req_send,stat_send,…)
```

It works, but complicated operations.

Not looks like SPMD.

Not portable.

t1

Ex.2: Send-Recv an Array (3/4)

```
if (my_rank.eq.0) then
  NEIB= 1
   start_send=   1
  length_send=  11
   start_recv=  length_send + 1
  length_recv=  25
endif

if (my_rank.eq.1) then
  NEIB= 0
   start_send=  1
  length_send= 25
   start_recv= length_send + 1
  length_recv= 11
endif

call MPI_Isend                                                    &
(VEC(start_send),length_send,MPI_DOUBLE_PRECISION,NEIB,…,req_send,…)
call MPI_Irecv                                                    &
(VEC(start_recv),length_recv,MPI_DOUBLE_PRECISION,NEIB,…,req_recv,…)

call MPI_Waitall (…,req_recv,stat_recv,…)
call MPI_Waitall (…,req_send,stat_send,…)
```

This is “SMPD” !!

t1

Ex.2: Send-Recv an Array (4/4)

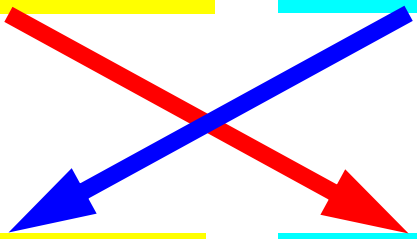
```
if (my_rank.eq.0) then
  NEIB= 1
   start_send=   1
  length_send=  11
   start_recv=  length_send + 1
  length_recv=  25
endif

if (my_rank.eq.1) then
  NEIB= 0
   start_send=  1
  length_send= 25
   start_recv= length_send + 1
  length_recv= 11
endif

call MPI_Sendrecv                                                  &
(VEC(start_send),length_send,MPI_DOUBLE_PRECISION,NEIB,…           &
 VEC(start_recv),length_recv,MPI_DOUBLE_PRECISION,NEIB,…, status,…)
```

t1

Notice: Send/Recv Arrays

```
#PE0
  send:
    VEC(start_send)~
    VEC(start_send+length_send-1)
```

```
#PE1
  send:
    VEC(start_send)~
    VEC(start_send+length_send-1)
```



```
#PE0
  recv:
    VEC(start_recv)~
    VEC(start_recv+length_recv-1)
```

```
#PE1
  recv:
    VEC(start_recv)~
    VEC(start_recv+length_recv-1)
```

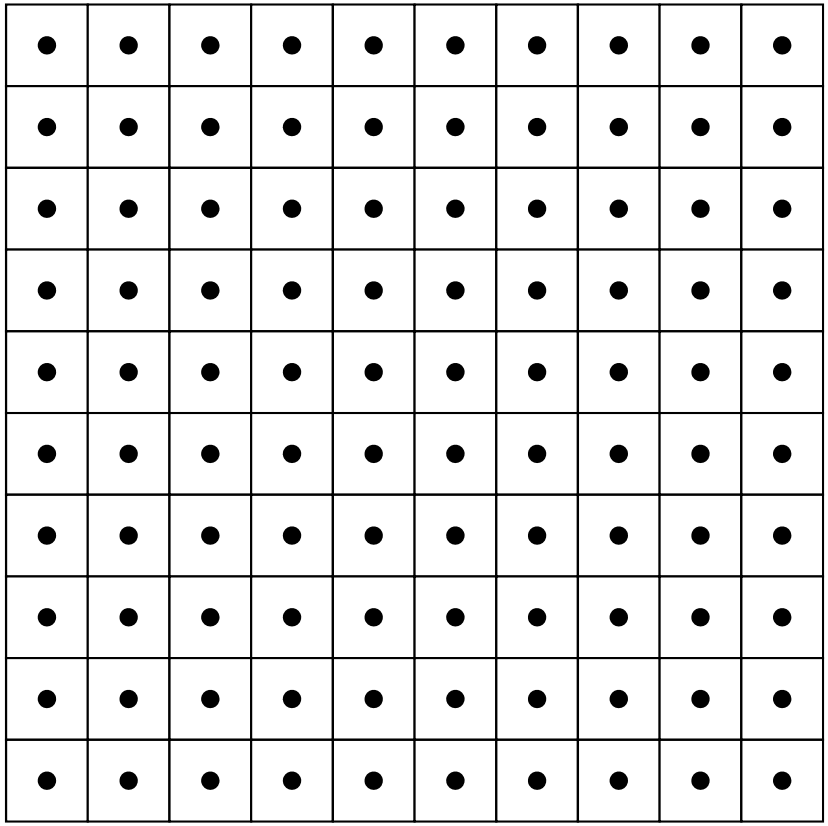
- “length_send” of sending process must be equal to “length_recv” of receiving process.
  - PE#0 to PE#1, PE#1 to PE#0
- “sendbuf” and “recvbuf”: different address

Peer-to-Peer Communication

- What is P2P Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

2D FDM (1/5)

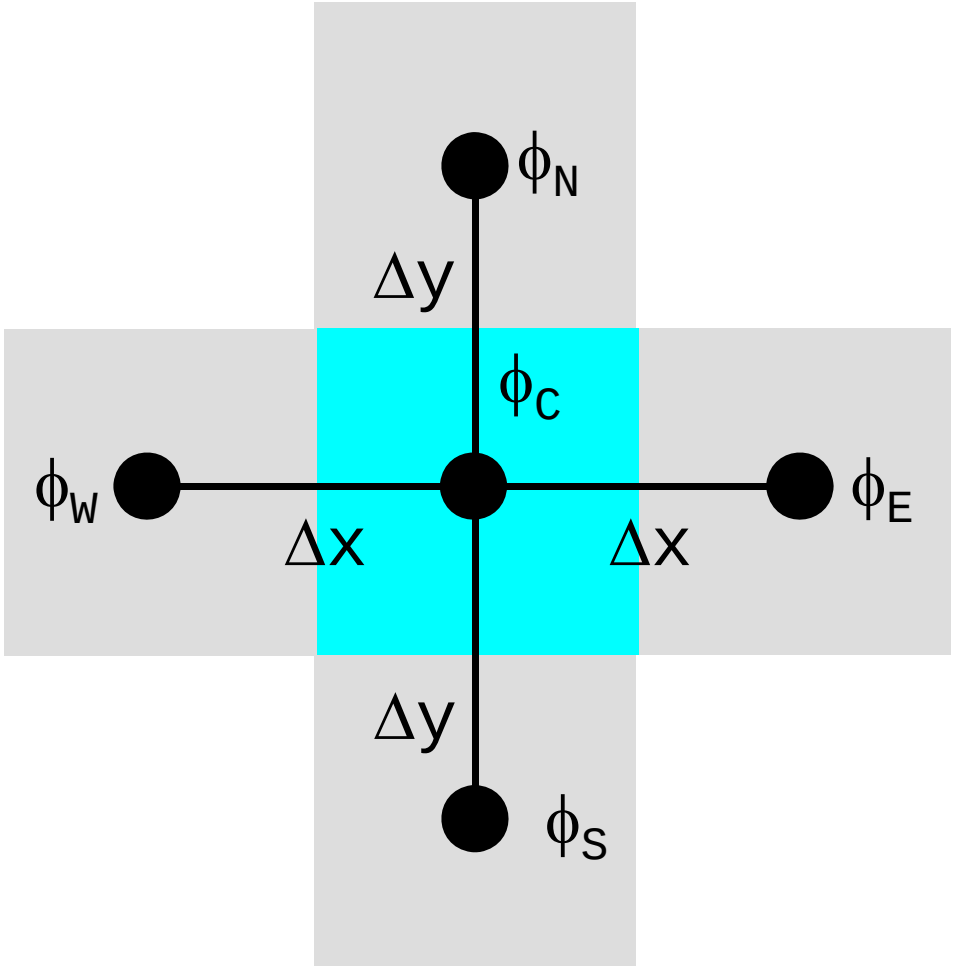
Entire Mesh



2D FDM (5-point, central difference)

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = f$$

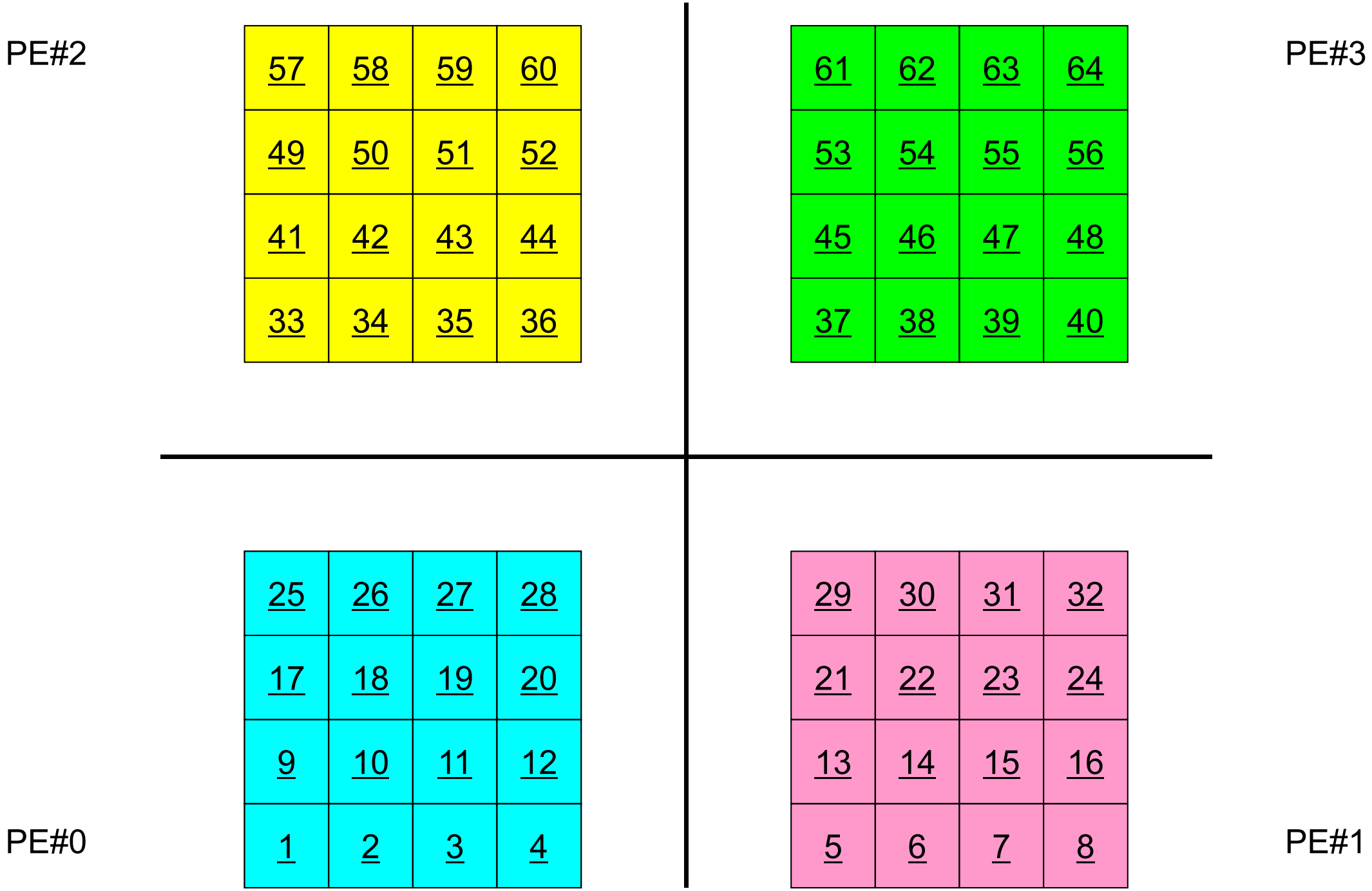
$$\left(\frac{\phi_E - 2\phi_C + \phi_W}{\Delta x^2} \right) + \left(\frac{\phi_N - 2\phi_C + \phi_S}{\Delta y^2} \right) = f_C$$



Decompose into 4 domains

57	58	59	60	61	62	63	64
49	50	51	52	53	54	55	56
41	42	43	44	45	46	47	48
33	34	35	36	37	38	39	40
25	26	27	28	29	30	31	32
17	18	19	20	21	22	23	24
9	10	11	12	13	14	15	16
1	2	3	4	5	6	7	8

4 domains: Global ID



4 domains: Local ID

PE#2

13	14	15	16
9	10	11	12
5	6	7	8
1	2	3	4

PE#3

13	14	15	16
9	10	11	12
5	6	7	8
1	2	3	4

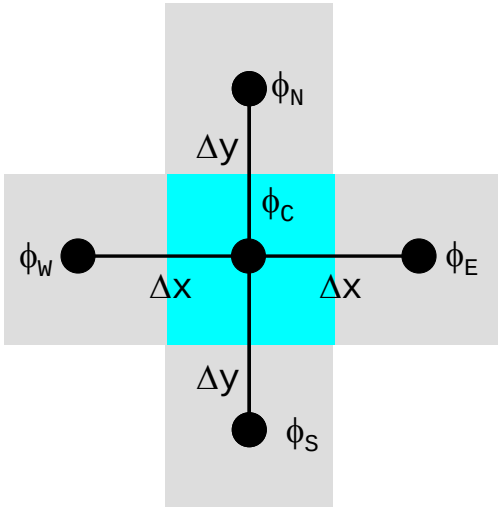
PE#0

13	14	15	16
9	10	11	12
5	6	7	8
1	2	3	4

PE#1

13	14	15	16
9	10	11	12
5	6	7	8
1	2	3	4

External Points: Overlapped Region



PE#2

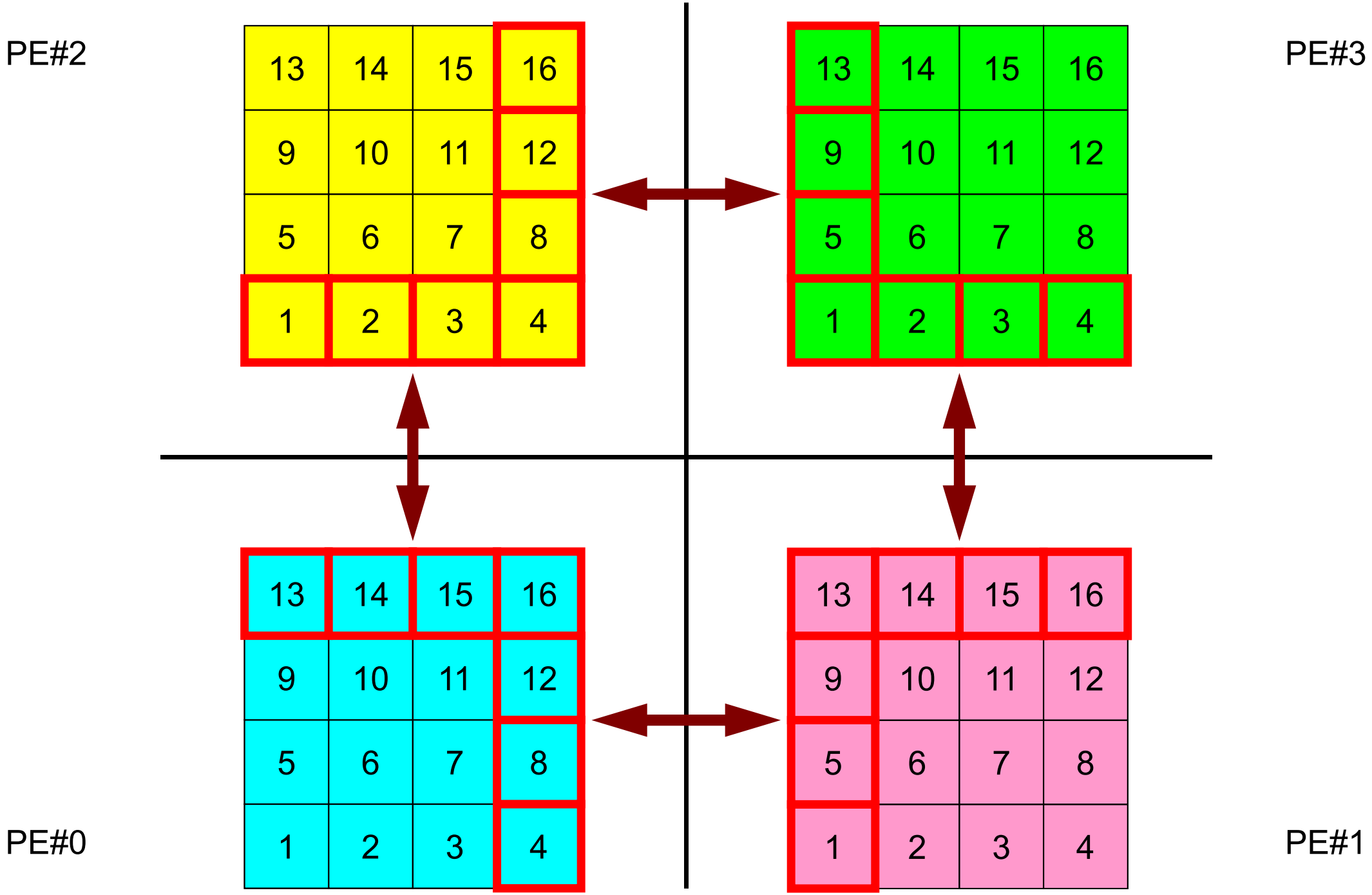
PE#3

13	14	15	16	13	14	15	16
9	10	11	12	9	10	11	12
5	6	7	8	5	6	7	8
1	2	3	4	1	2	3	4
13	14	15	16	13	14	15	16
9	10	11	12	9	10	11	12
5	6	7	8	5	6	7	8
1	2	3	4	1	2	3	4

PE#0

PE#1

External Points: Overlapped Region



Local ID of External Points ?

PE#2

13	14	15	16	?
9	10	11	12	?
5	6	7	8	?
1	2	3	4	?
?	?	?	?	

PE#3

?	13	14	15	16
?	9	10	11	12
?	5	6	7	8
?	1	2	3	4
	?	?	?	?

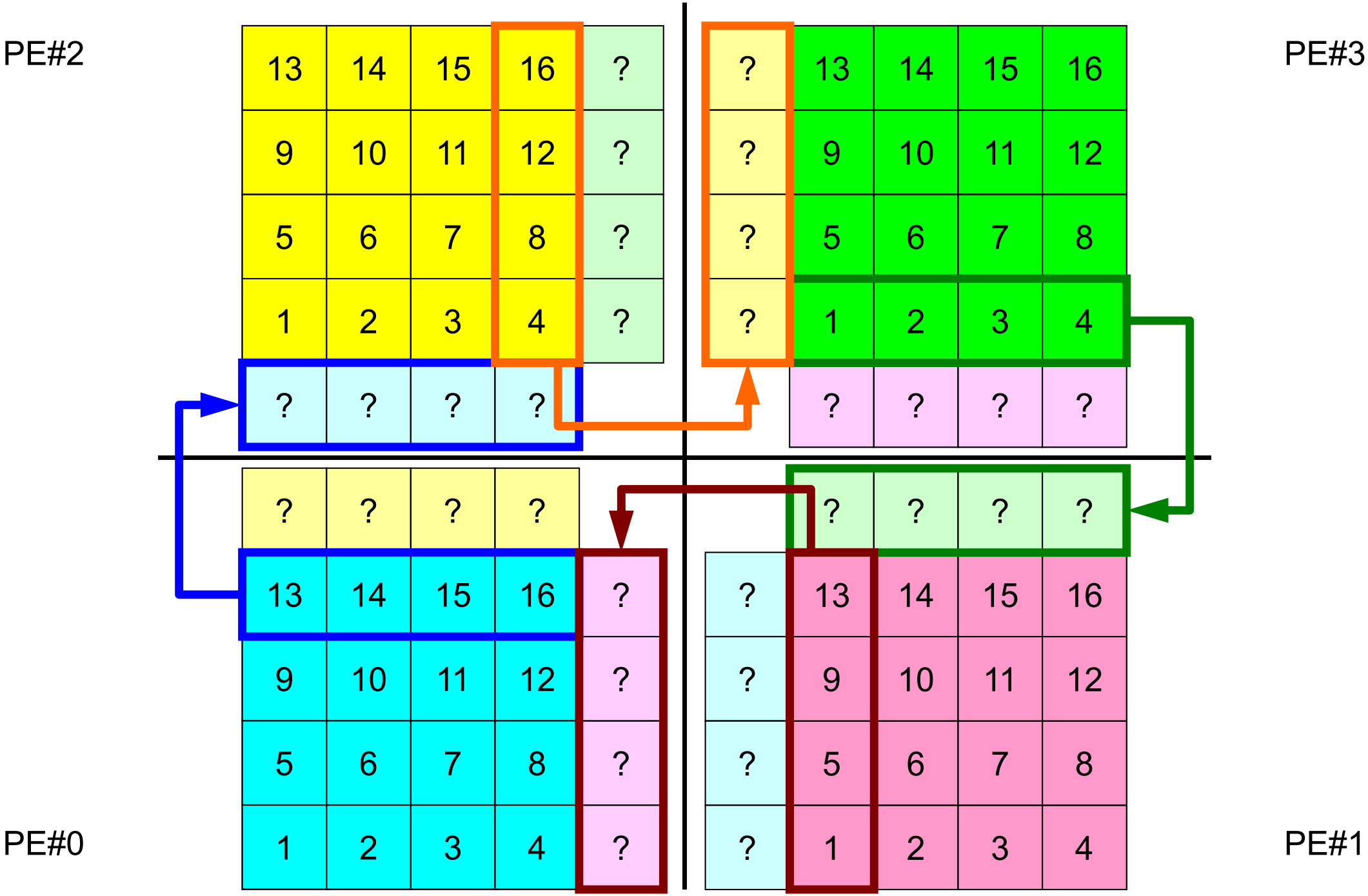
PE#0

?	?	?	?	
13	14	15	16	?
9	10	11	12	?
5	6	7	8	?
1	2	3	4	?

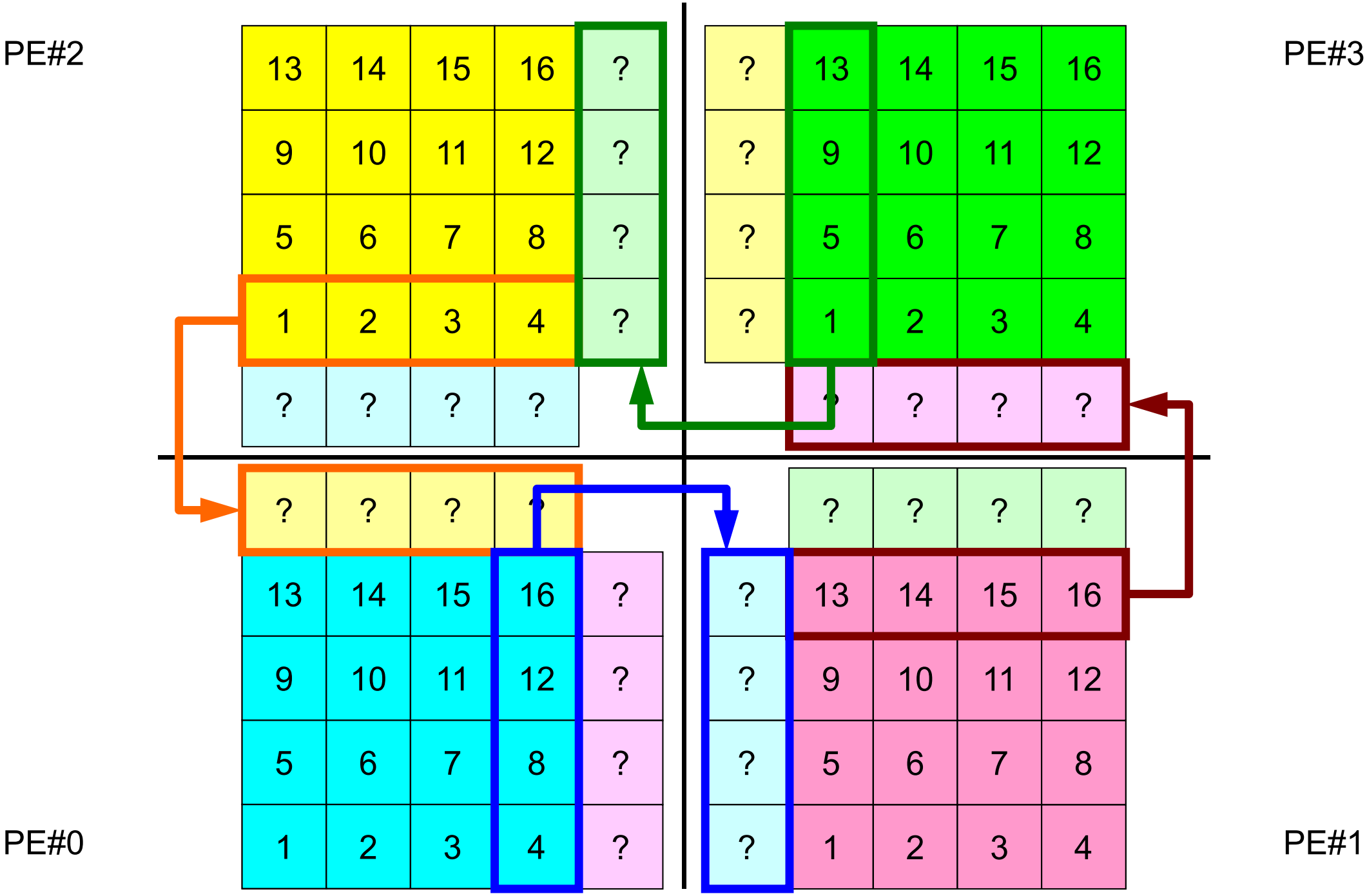
PE#1

	?	?	?	?
?	13	14	15	16
?	9	10	11	12
?	5	6	7	8
?	1	2	3	4

Overlapped Region



Overlapped Region



Peer-to-Peer Communication

- What is P2P Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

Problem Setting: 2D FDM

57	58	59	60	61	62	63	64
49	50	51	52	53	54	55	56
41	42	43	44	45	46	47	48
33	34	35	36	37	38	39	40
25	26	27	28	29	30	31	32
17	18	19	20	21	22	23	24
9	10	11	12	13	14	15	16
1	2	3	4	5	6	7	8

- 2D region with 64 meshes (8x8)
- Each mesh has global ID from 1 to 64
  - In this example, this global ID is considered as dependent variable, such as temperature, pressure etc.
  - Something like computed results

Problem Setting: Distributed Local Data

PE#2

57	58	59	60
49	50	51	52
41	42	43	44
33	34	35	36

PE#3

61	62	63	64
53	54	55	56
45	46	47	48
37	38	39	40

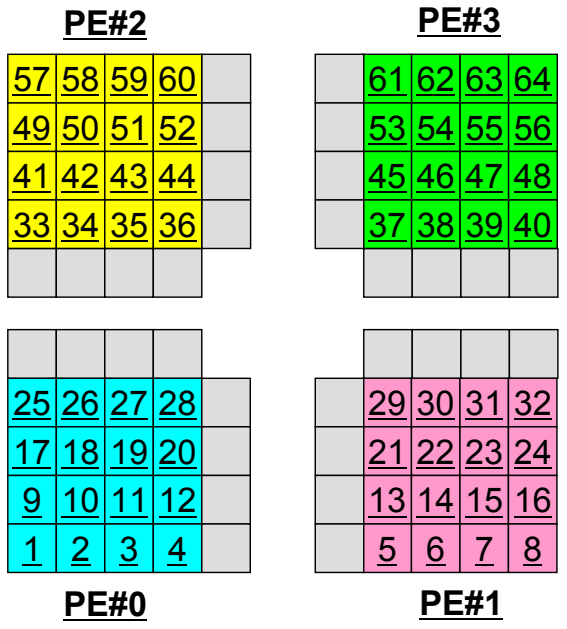
25	26	27	28
17	18	19	20
9	10	11	12
1	2	3	4

PE#0

29	30	31	32
21	22	23	24
13	14	15	16
5	6	7	8

PE#1

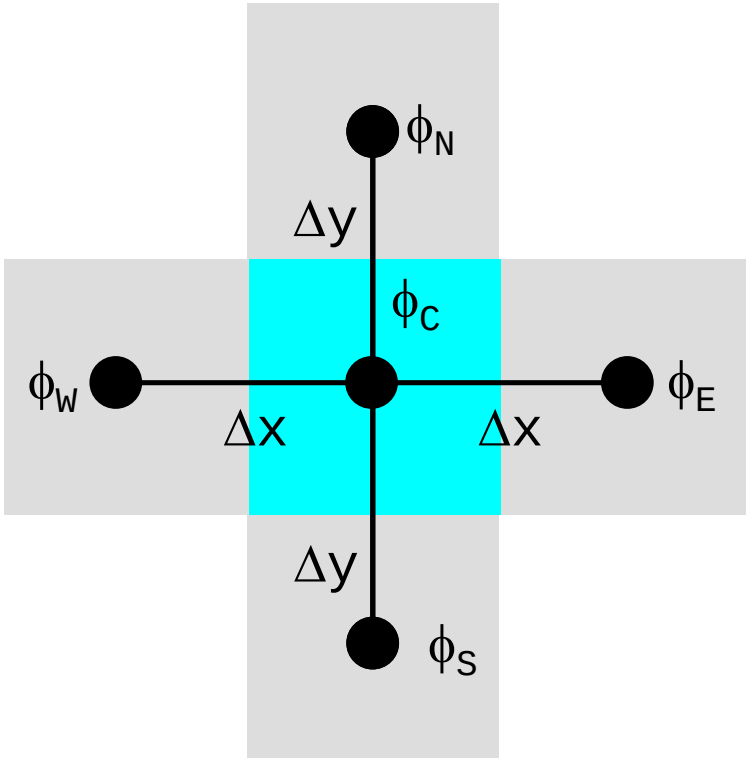
- 4 sub-domains.
- Info. of external points (global ID of mesh) is received from neighbors.
  - PE#0 receives □



Operations of 2D FDM

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = f$$

$$\left(\frac{\phi_E - 2\phi_C + \phi_W}{\Delta x^2} \right) + \left(\frac{\phi_N - 2\phi_C + \phi_S}{\Delta y^2} \right) = f_C$$

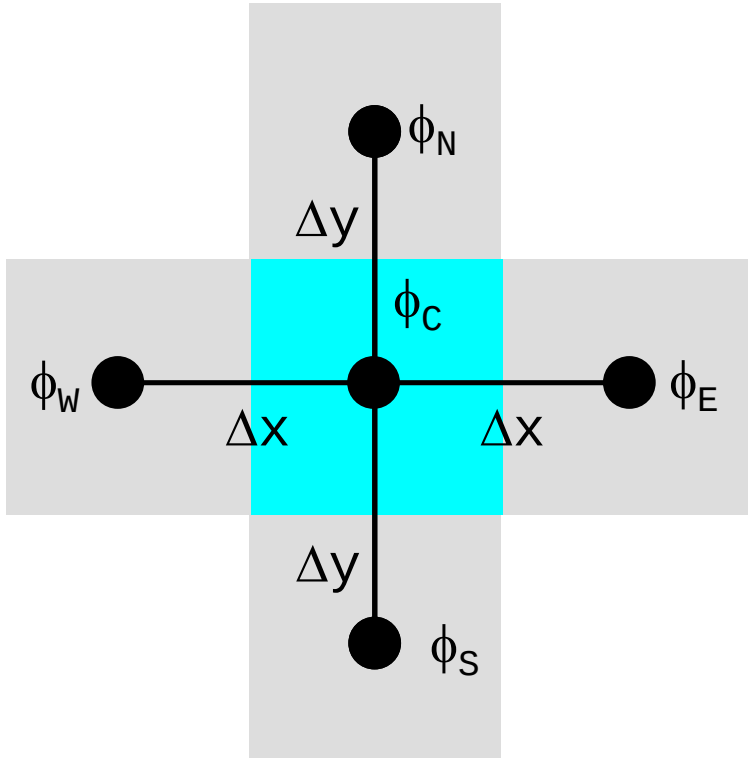


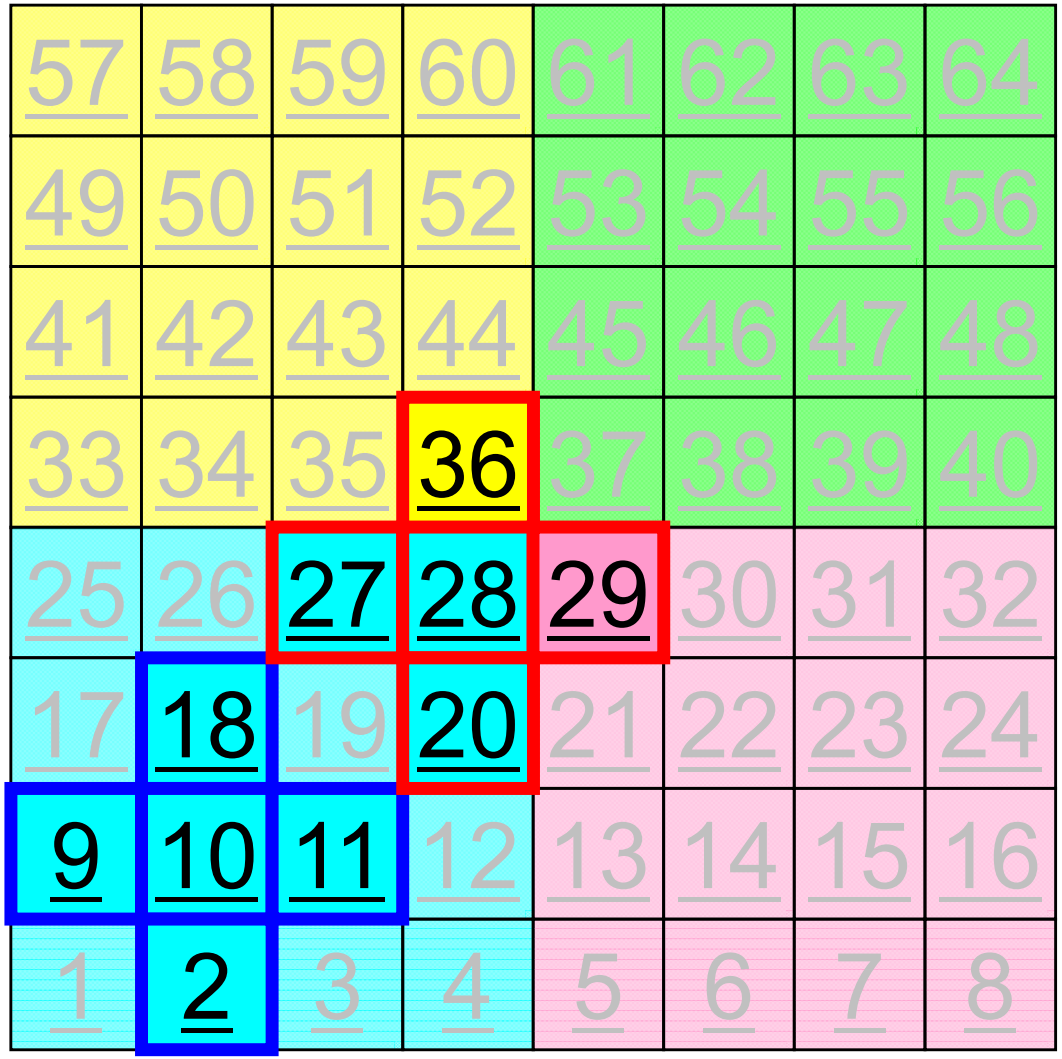
57	58	59	60	61	62	63	64
49	50	51	52	53	54	55	56
41	42	43	44	45	46	47	48
33	34	35	36	37	38	39	40
25	26	27	28	29	30	31	32
17	18	19	20	21	22	23	24
9	10	11	12	13	14	15	16
1	2	3	4	5	6	7	8

Operations of 2D FDM

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = f$$

$$\left(\frac{\phi_E - 2\phi_C + \phi_W}{\Delta x^2} \right) + \left(\frac{\phi_N - 2\phi_C + \phi_S}{\Delta y^2} \right) = f_C$$





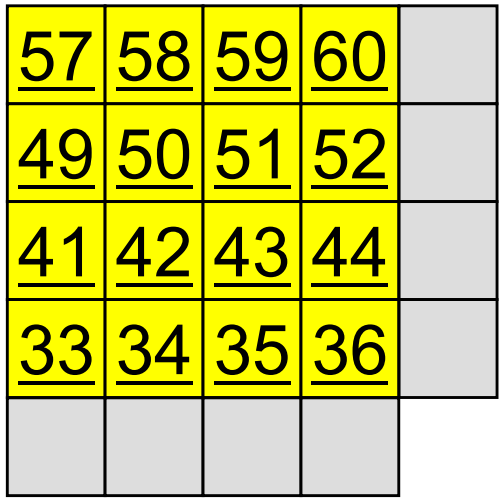
Computation (1/3)

- On each PE, info. of internal pts (i=1-N(=16)) are read from distributed local data, info. of boundary pts are sent to neighbors, and they are received as info. of external pts.

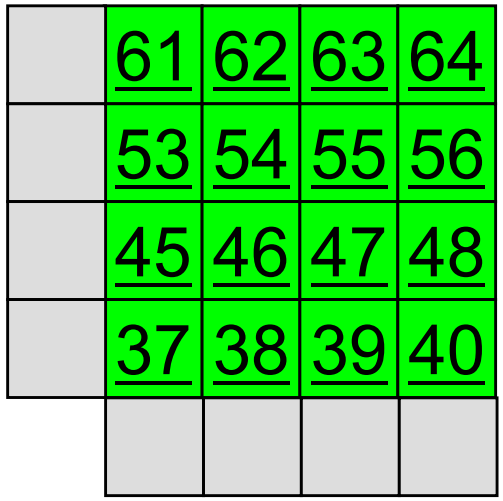
Computation (2/3): Before Send/Recv

PE#2

1: 33	9: 49	17: ?
2: 34	10: 50	18: ?
3: 35	11: 51	19: ?
4: 36	12: 52	20: ?
5: 41	13: 57	21: ?
6: 42	14: 58	22: ?
7: 43	15: 59	23: ?
8: 44	16: 60	24: ?

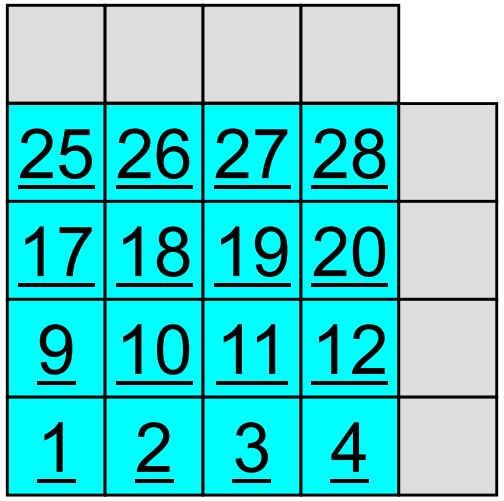


PE#3

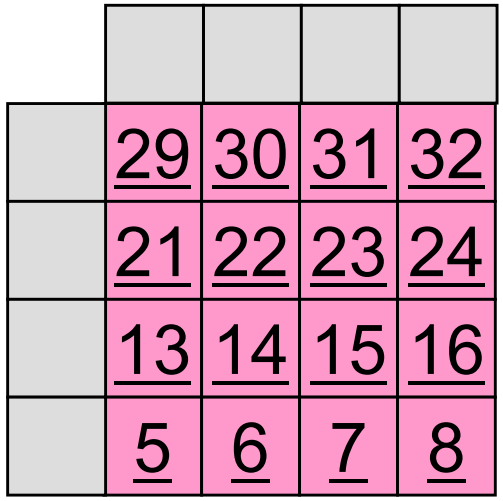


1: 37	9: 53	17: ?
2: 38	10: 54	18: ?
3: 39	11: 55	19: ?
4: 40	12: 56	20: ?
5: 45	13: 61	21: ?
6: 46	14: 62	22: ?
7: 47	15: 63	23: ?
8: 48	16: 64	24: ?

1: 1	9: 17	17: ?
2: 2	10: 18	18: ?
3: 3	11: 19	19: ?
4: 4	12: 20	20: ?
5: 9	13: 25	21: ?
6: 10	14: 26	22: ?
7: 11	15: 27	23: ?
8: 12	16: 28	24: ?



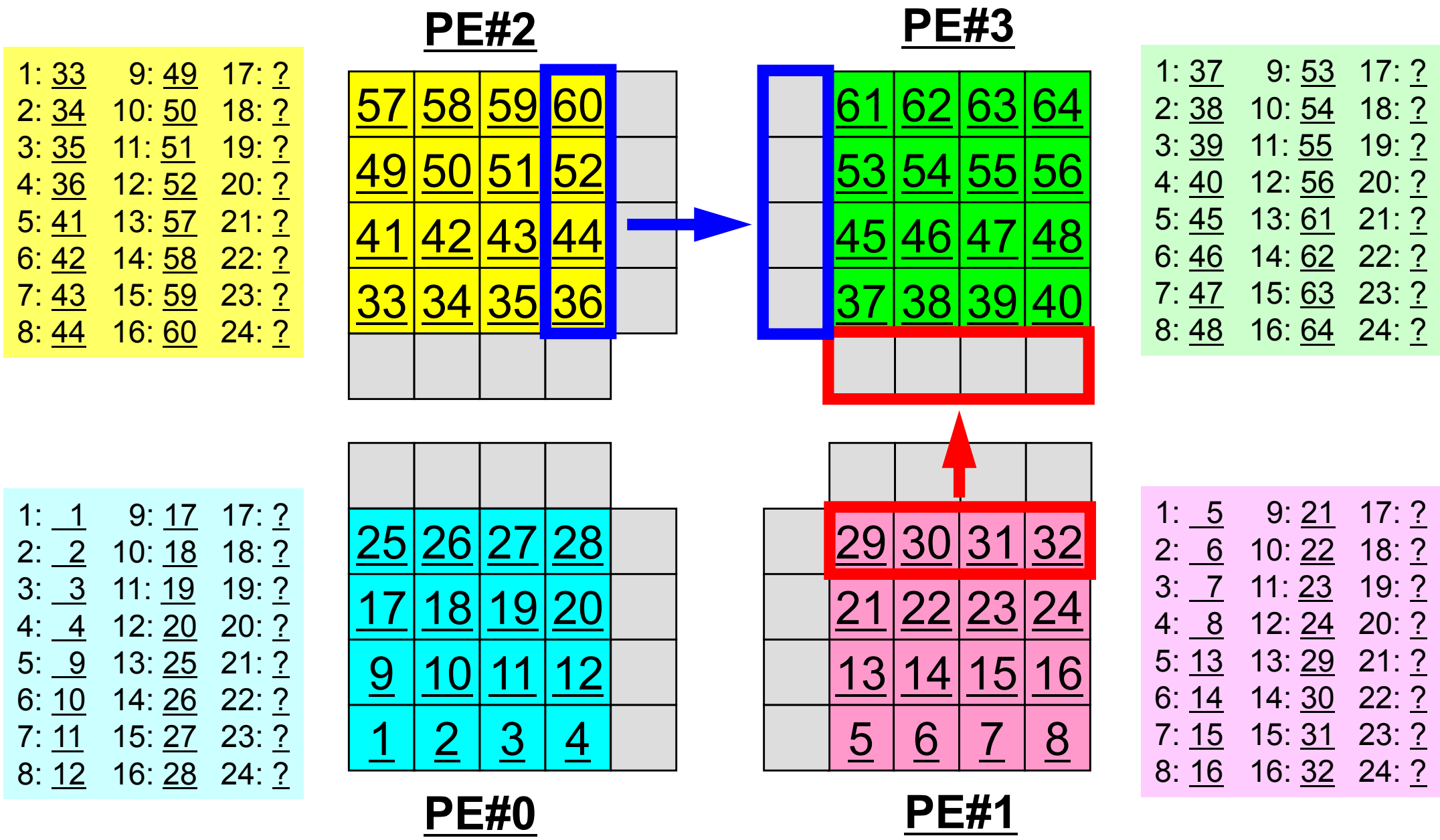
PE#0



PE#1

1: 5	9: 21	17: ?
2: 6	10: 22	18: ?
3: 7	11: 23	19: ?
4: 8	12: 24	20: ?
5: 13	13: 29	21: ?
6: 14	14: 30	22: ?
7: 15	15: 31	23: ?
8: 16	16: 32	24: ?

Computation (2/3): Before Send/Recv



Computation (3/3): After Send/Recv

PE#2

57	58	59	60	61
49	50	51	52	53
41	42	43	44	45
33	34	35	36	37
25	26	27	28	

1: 33	9: 49	17: 37
2: 34	10: 50	18: 45
3: 35	11: 51	19: 53
4: 36	12: 52	20: 61
5: 41	13: 57	21: 25
6: 42	14: 58	22: 26
7: 43	15: 59	23: 27
8: 44	16: 60	24: 28

PE#3

60	61	62	63	64
52	53	54	55	56
44	45	46	47	48
36	37	38	39	40
	29	30	31	32

1: 37	9: 53	17: 36
2: 38	10: 54	18: 44
3: 39	11: 55	19: 52
4: 40	12: 56	20: 60
5: 45	13: 61	21: 29
6: 46	14: 62	22: 30
7: 47	15: 63	23: 31
8: 48	16: 64	24: 32

33	34	35	36	
25	26	27	28	29
17	18	19	20	21
9	10	11	12	13
1	2	3	4	5

1: 1	9: 17	17: 5
2: 2	10: 18	18: 14
3: 3	11: 19	19: 21
4: 4	12: 20	20: 29
5: 9	13: 25	21: 33
6: 10	14: 26	22: 34
7: 11	15: 27	23: 35
8: 12	16: 28	24: 36

PE#0

	37	38	39	40
28	29	30	31	32
20	21	22	23	24
12	13	14	15	16
4	5	6	7	8

1: 5	9: 21	17: 4
2: 6	10: 22	18: 12
3: 7	11: 23	19: 20
4: 8	12: 24	20: 28
5: 13	13: 29	21: 37
6: 14	14: 30	22: 38
7: 15	15: 31	23: 39
8: 16	16: 32	24: 40

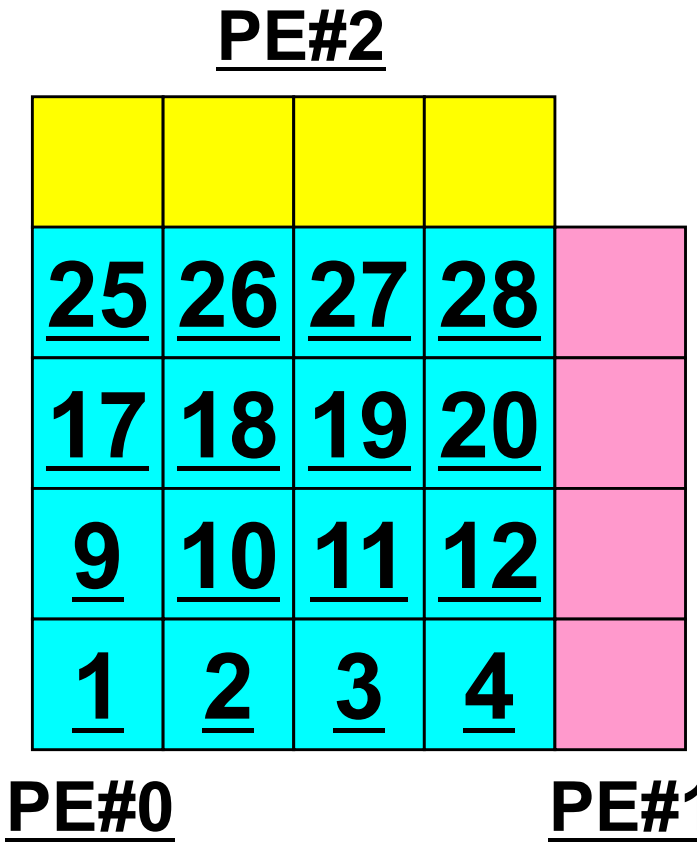
PE#1

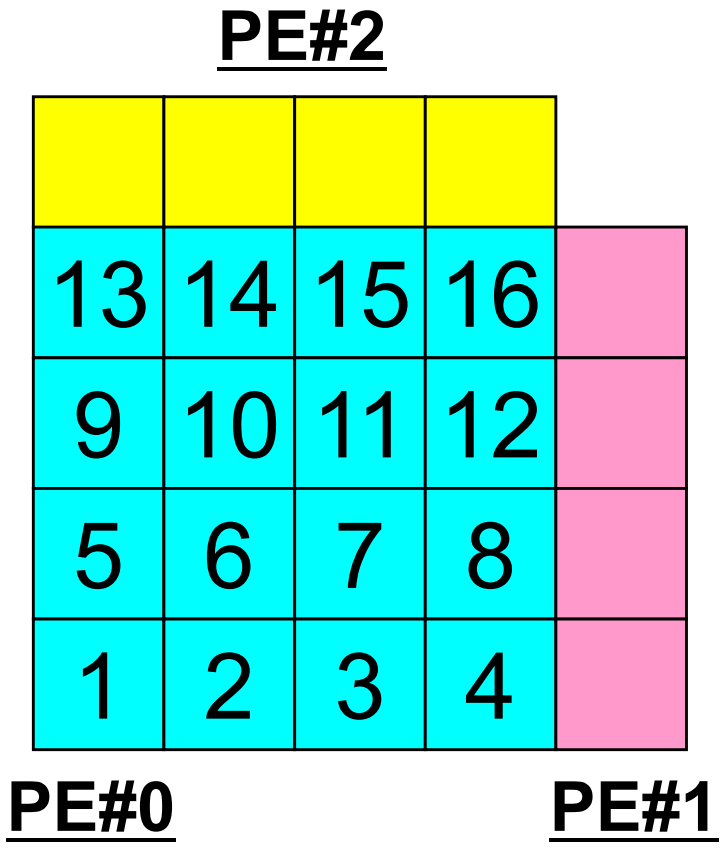
Peer-to-Peer Communication

- What is P2P Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

Overview of Distributed Local Data

Example on PE#0

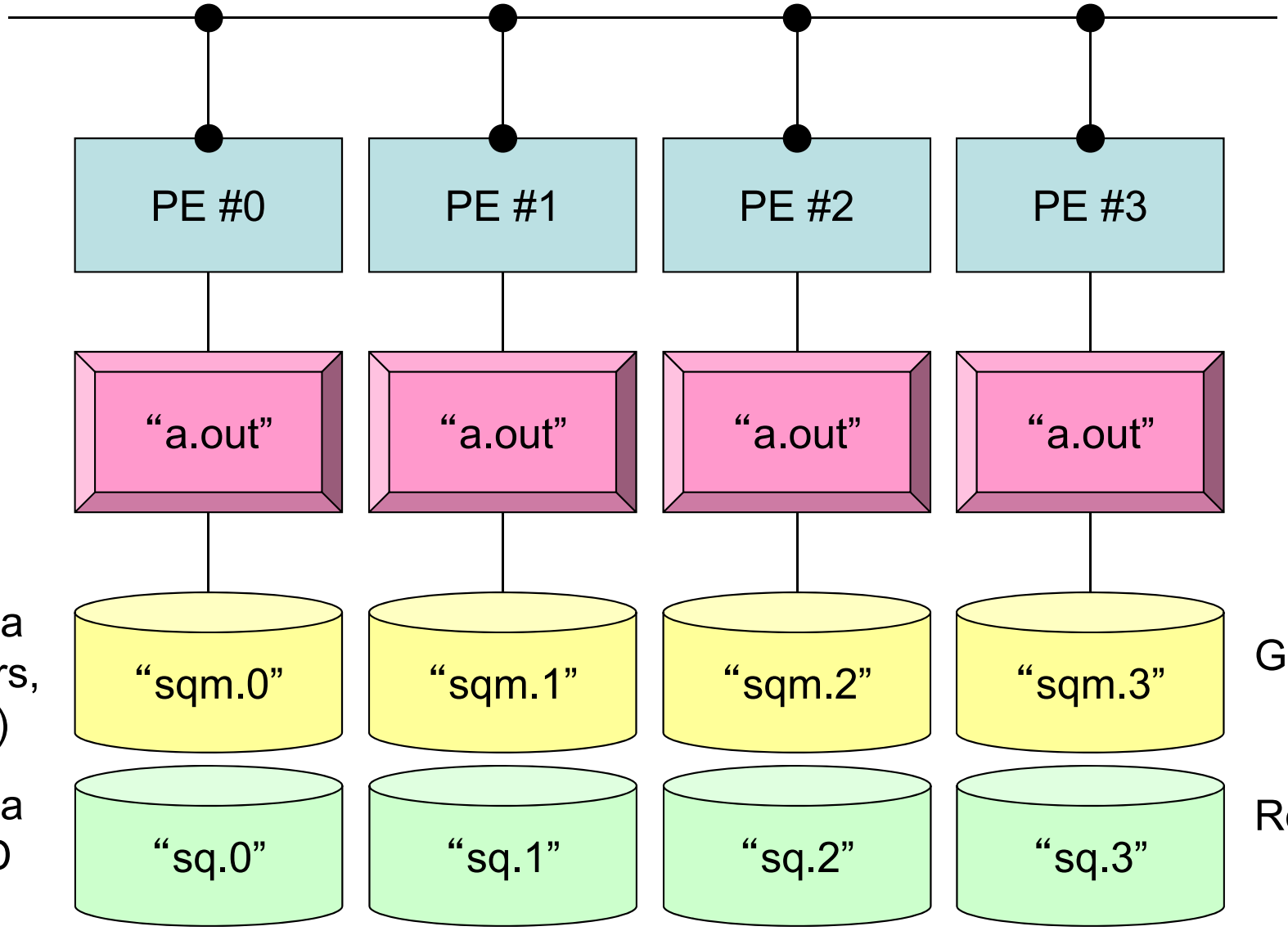




Value at each mesh (= Global ID)

Local ID

SPMD・・・



Dist. Local Data Sets (Neighbors, Comm. Tables)

Geometry

Dist. Local Data Sets (Global ID of Internal Points)

Results

2D FDM: PE#0

Information at each domain (1/4)

Internal Points

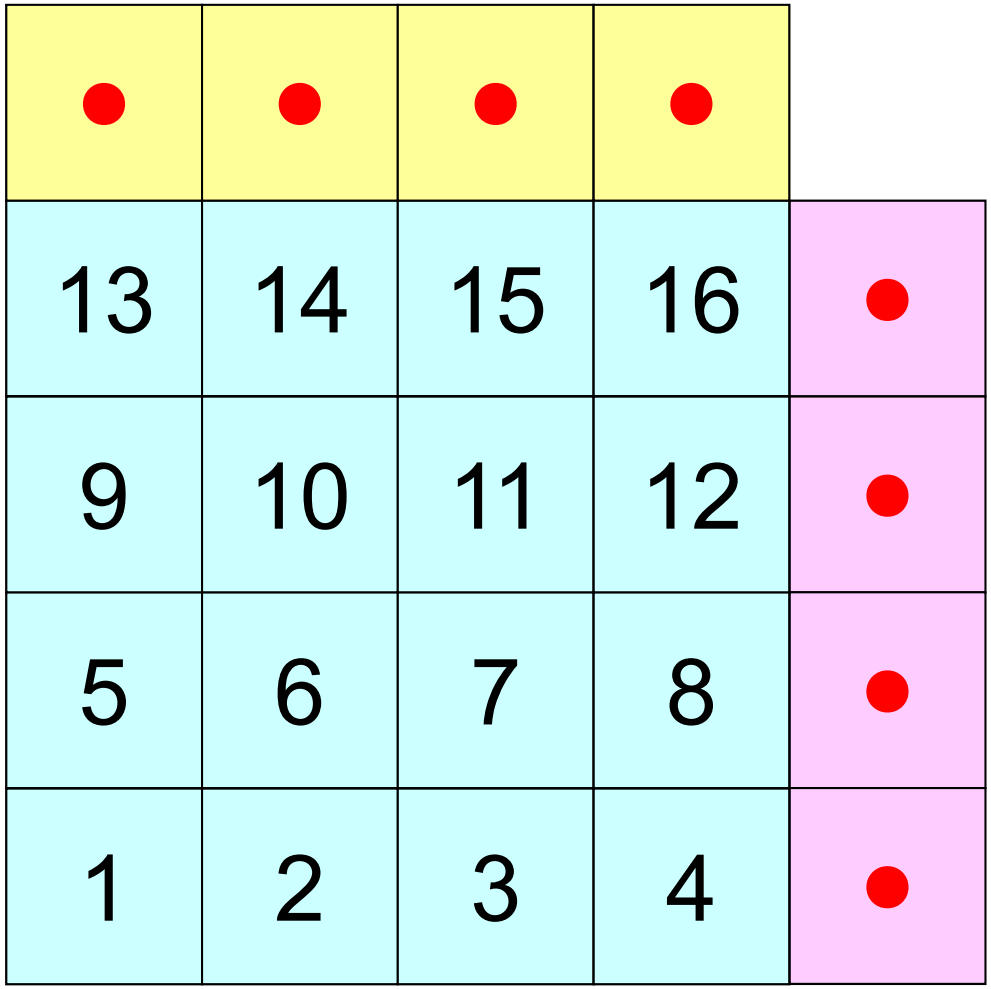
Meshes originally assigned to the domain

13	14	15	16
9	10	11	12
5	6	7	8
1	2	3	4

2D FDM: PE#0

Information at each domain (2/4)

PE#2



Internal Points

Meshes originally assigned to the domain

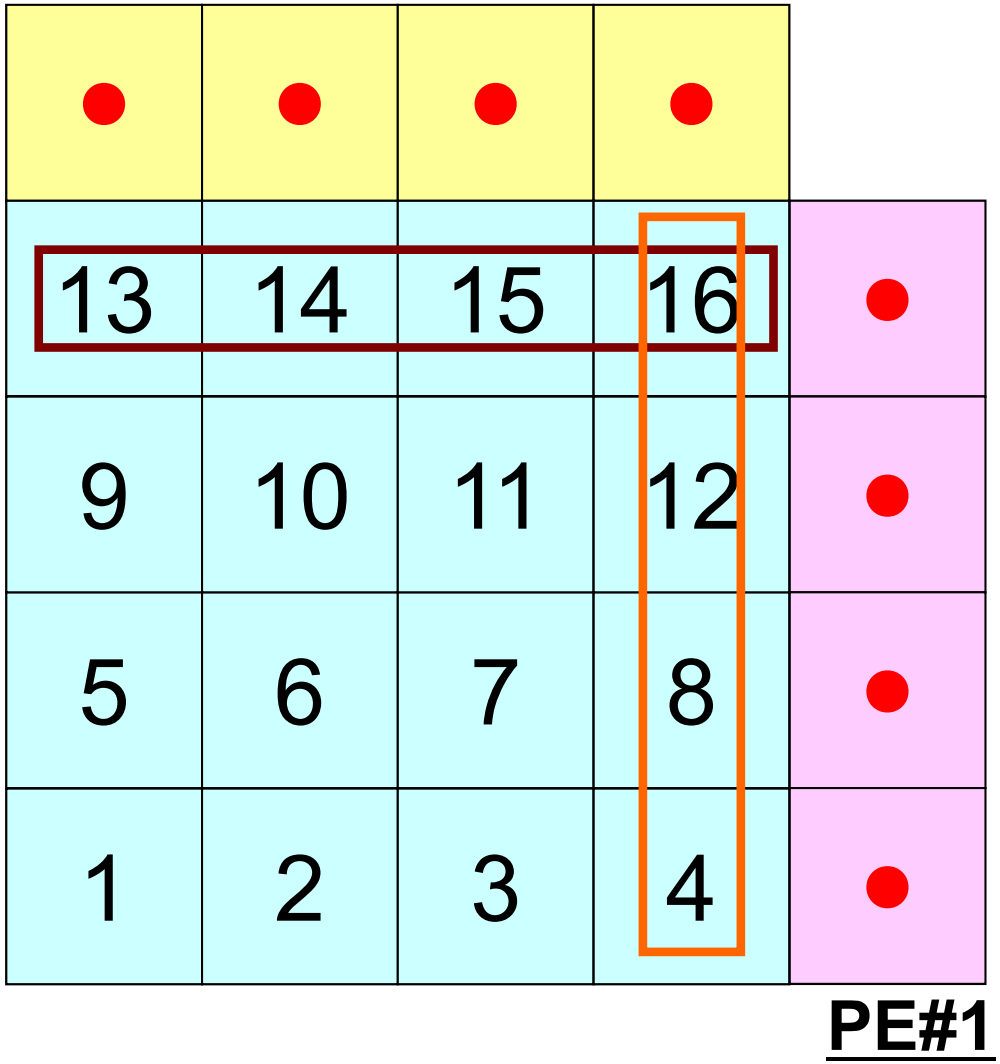
External Points

Meshes originally assigned to different domain, but required for computation of meshes in the domain (meshes in overlapped regions)

- Sleeves
- Halo

2D FDM: PE#0

Information at each domain (3/4)



Internal Points
Meshes originally assigned to the domain

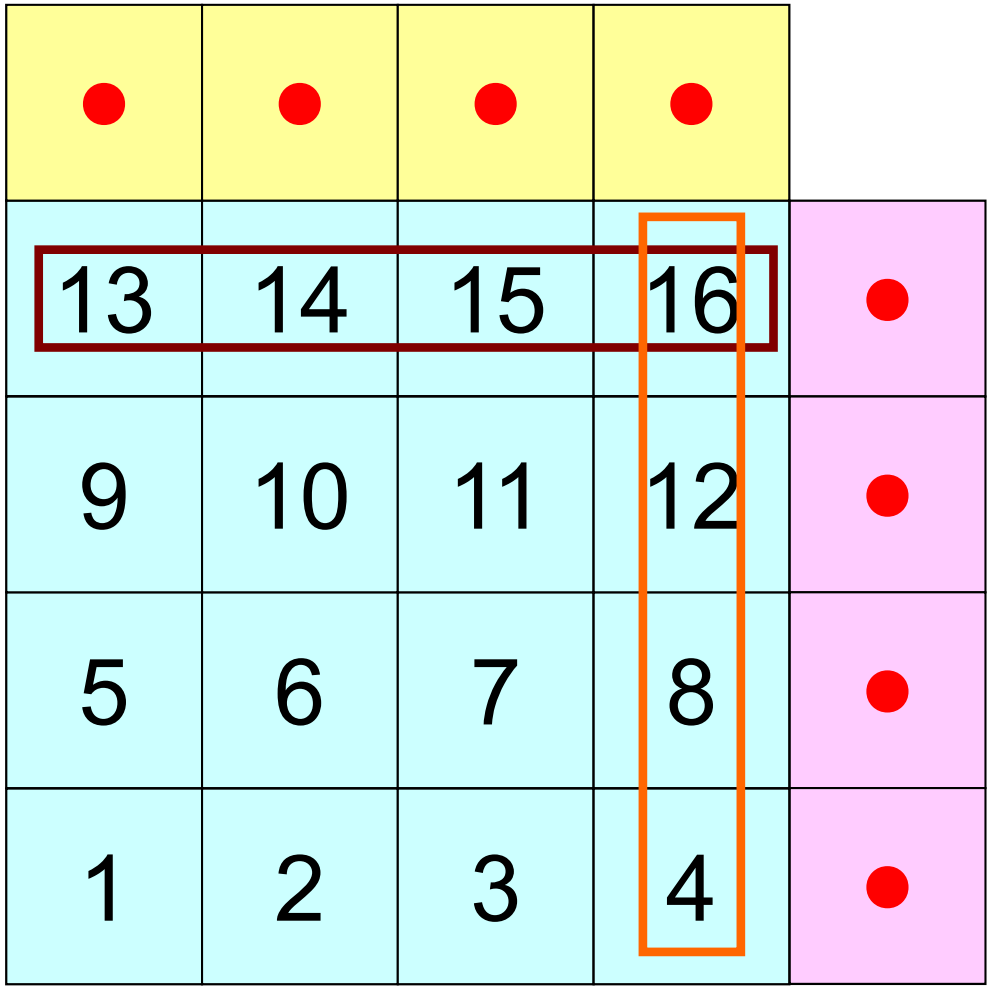
External Points
Meshes originally assigned to different domain, but required for computation of meshes in the domain (meshes in overlapped regions)

Boundary Points
Internal points, which are also external points of other domains (used in computations of meshes in other domains)

2D FDM: PE#0

Information at each domain (4/4)

PE#2



PE#1

Internal Points

Meshes originally assigned to the domain

External Points

Meshes originally assigned to different domain, but required for computation of meshes in the domain (meshes in overlapped regions)

Boundary Points

Internal points, which are also external points of other domains (used in computations of meshes in other domains)

Relationships between Domains

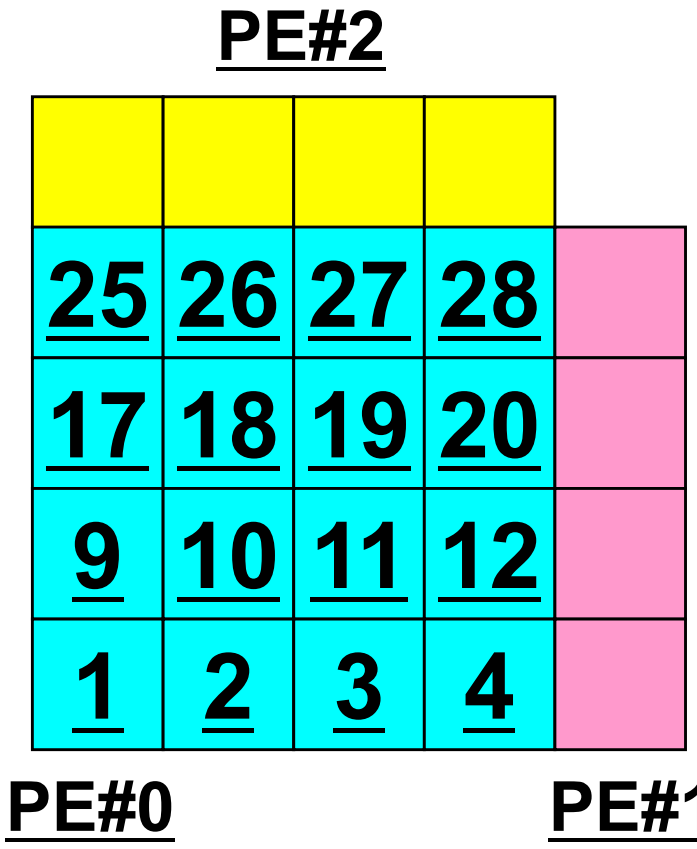
Communication Table: External/Boundary Points Neighbors

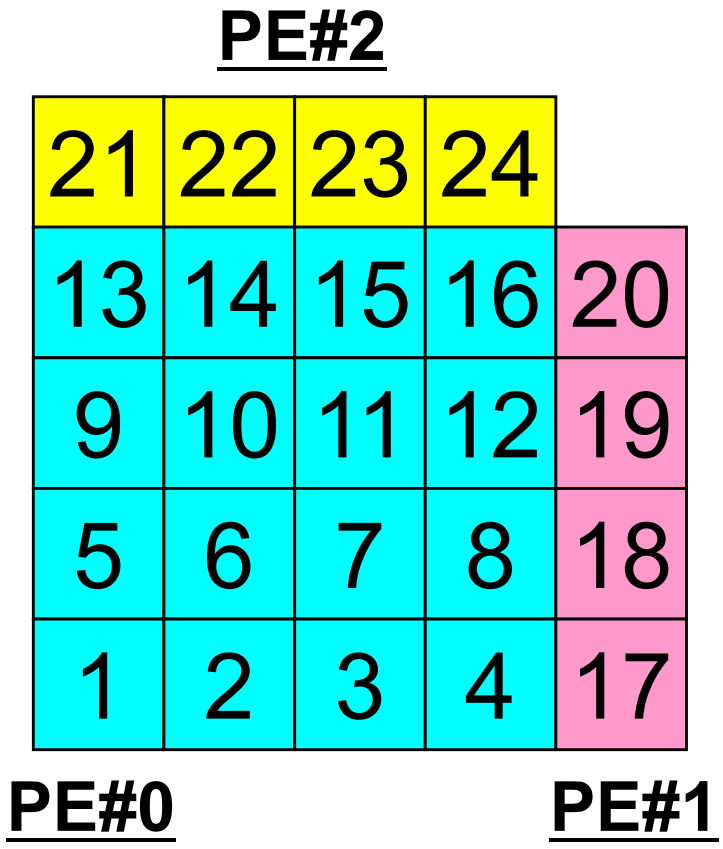
Description of Distributed Local Data

- Internal/External Points
  - Numbering: Starting from internal pts, then external pts after that
- Neighbors
  - Shares overlapped meshes
  - Number and ID of neighbors
- Import Table (Receive)
  - From where, how many, and which external points are received/imported ?
- Export Table (Send)
  - To where, how many and which boundary points are sent/exported ?

Overview of Distributed Local Data

Example on PE#0





Value at each mesh (= Global ID)

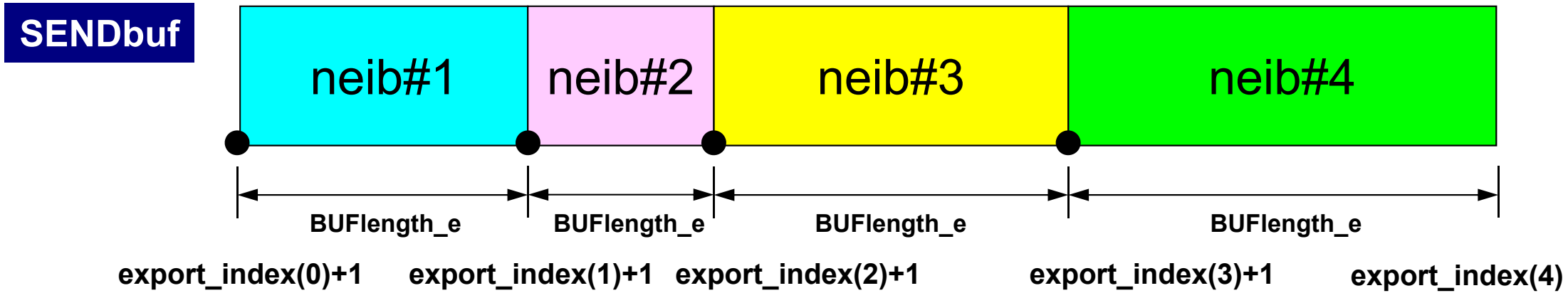
Local ID

Generalized Comm. Table: Send

- Neighbors
  - NEIBPETOT, NEIBPE(neib)
- Message size for each neighbor
  - export_index(neib), neib= 0, NEIBPETOT
- ID of **boundary** points
  - export_item(k), k= 1, export_index(NEIBPETOT)
- Messages to each neighbor
  - SENDbuf(k), k= 1, export_index(NEIBPETOT)

Fortran

SEND: MPI_Isend/Irecv/Waitall Fortran




```
do neib= 1, NEIBPETOT
  do k= export_index(neib-1)+1, export_index(neib)
    kk= export_item(k)
    SENDbuf(k)= VAL(kk)
  enddo
enddo

do neib= 1, NEIBPETOT
  iS_e= export_index(neib-1) + 1
  iE_e= export_index(neib  )
  BUFlength_e= iE_e + 1 - iS_e

  call MPI_ISEND                                                    &
&         (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_send(neib), ierr)
enddo

call MPI_WAITALL (NEIBPETOT, request_send, stat_recv, ierr)
```

Copied to sending buffers

Generalized Comm. Table: Receive

- Neighbors
  - NEIBPETOT, NEIBPE(neib)
- Message size for each neighbor
  - import_index(neib), neib= 0, NEIBPETOT
- ID of **external** points
  - import_item(k), k= 1, import_index(NEIBPETOT)
- Messages from each neighbor
  - RECVbuf(k), k= 1, import_index(NEIBPETOT)

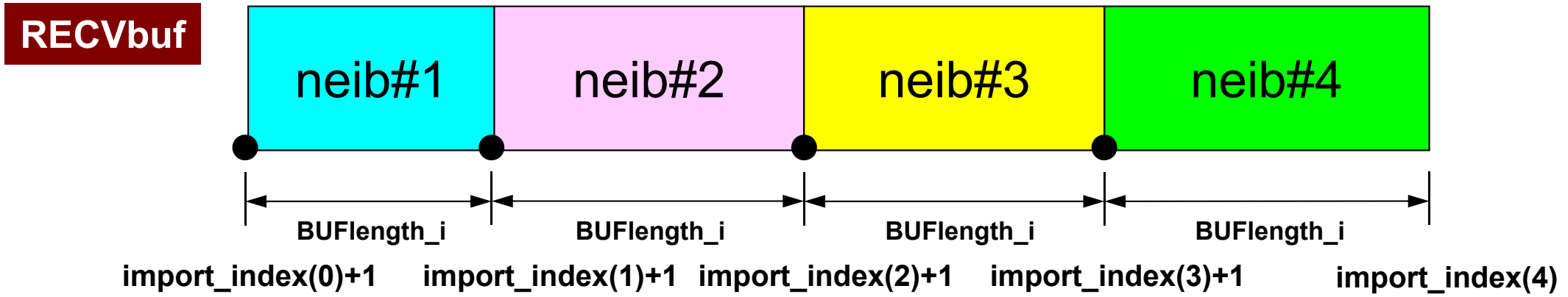
Fortran

RECV: MPI_Isend/Irecv/Waitall

Fortran

```
 do neib= 1, NEIBPETOT
   iS_i= import_index(neib-1) + 1
   iE_i= import_index(neib  )
   BUFlength_i= iE_i + 1 - iS_i

   call MPI_IRECV                                                  &
&         (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_recv(neib), ierr)
  enddo

  call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

  do neib= 1, NEIBPETOT
     do k= import_index(neib-1)+1, import_index(neib)
       kk= import_item(k)
       VAL(kk)= RECVbuf(k)
     enddo
  enddo
```

Copied from receiving buffer



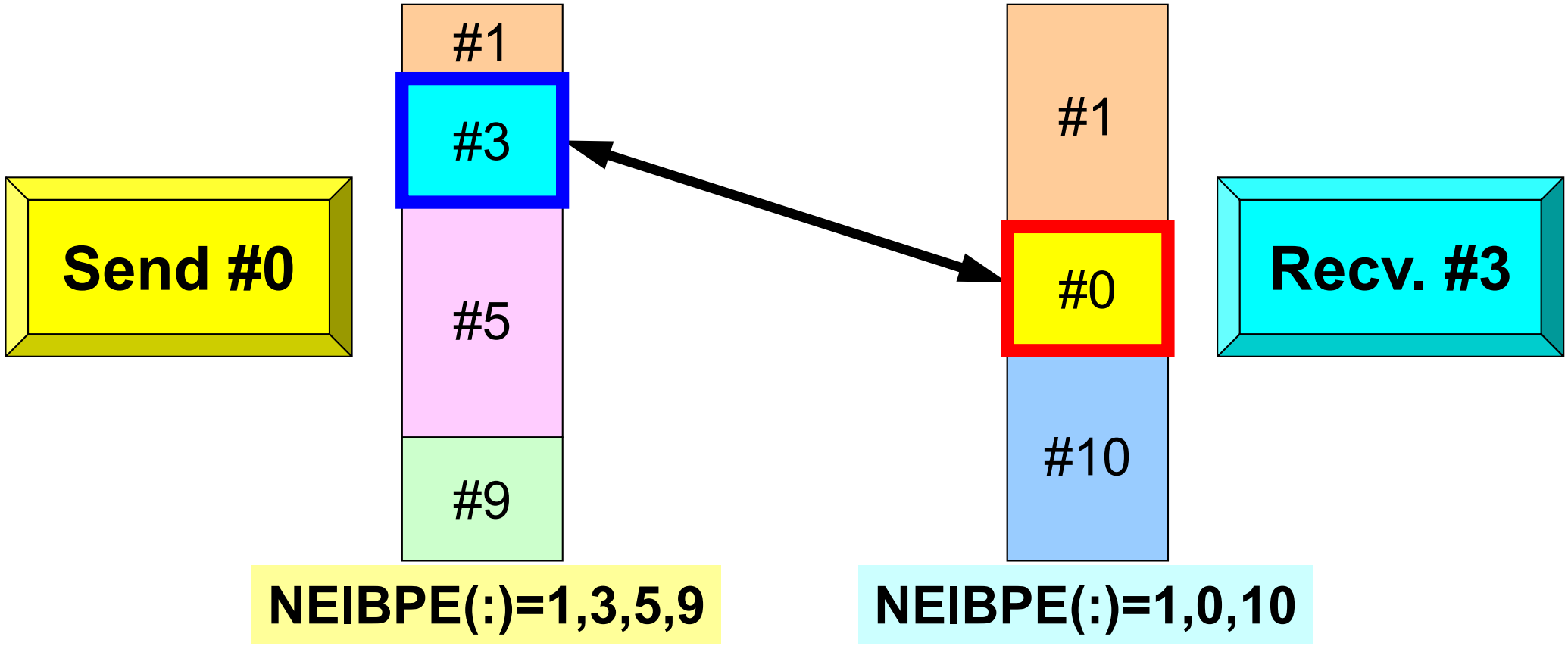
Relationship SEND/RECV

```
 do neib= 1, NEIBPETOT
   iS_e= export_index(neib-1) + 1
   iE_e= export_index(neib  )
   BUFlength_e= iE_e + 1 - iS_e

   call MPI_ISEND                                                  &
&         (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_send(neib), ierr)
  enddo
```

```
 do neib= 1, NEIBPETOT
   iS_i= import_index(neib-1) + 1
   iE_i= import_index(neib  )
   BUFlength_i= iE_i + 1 - iS_i

   call MPI_IRECV                                                  &
&         (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_recv(neib), ierr)
  enddo
```

- Consistency of ID’s of sources/destinations, size and contents of messages !
- Communication occurs when NEIBPE(neib) matches

Relationship SEND/RECV (#0 to #3)



- Consistency of ID's of sources/destinations, size and contents of messages !
- Communication occurs when NEIBPE(neib) matches

Generalized Comm. Table (1/6)

PE#2

PE#1

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORT_index
4  8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4  8
#EXPORT_items
4
8
12
16
13
14
15
16
```

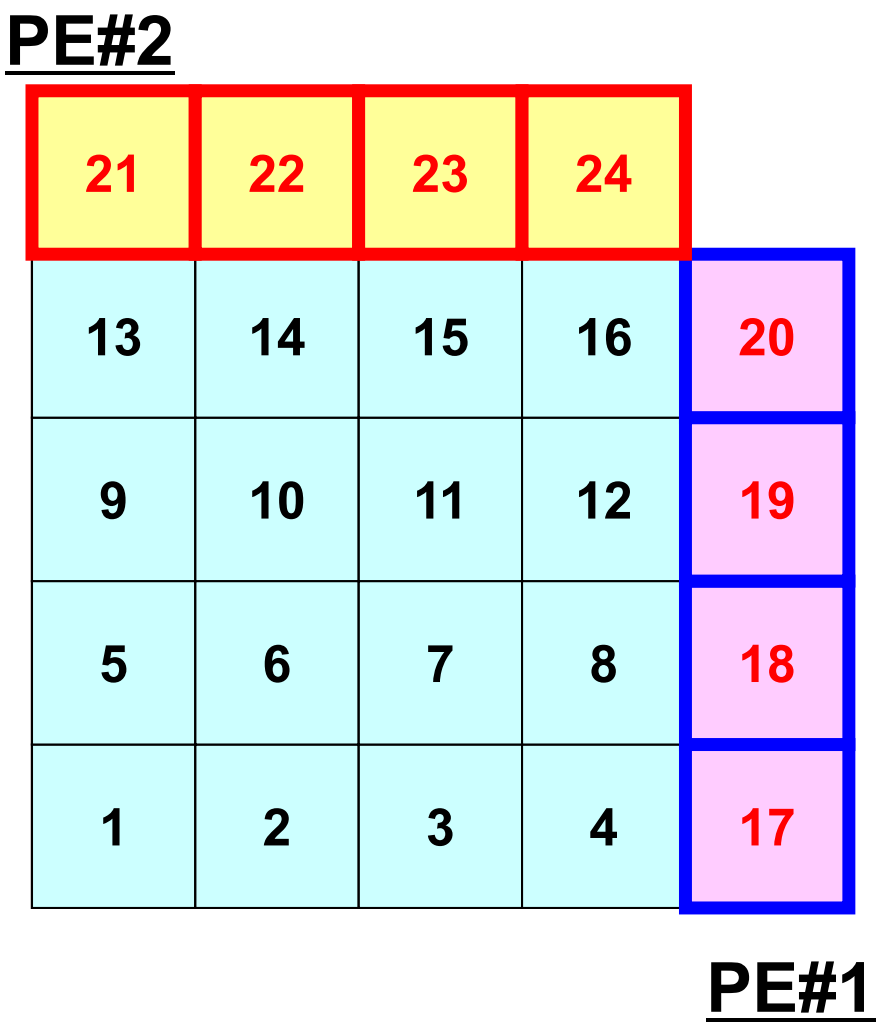
Generalized Comm. Table (2/6)

PE#2

PE#1

```
#NEIBPEtot    Number of neighbors
2
#NEIBPE       ID of neighbors
1  2
#NODE
24 16         Ext/Int Pts, Int Pts
#IMPORT_index
4  8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4  8
#EXPORT_items
4
8
12
16
13
14
15
16
```

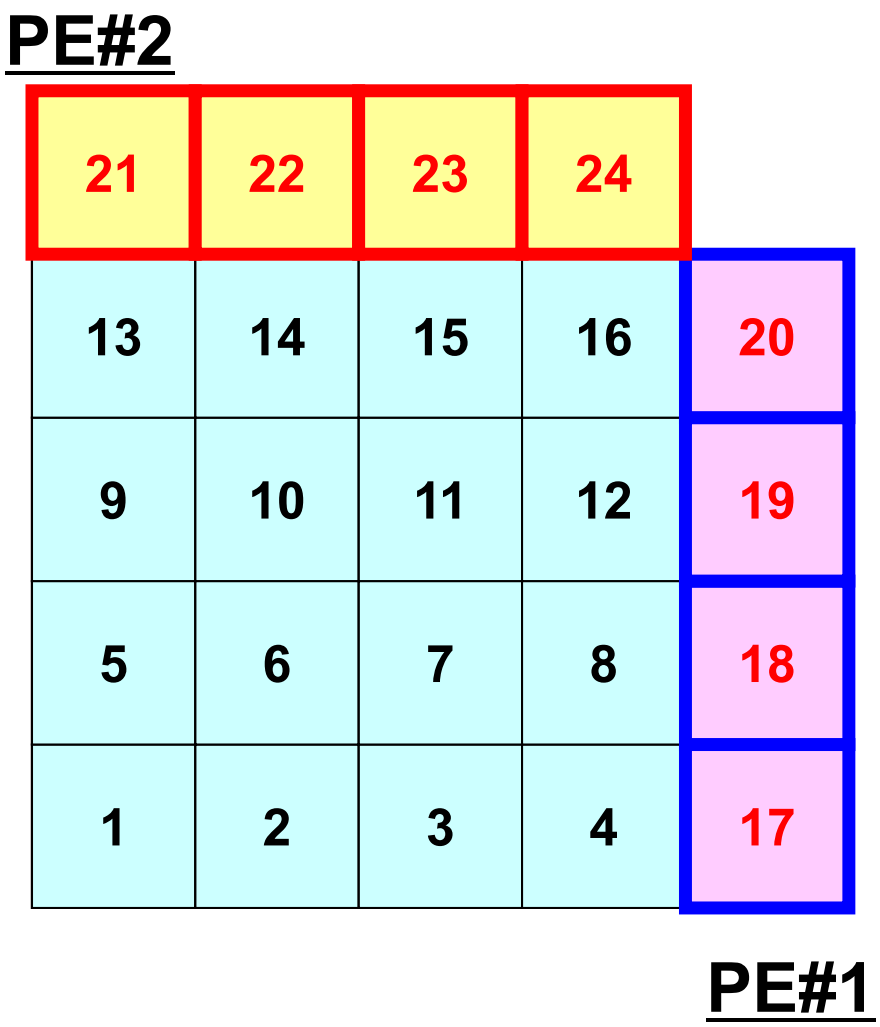
Generalized Comm. Table (3/6)




```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORT_index
4  8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4  8
#EXPORT_items
4
8
12
16
13
14
15
16
```

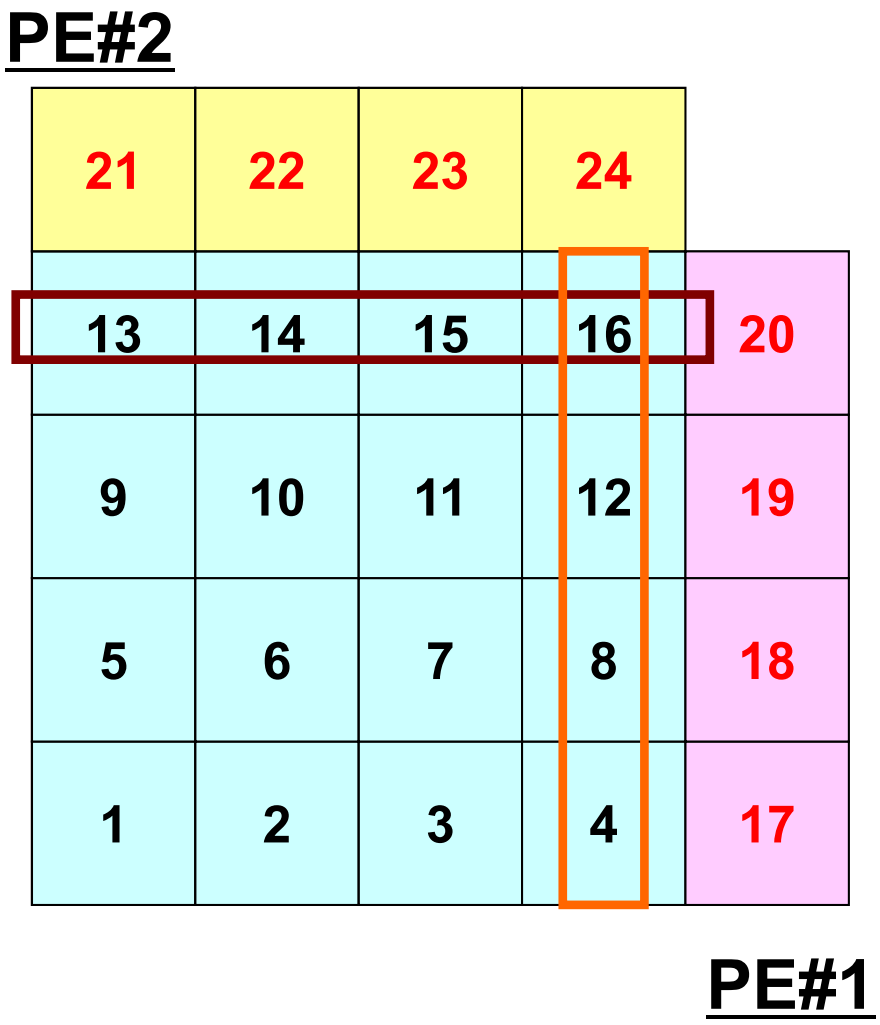
Four ext pts (1st-4th items) are imported from 1st neighbor (PE#1), and four (5th-8th items) are from 2nd neighbor (PE#2).

Generalized Comm. Table (4/6)




```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORT_index
4  8
#IMPORT_items
17
18          imported from 1st Neighbor
19          (PE#1) (1st-4th items)
20
21
22          imported from 2nd Neighbor
23          (PE#2) (5th-8th items)
24
#EXPORT_index
4  8
#EXPORT_items
4
8
12
16
13
14
15
16
```

Generalized Comm. Table (5/6)




```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORT_index
4  8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4  8
#EXPORT_items
4
8
12
16
13
14
15
16
```

Four boundary pts (1st-4th items) are exported to 1st neighbor (PE#1), and four (5th-8th items) are to 2nd neighbor (PE#2).

Generalized Comm. Table (6/6)

PE#2

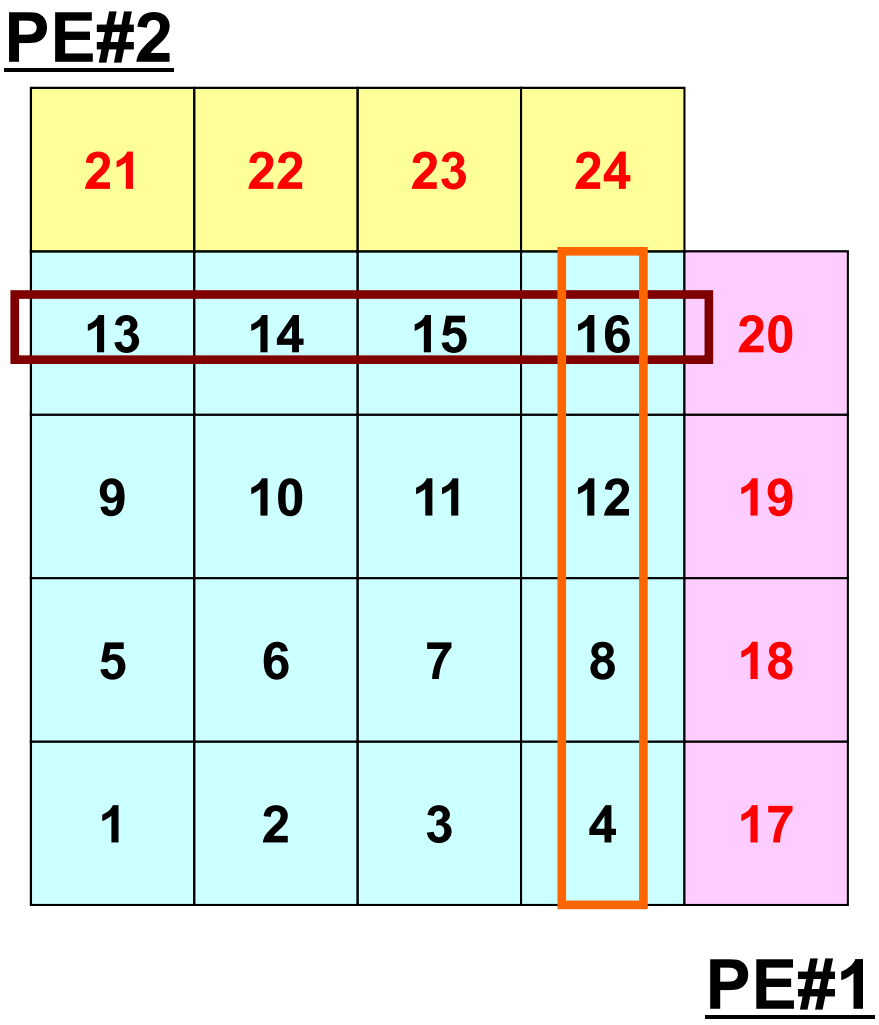
PE#1

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORT_index
4  8
#IMPORT_items
17
18
19
20
21
22
23
24
#EXPORT_index
4  8
#EXPORT_items
4
8
12
16
13
14
15
16
```

exported to 1st Neighbor (PE#1) (1st-4th items)

exported to 2nd Neighbor (PE#2) (5th-8th items)

Generalized Comm. Table (6/6)



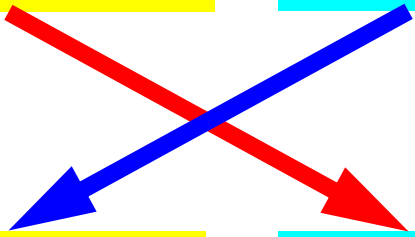
An external point is only sent from its original domain.

A boundary point could be referred from more than one domain, and sent to multiple domains (e.g. 16th mesh).

Notice: Send/Recv Arrays

```
#PE0
  send:
    VEC(start_send)~
    VEC(start_send+length_send-1)
```

```
#PE1
  send:
    VEC(start_send)~
    VEC(start_send+length_send-1)
```



```
#PE0
  recv:
    VEC(start_recv)~
    VEC(start_recv+length_recv-1)
```

```
#PE1
  recv:
    VEC(start_recv)~
    VEC(start_recv+length_recv-1)
```

- “length_send” of sending process must be equal to “length_recv” of receiving process.
  - PE#0 to PE#1, PE#1 to PE#0
- “sendbuf” and “recvbuf”: different address

Peer-to-Peer Communication

- What is P2P Communication ?
- 2D Problem, Generalized Communication Table
  - 2D FDM
  - Problem Setting
  - Distributed Local Data and Communication Table
  - Implementation
- Report S2

Sample Program for 2D FDM

```
$ cd <$O-S2>

$ mpifrtpx –Kfast sq-sr1.f
$ mpifccpx –Kfast sq-sr1.c

(modify go4.sh for 4 processes)
$ pjsub go4.sh
```

Example: sq-sr1.f (1/6)

Fortran

Initialization

```
      implicit REAL*8 (A-H,O-Z)
      include  'mpif.h'

      integer(kind=4) :: my_rank, PETOT
      integer(kind=4) :: N, NP, NEIBPETOT, BUFlength

      integer(kind=4), dimension(:), allocatable :: VAL
      integer(kind=4), dimension(:), allocatable :: SENDbuf, RECVbuf
      integer(kind=4), dimension(:), allocatable :: NEIBPE

      integer(kind=4), dimension(:), allocatable :: import_index, import_item
      integer(kind=4), dimension(:), allocatable :: export_index, export_item

      integer(kind=4), dimension(:,:), allocatable :: stat_send, stat_recv
      integer(kind=4), dimension(:  ), allocatable :: request_send
      integer(kind=4), dimension(:  ), allocatable :: request_recv

      character(len=80)          :: filename, line
!C
!C +-----------+
!C | INIT. MPI |
!C +-----------+
!C===
      call MPI_INIT      (ierr)
      call MPI_COMM_SIZE (MPI_COMM_WORLD, PETOT, ierr )
      call MPI_COMM_RANK (MPI_COMM_WORLD, my_rank, ierr )
```

Example: sq-sr1.f (2/6)

Fortran

Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N
        read (21,'(a80)') line
        read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                     nn= import_index(NEIBPETOT)
                     allocate (import_item(nn))
        do i= 1, nn
          read (21,*) import_item(i)
        enddo
        read (21,'(a80)') line
        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                     nn= export_index(NEIBPETOT)
                     allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

Example: sq-sr1.f (2/6)

Fortran

Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N

        read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                     nn= import_index(NEIBPETOT)
                     allocate (import_item(nn))
        do i= 1, nn
          read (21,*) import_item(i)
        enddo

        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                     nn= export_index(NEIBPETOT)
                     allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

Example: sq-sr1.f (2/6)

Fortran

Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N
        read (21,'(a80)') line
        do i= 1, nn
          read (21,*) import_item(i)
        enddo
        read (21,'(a80)') line
        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                    nn= export_index(NEIBPETOT)
                    allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

NP Number of all meshes (internal + external)

N Number of internal meshes

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

Example: sq-sr1.f (2/6)

Fortran

Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N

        read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                     nn= import_index(NEIBPETOT)
                     allocate (import_item(nn))
        do i= 1, nn
          read (21,*) import_item(i)
        enddo

        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                     nn= export_index(NEIBPETOT)
                     allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

Example: sq-sr1.f (2/6)

Fortran

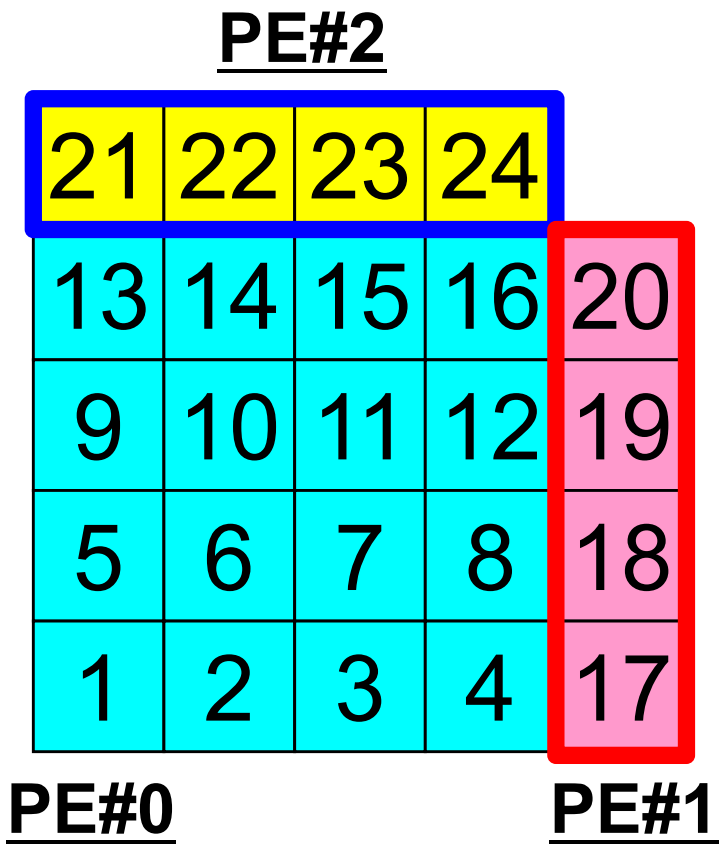
Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N

        read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                     nn= import_index(NEIBPETOT)
                     allocate (import_item(nn))
        do i= 1, nn
          read (21,*) import_item(i)
        enddo

        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                     nn= export_index(NEIBPETOT)
                     allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

RECV/Import: PE#0

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```



Example: sq-sr1.f (2/6)

Fortran

Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N

        read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                     nn= import_index(NEIBPETOT)
                     allocate (import_item(nn))
        do i= 1, nn
          read (21,*) import_item(i)
        enddo

        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                     nn= export_index(NEIBPETOT)
                     allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

Example: sq-sr1.f (2/6)

Fortran

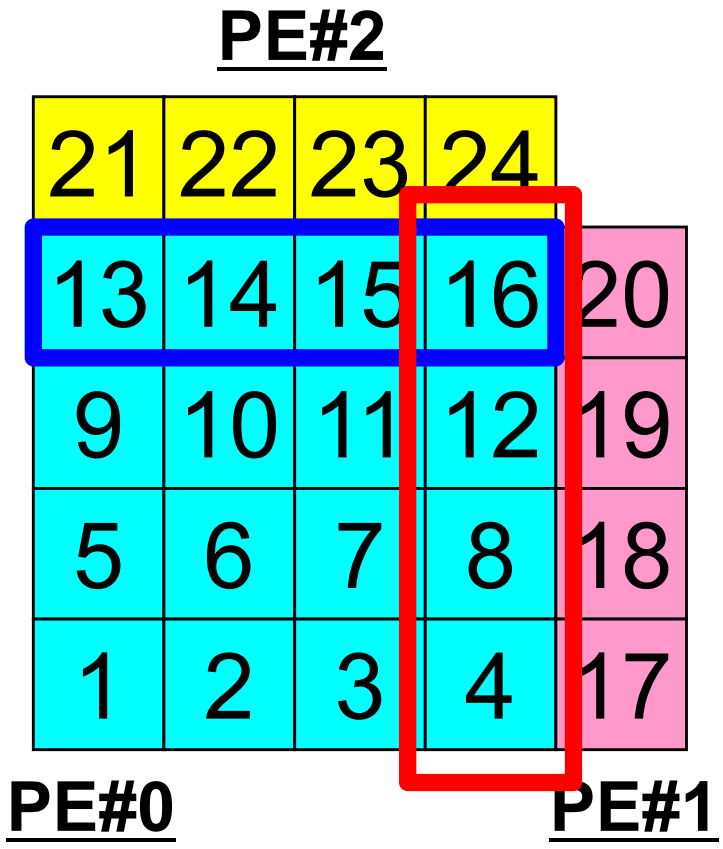
Reading distributed local data files (sqm.*)

```
!C
!C-- MESH
      if (my_rank.eq.0) filename= 'sqm.0'
      if (my_rank.eq.1) filename= 'sqm.1'
      if (my_rank.eq.2) filename= 'sqm.2'
      if (my_rank.eq.3) filename= 'sqm.3'
      open (21, file= filename, status= 'unknown')
        read (21,*) NEIBPETOT
                    allocate (NEIBPE(NEIBPETOT))
                    allocate (import_index(0:NEIBPETOT))
                    allocate (export_index(0:NEIBPETOT))
                              import_index= 0
                              export_index= 0
        read (21,*) (NEIBPE(neib), neib= 1, NEIBPETOT)
        read (21,*) NP, N

        read (21,*) (import_index(neib), neib= 1, NEIBPETOT)
                     nn= import_index(NEIBPETOT)
                     allocate (import_item(nn))
        do i= 1, nn
          read (21,*) import_item(i)
        enddo

        read (21,*) (export_index(neib), neib= 1, NEIBPETOT)
                     nn= export_index(NEIBPETOT)
                     allocate (export_item(nn))
        do i= 1, nn
          read (21,*) export_item(i)
        enddo
      close (21)
```

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

SEND/Export: PE#0

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```



Example: sq-sr1.f (3/6)

Fortran

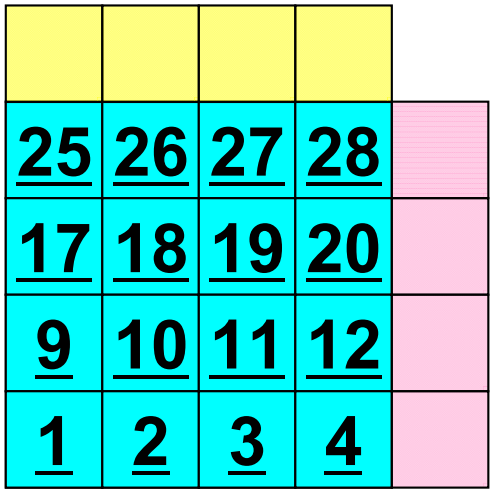
Reading distributed local data files (sq.*)

```
!C
!C-- VAL.
      if (my_rank.eq.0) filename= 'sq.0'
      if (my_rank.eq.1) filename= 'sq.1'
      if (my_rank.eq.2) filename= 'sq.2'
      if (my_rank.eq.3) filename= 'sq.3'

      allocate (VAL(NP))
      VAL= 0
      open (21, file= filename, status= 'unknown')
        do i= 1, N
          read (21,*) VAL(i)
        enddo
      close (21)
!C===
```

N : Number of internal points
VAL: Global ID of meshes

VAL on external points are unknown at this stage.

PE#2



PE#0 PE#1

```
1
2
3
4
9
10
11
12
17
18
19
20
25
26
27
28
```

Example: sq-sr1.f (4/6)

Fortran

Preparation of sending/receiving buffers

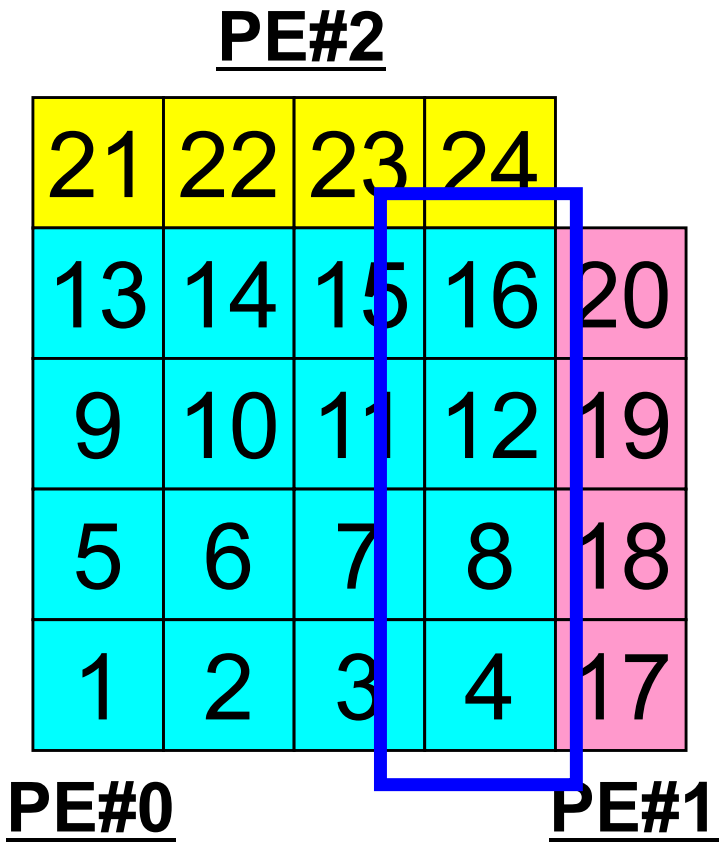
```
!C
!C +--------+
!C | BUFFER |
!C +--------+
!C===
      allocate (SENDbuf(export_index(NEIBPETOT)))
      allocate (RECVbuf(import_index(NEIBPETOT)))

      SENDbuf= 0
      RECVbuf= 0

      do neib= 1, NEIBPETOT
        iS= export_index(neib-1) + 1
        iE= export_index(neib  )
        do i= iS, iE
          SENDbuf(i)= VAL(export_item(i))
        enddo
      enddo
!C===
```

Info. of boundary points is written into sending buffer (**SendBuf**).
Info. sent to **NEIBPE(neib)** is **stored in export_index(neib-1)+1:export_inedx(neib)**

Sending Buffer is nice ...

Fortran

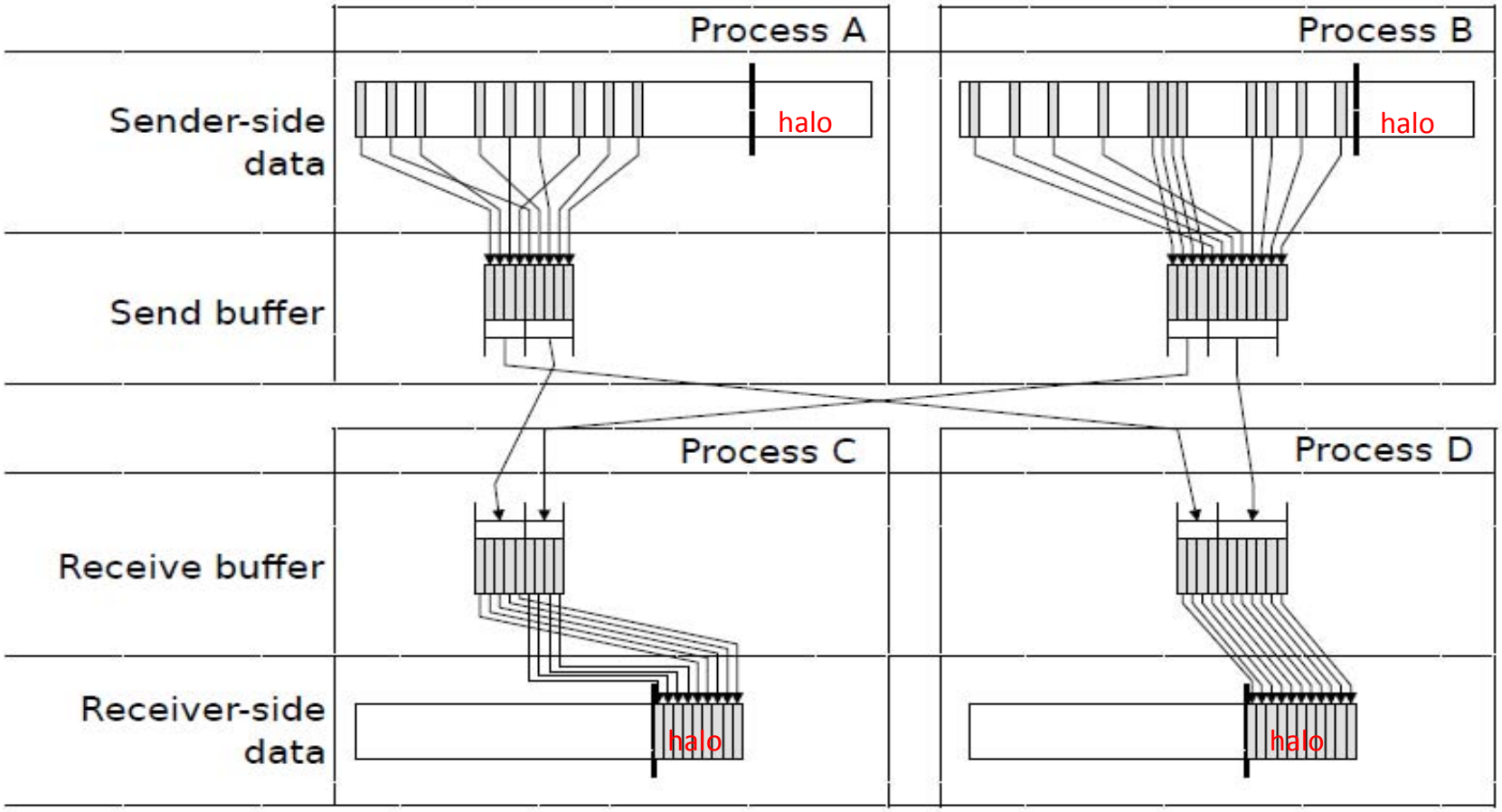
```
 do neib= 1, NEIBPETOT
   iS_e= export_index(neib-1) + 1
   iE_e= export_index(neib  )
   BUFlength_e= iE_e + 1 - iS_e

   call MPI_ISEND                                                  &
&         (VAL(...), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_send(neib), ierr)
 enddo
```



Numbering of these boundary nodes is not continuous, therefore the following procedure of MPI_Isend is not applied directly:

- Starting address of sending buffer
- XX-messages from that address

Communication Pattern using 1D Structure



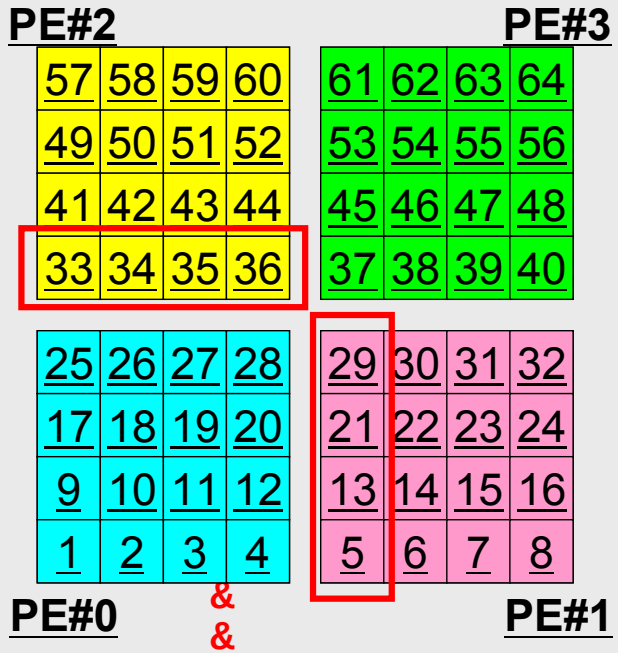
Dr. Osni Marques
（Lawrence Berkeley National Laboratory）より借用

Example: sq-sr1.f (5/6)

Fortran

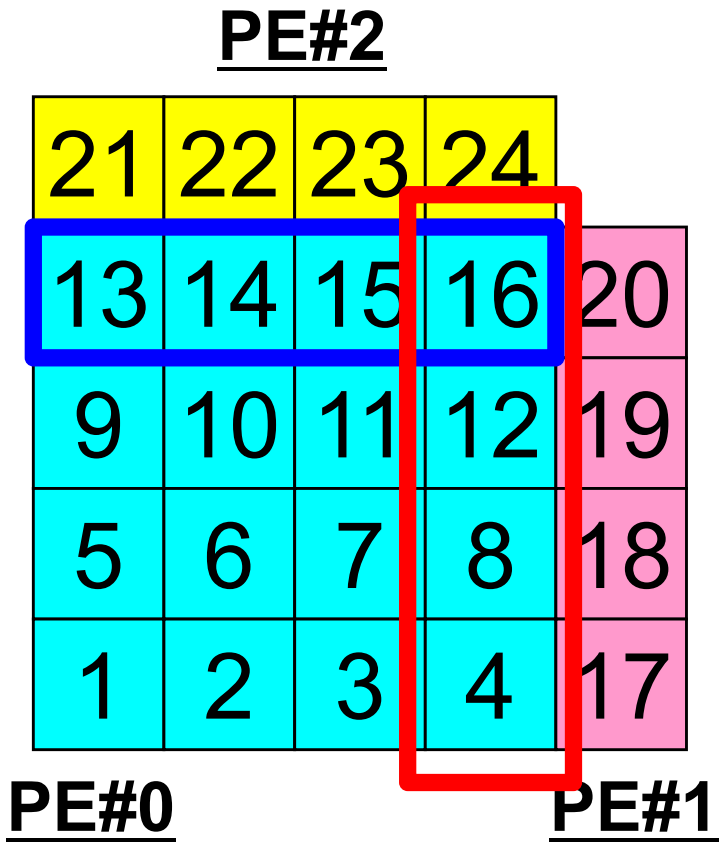
SEND/Export: MPI_Isend

```
!C
!C +-----------+
!C | SEND-RECV |
!C +-----------+
!C===
      allocate (stat_send(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (stat_recv(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (request_send(NEIBPETOT))
      allocate (request_recv(NEIBPETOT))

      do neib= 1, NEIBPETOT
        iS= export_index(neib-1) + 1
        iE= export_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_ISEND (SENDbuf(iS), BUFlength, MPI_INTEGER,
     &                  NEIBPE(neib), 0, MPI_COMM_WORLD,
     &                  request_send(neib), ierr)
      enddo

      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_IRECV (RECVbuf(iS), BUFlength, MPI_INTEGER,
     &                  NEIBPE(neib), 0, MPI_COMM_WORLD,
     &                  request_recv(neib), ierr)
      enddo
```

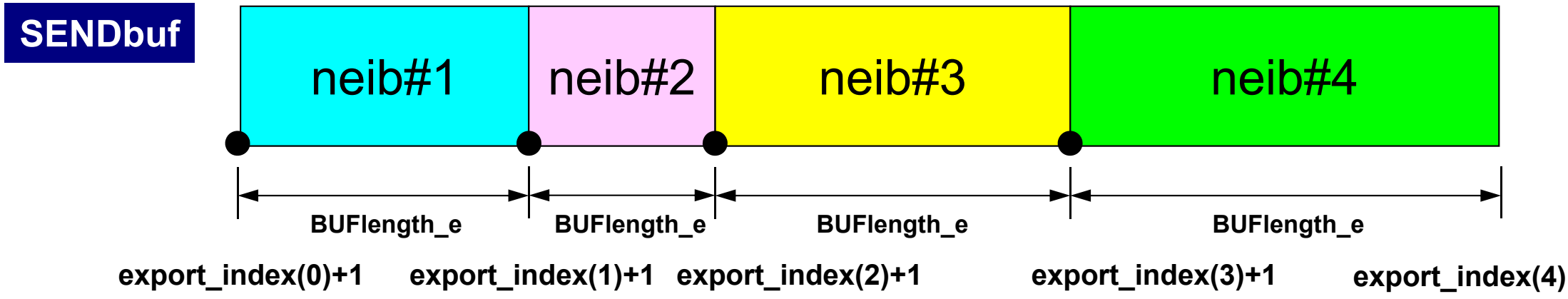


SEND/Export: PE#0

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```



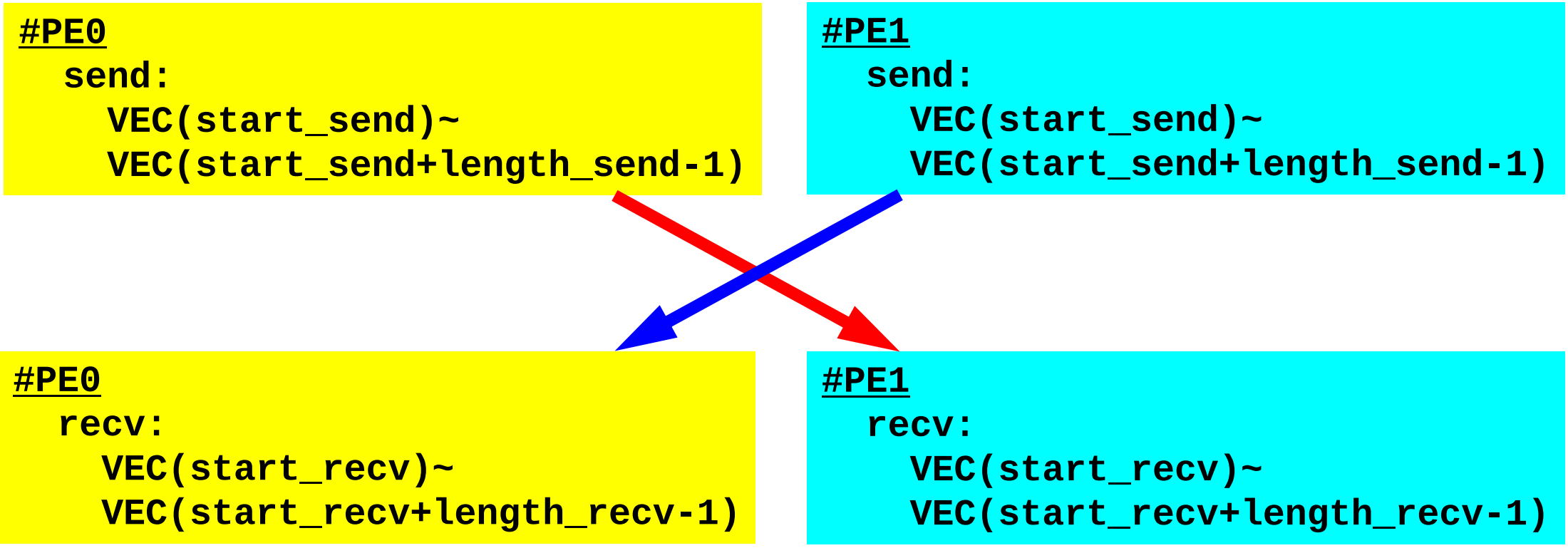
SEND: MPI_Isend/Irecv/Waitall Fortran




```
do neib= 1, NEIBPETOT
  do k= export_index(neib-1)+1, export_index(neib)
    kk= export_item(k)
    SENDbuf(k)= VAL(kk)
  enddo
enddo

do neib= 1, NEIBPETOT
  iS_e= export_index(neib-1) + 1
  iE_e= export_index(neib  )
  BUFlength_e= iE_e + 1 - iS_e

  call MPI_ISEND                                                    &
&         (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_send(neib), ierr)
enddo

call MPI_WAITALL (NEIBPETOT, request_send, stat_recv, ierr)
```

Copies to sending buffers

Notice: Send/Recv Arrays



- "length_send" of sending process must be equal to "length_recv" of receiving process.
  - PE#0 to PE#1, PE#1 to PE#0
- "sendbuf" and "recvbuf": different address

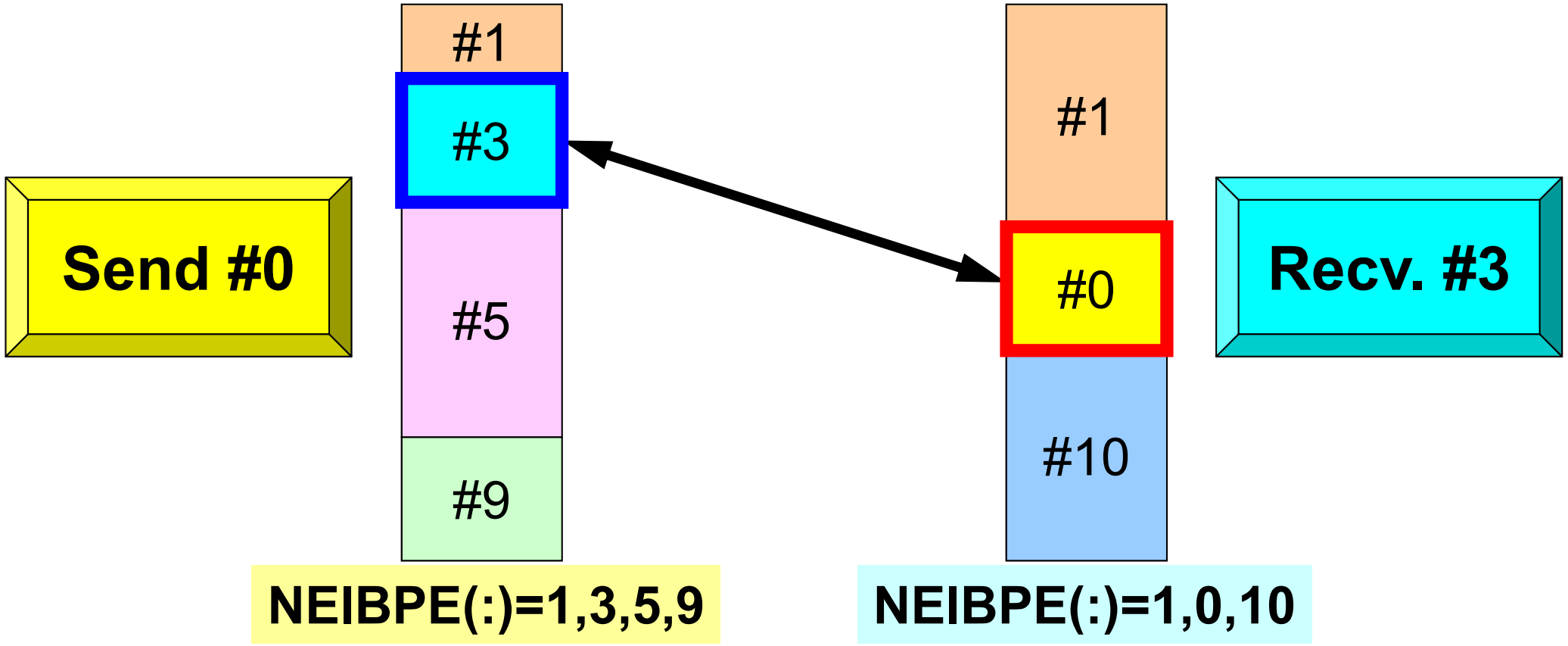
Relationship SEND/RECV

```
 do neib= 1, NEIBPETOT
   iS_e= export_index(neib-1) + 1
   iE_e= export_index(neib  )
   BUFlength_e= iE_e + 1 - iS_e

   call MPI_ISEND                                                  &
&         (SENDbuf(iS_e), BUFlength_e, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_send(neib), ierr)
  enddo
```

```
 do neib= 1, NEIBPETOT
   iS_i= import_index(neib-1) + 1
   iE_i= import_index(neib  )
   BUFlength_i= iE_i + 1 - iS_i

   call MPI_IRECV                                                  &
&         (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_recv(neib), ierr)
  enddo
```

- Consistency of ID’s of sources/destinations, size and contents of messages !
- Communication occurs when NEIBPE(neib) matches

Relationship SEND/RECV (#0 to #3)



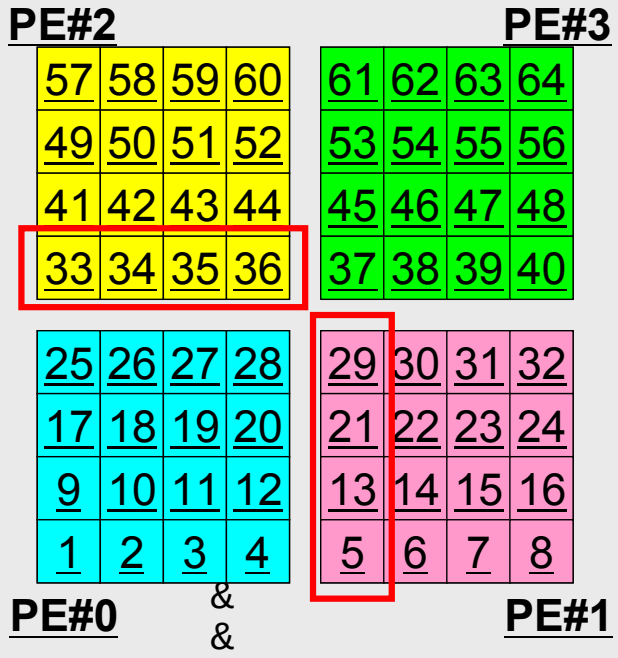
- Consistency of ID's of sources/destinations, size and contents of messages !
- Communication occurs when NEIBPE(neib) matches

Example: sq-sr1.f (5/6)

Fortran

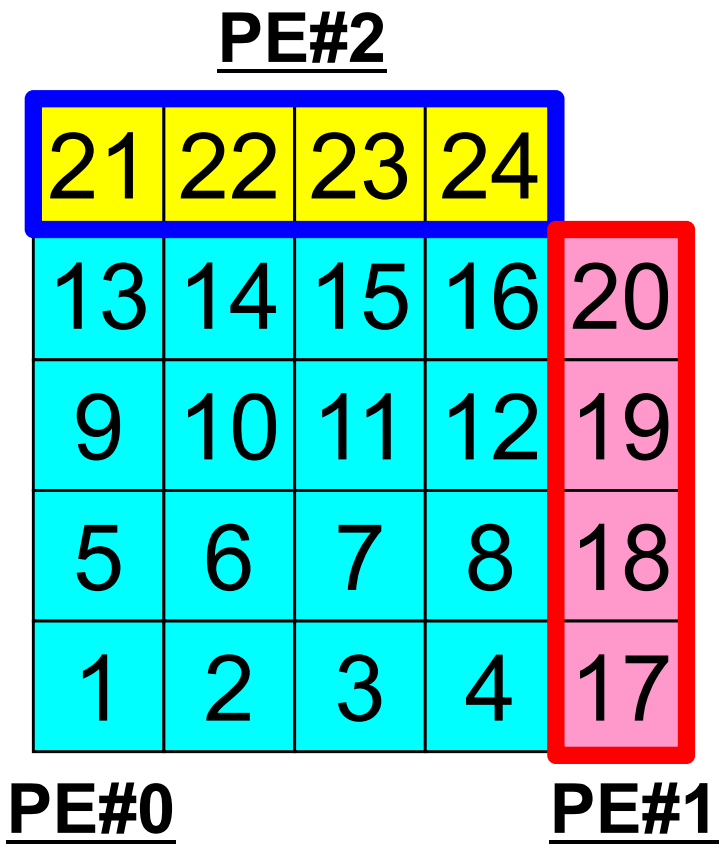
RECV/Import: MPI_Irecv

```
!C
!C +-----------+
!C | SEND-RECV |
!C +-----------+
!C===
      allocate (stat_send(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (stat_recv(MPI_STATUS_SIZE,NEIBPETOT))
      allocate (request_send(NEIBPETOT))
      allocate (request_recv(NEIBPETOT))

      do neib= 1, NEIBPETOT
        iS= export_index(neib-1) + 1
        iE= export_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_ISEND (SENDbuf(iS), BUFlength, MPI_INTEGER,
     &                  NEIBPE(neib), 0, MPI_COMM_WORLD,
     &                  request_send(neib), ierr)
      enddo

      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        BUFlength= iE + 1 - iS
        call MPI_IRECV (RECVbuf(iS), BUFlength, MPI_INTEGER,          &
     &                  NEIBPE(neib), 0, MPI_COMM_WORLD,              &
     &                  request_recv(neib), ierr)
      enddo
```



RECV/Import: PE#0

```
#NEIBPEtot
2
#NEIBPE
1  2
#NODE
24 16
#IMPORTindex
4  8
#IMPORTitems
17
18
19
20
21
22
23
24
#EXPORTindex
4  8
#EXPORTitems
4
8
12
16
13
14
15
16
```

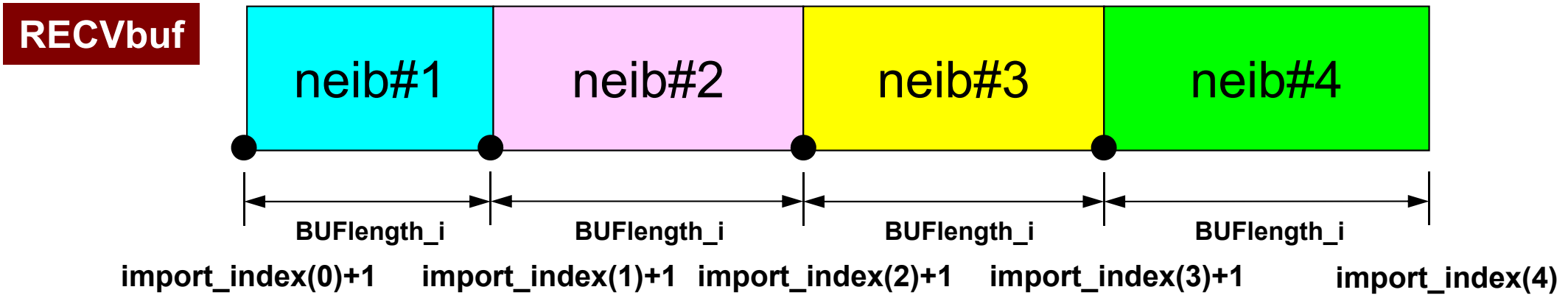


RECV: MPI_Isend/Irecv/Waitall

Fortran

```
 do neib= 1, NEIBPETOT
   iS_i= import_index(neib-1) + 1
   iE_i= import_index(neib  )
   BUFlength_i= iE_i + 1 - iS_i

   call MPI_IRECV                                                  &
&         (RECVbuf(iS_i), BUFlength_i, MPI_INTEGER, NEIBPE(neib), 0,&
&          MPI_COMM_WORLD, request_recv(neib), ierr)
  enddo

  call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

  do neib= 1, NEIBPETOT
     do k= import_index(neib-1)+1, import_index(neib)
       kk= import_item(k)
       VAL(kk)= RECVbuf(k)
     enddo
  enddo
```

Copies from receiving buffers



Example: sq-sr1.f (6/6)

Fortran

Reading info of ext pts from receiving buffers

```
      call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        do i= iS, iE
          VAL(import_item(i))= RECVbuf(i)
        enddo
      enddo

      call MPI_WAITALL (NEIBPETOT, request_send, stat_send, ierr)
!C===

!C
!C +--------+
!C | OUTPUT |
!C +--------+
!C===
      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        do i= iS, iE
          in= import_item(i)
          write (*,'(a, 3i8)') 'RECVbuf', my_rank, NEIBPE(neib), VAL(in)
        enddo
      enddo
!C===
      call MPI_FINALIZE (ierr)
      stop

      end
```

Contents of **RecvBuf** are copied to values at external points.

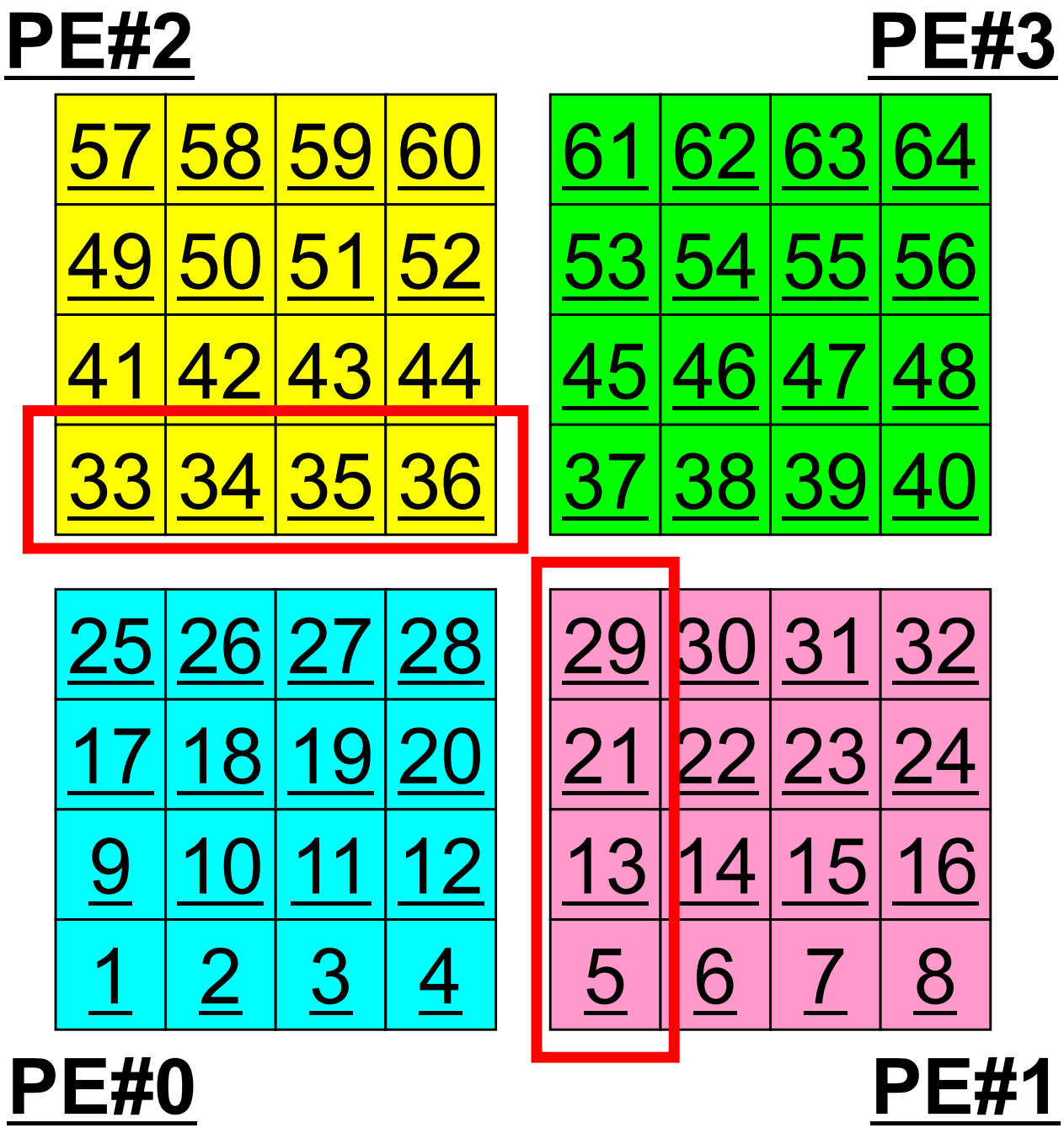
Example: sq-sr1.f (6/6)

Fortran

Writing values at external points

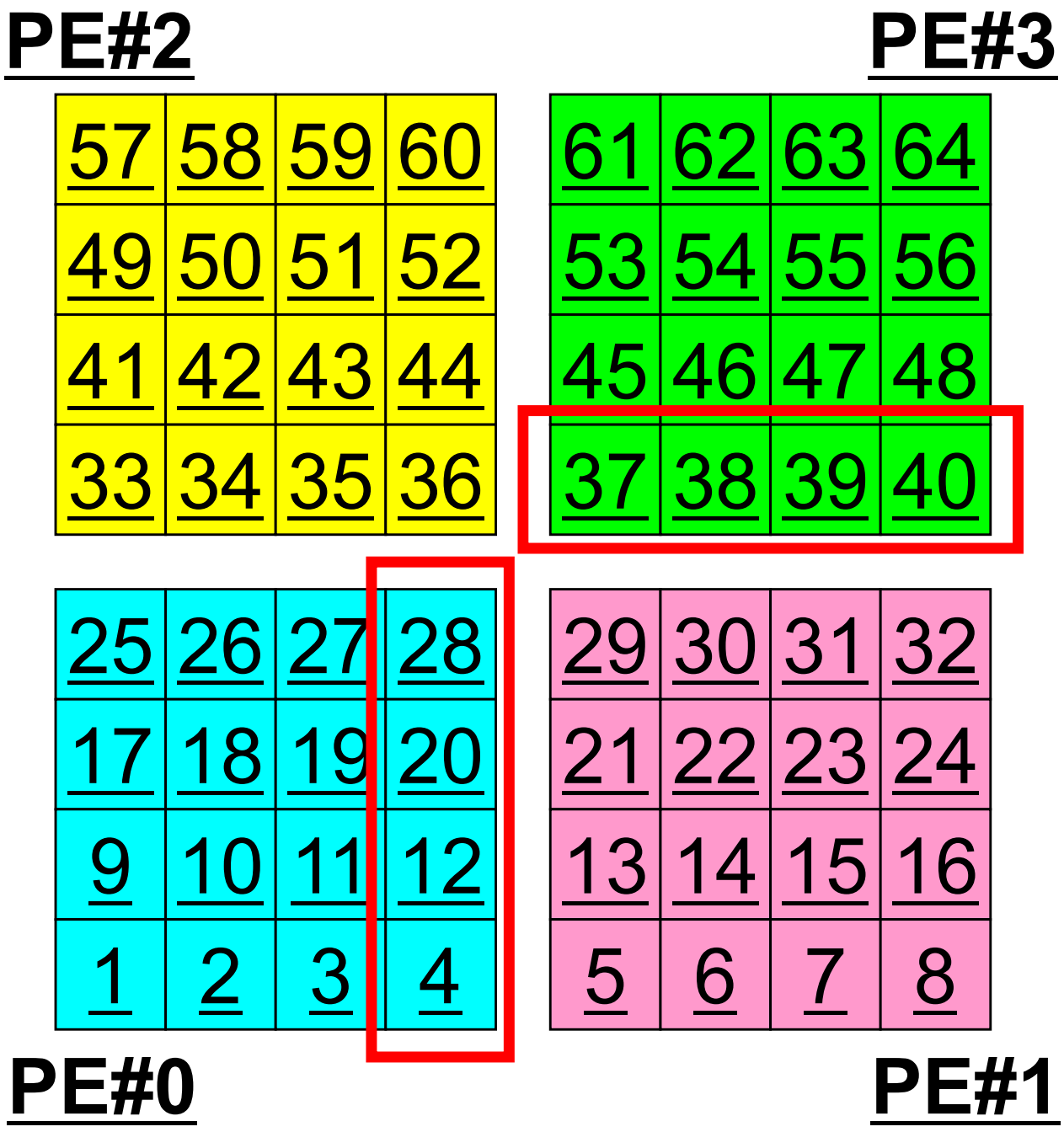
```
      call MPI_WAITALL (NEIBPETOT, request_recv, stat_recv, ierr)

      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        do i= iS, iE
          VAL(import_item(i))= RECVbuf(i)
        enddo
      enddo

      call MPI_WAITALL (NEIBPETOT, request_send, stat_send, ierr)
!C===

!C
!C +--------+
!C | OUTPUT |
!C +--------+
!C===
      do neib= 1, NEIBPETOT
        iS= import_index(neib-1) + 1
        iE= import_index(neib  )
        do i= iS, iE
          in= import_item(i)
          write (*,'(a, 3i8)') 'RECVbuf', my_rank, NEIBPE(neib), VAL(in)
        enddo
      enddo
!C===
      call MPI_FINALIZE (ierr)
      stop

      end
```

Results (PE#0)



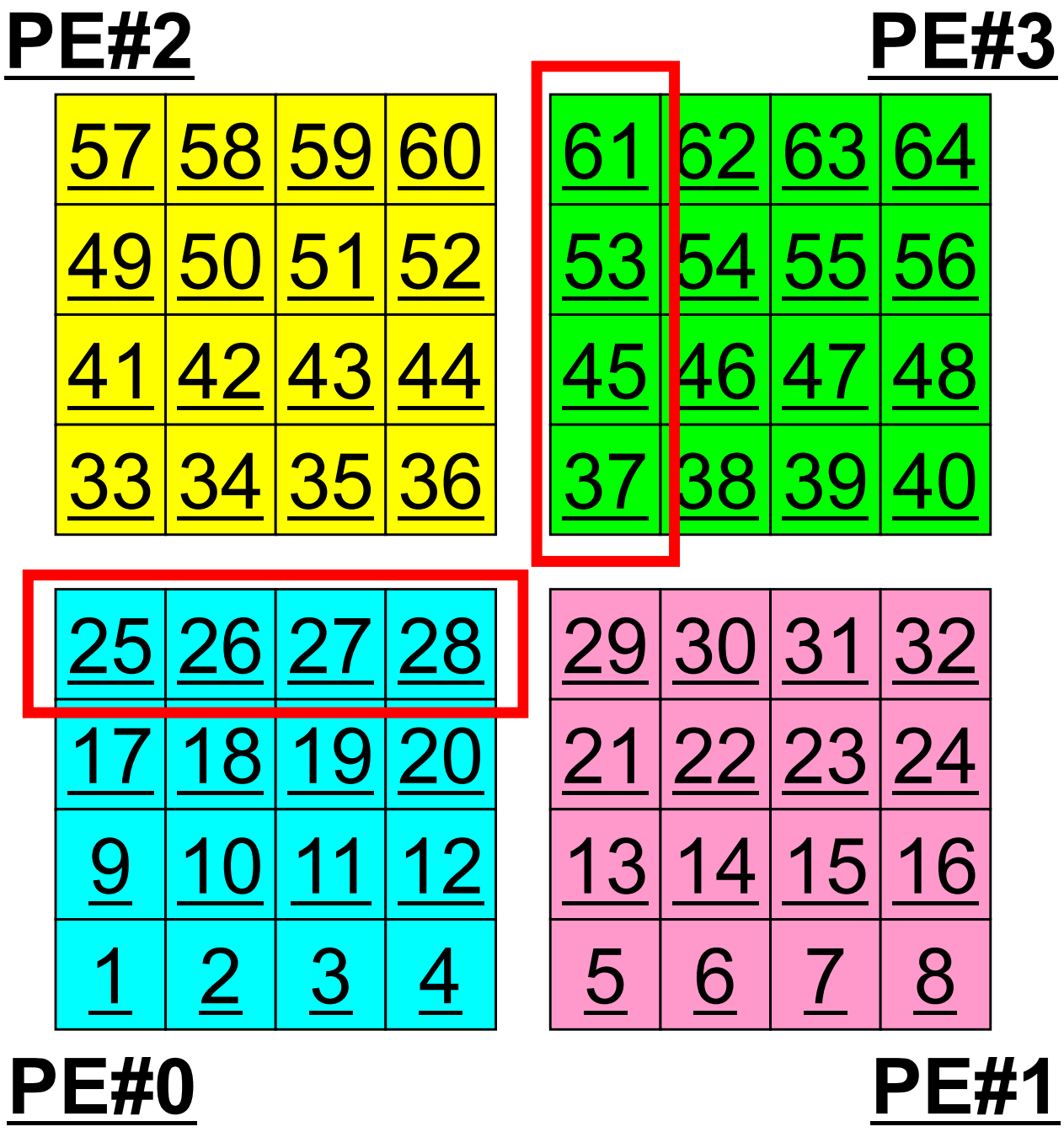

```
RECVbuf      0      1      5
RECVbuf      0      1     13
RECVbuf      0      1     21
RECVbuf      0      1     29
RECVbuf      0      2     33
RECVbuf      0      2     34
RECVbuf      0      2     35
RECVbuf      0      2     36

RECVbuf      1      0      4
RECVbuf      1      0     12
RECVbuf      1      0     20
RECVbuf      1      0     28
RECVbuf      1      3     37
RECVbuf      1      3     38
RECVbuf      1      3     39
RECVbuf      1      3     40

RECVbuf      2      3     37
RECVbuf      2      3     45
RECVbuf      2      3     53
RECVbuf      2      3     61
RECVbuf      2      0     25
RECVbuf      2      0     26
RECVbuf      2      0     27
RECVbuf      2      0     28

RECVbuf      3      2     36
RECVbuf      3      2     44
RECVbuf      3      2     52
RECVbuf      3      2     60
RECVbuf      3      1     29
RECVbuf      3      1     30
RECVbuf      3      1     31
RECVbuf      3      1     32
```

Results (PE#1)



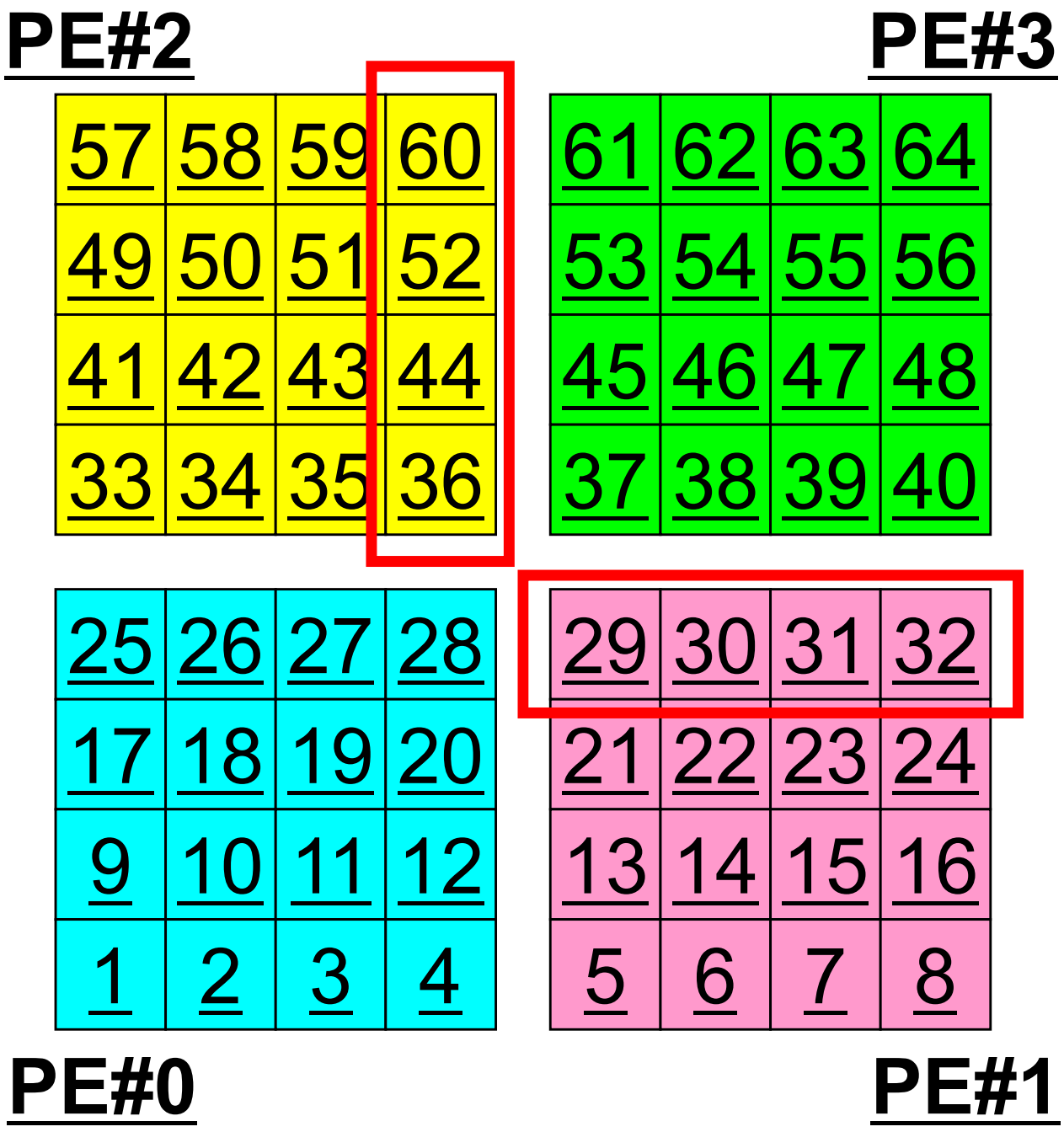

```
RECVbuf      0      1       5
RECVbuf      0      1      13
RECVbuf      0      1      21
RECVbuf      0      1      29
RECVbuf      0      2      33
RECVbuf      0      2      34
RECVbuf      0      2      35
RECVbuf      0      2      36

RECVbuf      1      0       4
RECVbuf      1      0      12
RECVbuf      1      0      20
RECVbuf      1      0      28
RECVbuf      1      3      37
RECVbuf      1      3      38
RECVbuf      1      3      39
RECVbuf      1      3      40

RECVbuf      2      3      37
RECVbuf      2      3      45
RECVbuf      2      3      53
RECVbuf      2      3      61
RECVbuf      2      0      25
RECVbuf      2      0      26
RECVbuf      2      0      27
RECVbuf      2      0      28

RECVbuf      3      2      36
RECVbuf      3      2      44
RECVbuf      3      2      52
RECVbuf      3      2      60
RECVbuf      3      1      29
RECVbuf      3      1      30
RECVbuf      3      1      31
RECVbuf      3      1      32
```

Results (PE#2)




```
RECVbuf      0      1       5
RECVbuf      0      1      13
RECVbuf      0      1      21
RECVbuf      0      1      29
RECVbuf      0      2      33
RECVbuf      0      2      34
RECVbuf      0      2      35
RECVbuf      0      2      36

RECVbuf      1      0       4
RECVbuf      1      0      12
RECVbuf      1      0      20
RECVbuf      1      0      28
RECVbuf      1      3      37
RECVbuf      1      3      38
RECVbuf      1      3      39
RECVbuf      1      3      40

RECVbuf      2      3      37
RECVbuf      2      3      45
RECVbuf      2      3      53
RECVbuf      2      3      61
RECVbuf      2      0      25
RECVbuf      2      0      26
RECVbuf      2      0      27
RECVbuf      2      0      28

RECVbuf      3      2      36
RECVbuf      3      2      44
RECVbuf      3      2      52
RECVbuf      3      2      60
RECVbuf      3      1      29
RECVbuf      3      1      30
RECVbuf      3      1      31
RECVbuf      3      1      32
```

Results (PE#3)




```
RECVbuf         0         1          5
RECVbuf         0         1         13
RECVbuf         0         1         21
RECVbuf         0         1         29
RECVbuf         0         2         33
RECVbuf         0         2         34
RECVbuf         0         2         35
RECVbuf         0         2         36

RECVbuf         1         0          4
RECVbuf         1         0         12
RECVbuf         1         0         20
RECVbuf         1         0         28
RECVbuf         1         3         37
RECVbuf         1         3         38
RECVbuf         1         3         39
RECVbuf         1         3         40

RECVbuf         2         3         37
RECVbuf         2         3         45
RECVbuf         2         3         53
RECVbuf         2         3         61
RECVbuf         2         0         25
RECVbuf         2         0         26
RECVbuf         2         0         27
RECVbuf         2         0         28

RECVbuf         3         2         36
RECVbuf         3         2         44
RECVbuf         3         2         52
RECVbuf         3         2         60
RECVbuf         3         1         29
RECVbuf         3         1         30
RECVbuf         3         1         31
RECVbuf         3         1         32
```

Distributed Local Data Structure for Parallel Computation

- Distributed local data structure for domain-to-doain communications has been introduced, which is appropriate for such applications with sparse coefficient matrices (e.g. FDM, FEM, FVM etc.).
  - SPMD
  - Local Numbering: Internal pts to External pts
  - Generalized communication table

- Everything is easy, if proper data structure is defined:
  - Values at boundary pts are copied into sending buffers
  - Send/Recv
  - Values at external pts are updated through receiving buffers

Initial Mesh

t2

21	22	23	24	25
16	17	18	19	20
11	12	13	14	15
6	7	8	9	10
1	2	3	4	5

Three Domains

t2

#PE2

21	22	23	24
16	17	18	19
11	12	13	14
6	7	8	

#PE1

23	24	25
18	19	20
13	14	15
8	9	10
	4	5

#PE0

11	12	13		
6	7	8	9	10
1	2	3	4	5

Three Domains

t2

#PE2

7 21	8 22	9 23	15 24
4 16	5 17	6 18	14 19
1 11	2 12	3 13	13 14
10 6	11 7	12 8	

#PE1

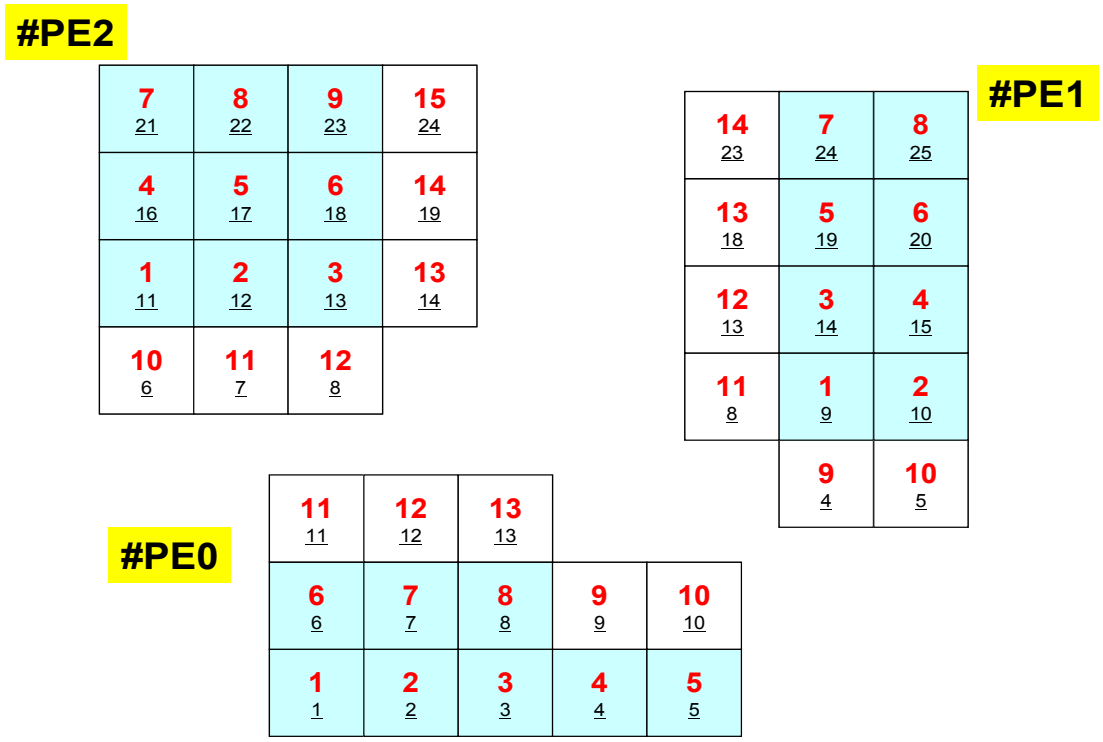
14 23	7 24	8 25
13 18	5 19	6 20
12 13	3 14	4 15
11 8	1 9	2 10
	9 4	10 5

#PE0

11 11	12 12	13 13		
6 6	7 7	8 8	9 9	10 10
1 1	2 2	3 3	4 4	5 5

t2

PE#0: sqm.0: fill ○'s




```
#NEIBPEtot
     2
#NEIBPE
     1    2
#NODE
    13    8  (int+ext, int pts)
#IMPORTindex
     ○    ○
#IMPORTitems
     ○…
#EXPORTindex
     ○    ○
#EXPORTitems
     ○…
```

t2

PE#1: sqm.1: fill ○'s

#PE2

7 21	8 22	9 23	15 24
4 16	5 17	6 18	14 19
1 11	2 12	3 13	13 14
10 6	11 7	12 8	

#PE1

14 23	7 24	8 25
13 18	5 19	6 20
12 13	3 14	4 15
11 8	1 9	2 10
	9 4	10 5

#PE0

11 11	12 12	13 13		
6 6	7 7	8 8	9 9	10 10
1 1	2 2	3 3	4 4	5 5

```
#NEIBPEtot
     2
#NEIBPE
     0     2
#NODE
    14     8 (int+ext, int pts)
#IMPORTindex
     ○     ○
#IMPORTitems
     ○…
#EXPORTindex
     ○     ○
#EXPORTitems
     ○…
```

t2

PE#2: sqm.2: fill ○'s

#PE2

7 21	8 22	9 23	15 24
4 16	5 17	6 18	14 19
1 11	2 12	3 13	13 14
10 6	11 7	12 8	

#PE1

14 23	7 24	8 25
13 18	5 19	6 20
12 13	3 14	4 15
11 8	1 9	2 10
	9 4	10 5

#PE0

11 11	12 12	13 13		
6 6	7 7	8 8	9 9	10 10
1 1	2 2	3 3	4 4	5 5

```
#NEIBPEtot
     2
#NEIBPE
     1     0
#NODE
    15     9 (int+ext, int pts)
#IMPORTindex
     ○     ○
#IMPORTitems
     ○…
#EXPORTindex
     ○     ○
#EXPORTitems
     ○…
```

t2

#PE2

7 21	8 22	9 23	15 24
4 16	5 17	6 18	14 19
1 11	2 12	3 13	13 14
10 6	11 7	12 8	

#PE1

14 23	7 24	8 25
13 18	5 19	6 20
12 13	3 14	4 15
11 8	1 9	2 10
	9 4	10 5

#PE0

11 11	12 12	13 13		
6 6	7 7	8 8	9 9	10 10
1 1	2 2	3 3	4 4	5 5

t2

Procedures

- Number of Internal/External Points
- Where do External Pts come from ?
  - **`IMPORTindex`**, **`IMPORTitems`**
  - Sequence of **`NEIBPE`**
- Then check destinations of Boundary Pts.
  - **`EXPORTindex`**, **`EXPORTitems`**
  - Sequence of **`NEIBPE`**

- “sq.*” are in <$O-S2>/ex
- Create “sqm.*” by yourself
- copy <$O-S2>/a.out (by sq-sr1.f) to <$O-S2>/ex
- pjsub go3.sh

Report S2 (1/2)

- Parallelize 1D code (1d.f) using MPI
- Read entire element number, and decompose into sub-domains in your program

- Measure parallel performance

Report S2 (2/2)

- Deadline: 17:00 October 24th (Sat), 2015.
  - Send files via e-mail at **nakajima(at)cc.u-tokyo.ac.jp**
- Problem
  - Apply “Generalized Communication Table”
  - Read entire elem. #, decompose into sub-domains in your program
  - Evaluate parallel performance
    - You need huge number of elements, to get excellent performance.
    - Fix number of iterations (e.g. 100), if computations cannot be completed.
- Report
  - Cover Page: Name, ID, and Problem ID (S2) must be written.
  - Less than eight pages including figures and tables (A4).
    - Strategy, Structure of the Program, Remarks
  - Source list of the program (if you have bugs)
  - Output list (as small as possible)